# LOCAS - a Low Coverage Assembler for Next Generation Sequencing and Resequencing Data 

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## Abstract

Within the last five years, a new generation of sequencing technologies has dramatically reduced cost and at the same time increased throughput of genome sequencing. For most application fields these technologies have proven to be good alternatives to the traditional Sanger sequencing although they generate shorter read sequences. For the study of sequence variations like SNPs, indels and longer variant regions between highly related genomes, resequencing has become increasingly popular. Such analyses help to reveal the impact of sequence variations on responses to the environment and in developing diseases. They are, thus, of great interest to disease control, personal genomics and phylogenetic studies.

Currently, the most popular approach to resequencing large and complex genomes is the mapping-consensus approach. It maps the read sequences to a highly related reference genome and from the alignment calculates a consensus sequence which can be compared to the reference genome. Unfortunately, only SNPs and small indels can be detected with this approach. A more promising approach is homology-guided assembly. Here, the reads are mapped against a reference sequence and the layout of the reads is refined before the calculation of the consensus sequence. This method has the capability to additionally reveal the sequences of longer variant regions such as long insertions.

In this thesis, I present an extension to homology-guided assembly that aims at assembling not only regions that are homologous between the target and reference genome but also longer variant regions. After the reads have been mapped to the reference sequence, the reference sequence is partitioned into regions of a fixed length, called blocks. In a reassembly step, the reads of each pair of consecutive blocks are assembled together. In order to also find long variant regions, reads that cannot be mapped onto the reference genome, so called left-over reads, are recruited and incorporated in the assembly of the current blocks.

The main focus of this work was on the development of assembly algorithms for current resequencing projects. To meet the needs of these projects the developed algorithms were especially designed for short read data at low sequencing depth. Furthermore, this work comprises extensions to these assembly algorithms, which are used in the reassembly step of our homology-guided assembly approach. These algorithms additionally incorporate left-over reads in the assembly and can utilize mapping positions that are available for the reads. The assembly algorithms are implemented in the assembly tool LOCAS (Low Coverage ASsembly) and its extension SUPERLOCAS.

The developed tools were evaluated and compared to state-of-the-art assemblers on short read data within a homology-guided assembly approach. For this purpose,
resequencing scenarios with a low sequencing depth were simulated. In the first study, which simulated assemblies of blocks, LOCAS showed better or comparable results regarding error rate and contig size while producing contigs with the best trade-off between both measures. In the second study, which simulated assemblies of blocks with the incorporation of left-over reads, SUPERLOCAS proved to be the superior tool regarding contig size, error rate and runtime while assembling the same amount of long insertion regions as comparable assemblers. In a third study, which used real world data, LOCAS and SUPERLOCAS performed similar as in the simulated studies. In all studies both tools proved to be very robust to different parameter settings.

In conclusion, my homology-guided assembly approach overcomes the problems of the mapping-consensus approach. In addition to homologous regions, it also assembles longer variant regions. Compared to other assembly methods, LOCAS and SUPERLOCAS are well suited for reassembly and show superior performances in this scenario.

## Zusammenfassung

Eine neue Generation von Sequenziertechnologien hat in den letzten fünf Jahren die Kosten für die Genomsequenzierung deutlich verringert und gleichzeitig den Sequenzierdurchsatz erhöht. Die neuen Sequenziertechnologien haben sich in vielen Anwendungsgebieten als vielversprechende Alternative zur traditionellen Sangersequenzierung erwiesen, obwohl die erzeugten Sequenzfragmente, welche als Reads bezeichnet werden, deutlich kürzer sind. Zur Untersuchung von Punktmutationen (SNPs), kleinen Insertionen und Deletionen (Indels) sowie längeren variablen Bereichen von nahverwandten Genomen wird inzwischen immer häufiger das Verfahren der Resequenzierung eingesetzt. Mit diesem Analyseverfahren kann die Bedeutung von Sequenzvariationen bei Krankheiten oder in der Reaktion auf die Umwelt festgestellt werden. Daher ist die Resequenzierung von großem Interesse bei der Kontrolle von Krankheiten, in Bereich Personal-Genomics und in phylogenetischen Studien.

Momentan wird bei der Resequenzierung von langen und komplexen Genomen vor allem der Mapping-Consensus Ansatz verwendet. Dabei werden die Reads gegen ein nahverwandtes Referenzgenom aligniert und die Consensus-Sequenz der alignierten Reads berechnet, sodass diese mit der Referenzsequenz verglichen werden kann. Da die Reads meist nur diskontinuierlich aligniert werden können, besteht die Consensus-Sequenz meist aus mehreren Teilsequenzen, welche als Contigs bezeichnet werden. Der Nachteil bei diesem Ansatz ist, dass meist nur SNPs und Indels bestimmt werden können, während lange variable Bereiche unentdeckt bleiben. Ein Ansatz, der hierfür weitaus erfolgversprechender ist, ist das Homology-Guided Assembly. Hier werden die Reads ebenfalls gegen eine Referenzsequenz aligniert. Jedoch wird die Anordnung der Reads anschließend noch einmal verbessert, bevor schließlich die Consensus-Sequenz berechnet wird. Dieser Ansatz hat das Potenzial auch die Sequenz von längeren variable Bereichen, wie langen Insertionen, zu bestimmen.

In meiner Dissertation stelle ich einen erweiterten Ansatz des Homology-Guided Assemblies vor. Durch diesen neuen Ansatz werden nicht nur homologe Bereiche des Referenz- und Zielgenoms assembliert sondern auch lange variable Bereiche. Nachdem die Reads gegen die Referenzsequenz aligniert worden sind, wird die Referenzsequenz in Abschnitte einer festen Länge unterteilt, welche als Blocks bezeichnet werden. Diese Blocks werden anschließend reassembliert, d.h., alle Reads die zu zwei aufeinanderfolgenden Blocks zugeordnet sind werden miteinander assembliert. Dabei werden Reads, die nicht gegen das Referenzgenom aligniert werden konnten (Left-Over Reads), in das Assembly eingebaut, sodass auch lange variable Bereiche assembliert werden können.

Der Hauptaugenmerk meiner Arbeit lag auf der Entwicklung von Assemblierungsalgorithmen, die in Resequenzierungsprojekten, welche die neue Generation der Sequenziertechnologien nutzen, angewendet werden können. Um den Anforderungen dieser Projekte Rechnung zu tragen, wurden die Algorithmen speziell an eine kurze Länge der Reads und an eine niedrige Sequenziertiefe angepasst. Darüber hinaus wurden die Algorithmen so erweitert, dass sie auch zur Reassemblierung genutzt werden können. Durch diese Erweiterung werden auf eine effiziente Weise auch Left-Over Reads mit in das Assembly einbezogen. Weiterhin können eventuell vorhandene Positionen der Reads bezüglich der Referenzsequenz für die Assemblierung genutzt werden. Die Algorithmen wurden in das Assemblierungsprogramm LOCAS bzw. in dessen Erweiterung SUPERLOCAS implementiert.

Die entwickelte Software wurde in einer Vergleichsstudie evaluiert und mit anderen aktuellen Assemblern verglichen. Die Assembler wurden zur Reassemblierung innerhalb des beschriebenen Homology-Guided Assembly Ansatzes verwendet. Zu diesem Zweck wurden kurze Reads mit einer niedrigen Sequenziertiefe innerhalb von Resequenzierungsszenarien simuliert. In der ersten Studie, welche die Reassemblierung von Blocks simulierte, erzielte LOCAS bessere oder vergleichbare Ergebnisse bezüglich der Fehlerrate und der Contig-Länge. Gleichzeitig erreichte es den besten Kompromiss zwischen beiden Maßen. In der zweiten Studie, welche die Reassemblierung von Blocks unter Einbeziehung von Left-Over Reads simulierte, stellte sich SUPERLOCAS als der beste Assembler bezüglich der Contig-Länge, der Fehlerrate und der Laufzeit heraus. In einer dritten Studie, die auf realen Daten basierte, zeigten LOCAS und SUPERLOCAS die gleiche Leistung wie in den Simulationsstudien. In allen Studien waren beide Assembler sehr robust gegenüber unterschiedlichen Parametereinstellungen.

Aus den Ergebnissen dieser Arbeit lässt sich folgern, dass die angesprochenen Probleme des Mapping-Consensus Ansatzes durch den vorgestellten HomologyGuided Assembly Ansatz in weiten Punkten gelöst werden. Zusätzlich zu den homologen Bereichen werden nun auch längere variable Bereiche assembliert. LOCAS und SUPERLOCAS erwiesen sich für die Reassemblierung von Genomen innerhalb des Homology-Guided Assembly-Ansatzes als sehr geeignete Assembler, da sie ausgezeichnete Ergebnisse für dieses Szenario erzielten.

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In accordance with the standard scientific protocol, I will use the personal pronoun "we" to indicate the reader and the writer, or my scientific collaborators and myself.

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## 1. Introduction

Studying sequence variation, like single-nucleotide polymorphisms (SNPs), insertions and deletions, is important in disease genetics and pharmacogenomic studies. The alteration of SNP positions or appearance of insertions and deletions within gene sequences causes alterations in the function of proteins. Thus, these events can result in diseases, changed responses to drugs or environmental toxins and behavioral modifications.

The investigation of SNPs and other sequence variations in plants is essential for dealing with the growing world population in the future. Especially, sequence variations that have an effect on resistance and yield gain of cultured plants are of great interest. Consequently, these variations and their effects are widely studied in model organisms like Arabidopsis thaliana. Array-based genotyping, such as methods supported by Illumina and Affymetrix, has been the most prominent approach to investigate sequence variations. Due to advances in Second Generation Sequencing technologies (SGS, also called Next Generation Sequencing), whole genome resequencing studies have come as an alternative approach into focus. Popular examples are the 1000 Genomes Project, which aims at finding genetic variants that have frequencies of at least $1 \%$ in the human population, and the 1001 Genomes Project, which aims at discovering such variations in A. thaliana.

Since their introduction in 2005, SGS technologies have increased the throughput and cost-efficiency of sequencing by an order of magnitude. For example, at present, the Illumina Genome Analyzer GAllx, which became commercially available in 2009, can produce up to 10 Gb of sequence in less than three days, while the latest sequencer of Illumina, the HiSeq 2000 system, yields up to 100 Gb in the same amount of time. While the accuracy of new sequencing technologies is similar to that of Sanger sequencing, the achievable read length has decreased from 1 kbp to less than 500 bases for the GS FLX Titanium instrument from Roche/454 Life Sciences or to around 100 bases or less for Illumina's GAllx or HiSeq and Applied Biosystem's SOLiD instruments.

The SGS technologies are used in resequencing studies that investigate variations between strains of the same organism or closely related species. Usually, a known genome is used as reference genome in a mapping or mapping-consensus approach, in which the reads are aligned to the reference sequence to detect variations between the reference genome and the target genome. While this allows for the detection of small variations like SNPs or short insertions and deletions, so called indels, regions with high divergence or long insertions will not be represented in the resulting consensus sequence as the respective reads are often not alignable to the reference sequence.

An alternative approach is de novo assembly which calculates overlaps between reads to assemble longer sequences, which are called contigs. De novo assembly does not rely on alignments of reads onto a reference genome and, thus, is also capable of assembling highly polymorphic and longer insertion regions. Unfortunately, the de novo assembly of large genomes and genomes with complex regions that were sequenced with SGS technology still faces unsolved issues. Such assemblies result in large numbers of short contigs and demand high amounts of memory.

For short read data, neither the mapping-consensus approach nor de novo assembly can be utilized to detect longer variations in complex eukaryotic genomes. Thus, a novel assembly approach is required that detects all variations in a complex and large target genome, including longer insertions and polymorphic regions. Several strategies have been proposed to increase the number of detected variant regions, like reduced representation libraries $\left[\overline{\left.\mathrm{KUA}^{+} 07\right]}\right.$ and gene-boosted assembly [SSPL08]. In addition, other approaches that detect rearrangements in the target genome from read quantity or mate-pair data have been introduced. However, these approaches do not reveal additional sequence information. Only the homology-guided assembly [PPDS04, $\left.\mathrm{RKD}^{+} 09\right]$ approach has the potential to assemble eukaryotic genomes with longer variations. It combines the mappingconsensus approach with de novo assembly.

Comparable to the mapping-consensus approach, homology-guided (or comparative) assembly makes use of an available reference genome. The homology-guided assembly strategy presented in this thesis starts with aligning short reads to a reference genome followed by the local assemblies of reads that have been aligned within the same regions. These regions are called blocks. In the assembly of the blocks, also non-alignable reads, so called left-over reads, can be incorporated to reveal additional sequence information of the target genome, which often originates from insertions or highly polymorphic regions. This process of assembly and incorporation is called reassembly.
Currently, available assembly tools, such as VELVET ZB08, ZMMB09, EULER-SR [CP08], ABySS [SWJ+ 09] and SOAPdenovo [LLZ+ 09], do not provide time-efficient methods for problems that arise in reassembly such as the incorporation of left-over reads in a consecutive execution of multiple local assemblies. The set of left-over reads can be huge compared to the set of reads belonging to a block. Furthermore, it consists not only of reads from highly polymorphic regions but also of erroneous reads, which, in our experience, can comprise about $5 \%$ to $20 \%$ of all reads from a sample. Since existing assemblers do not distinguish between aligned reads and left-over reads, they would have to assemble each block using all left-over reads, leading to an unacceptable increase in runtime.

The reassembly problem becomes even more difficult in the context of genome resequencing projects that are performed at low sequencing depth. The choice to sequence with a low depth results from a simple cost-benefit analysis: Even with a sequencing depth of 7 x , most of the reference genome is covered by aligned reads, enabling the detection of most SNPs and small indels. Current state-of-
the-art assemblers for short reads calculate exact sub-sequence matches ( $k$-mers) of the input reads, represent this information in a de Bruijn graph and extract finally contigs from the graph. Thus, these assemblers do not calculate overlap alignments between reads, i.e., alignments that involve the ends of both read sequences, and, consequently, cannot detect overlaps of reads with a substantial number of mismatches. However, for low sequencing depths it is necessary to include as many overlaps as possible in order to assemble low-coverage regions. Thus, assembly tools based on the de Bruijn graph paradigm are not well suited for low sequencing depth assembly or reassembly as they typically require depths of 20x to 30x ZB08].

In the context of this thesis, we have developed algorithms to address the problems in reassembly of short read data at a low sequencing depth. These algorithms have been implemented in a new assembly tool, LOCAS (LOw Coverage Assembly Software). LOCAS is designed for assembling short to medium sized reads in a de novo fashion using an overlap-layout-consensus approach. In this approach, overlap alignments of reads are calculated and represented in a so called overlap graph from which the final contigs are extracted. It explicitly handles data of low sequencing depth by allowing mismatches in the overlap calculation of reads. An extension of LOCAS, called SUPERLOCAS, efficiently incorporates left-over reads in the assembly process. It calculates a pre-assembly for the left-over reads once and assembles each block separately by incorporating the part of the preassembly that overlaps with the reads of the respective block. In addition, it can take advantage of alignment positions of reads within the reference sequence. SUPERLOCAS' design is perfectly suited to the requirements of a homology-guided assembly approach for large genomes.

We show that LOCAS produces assemblies that are often better than those obtained by existing short read assemblers at a sequencing depth of 7.5 x as measured by the $N 50$ size and error rate. In addition, for the task of incorporating left-over reads, SUPERLOCAS shows to be superior to common assemblers regarding $N 50$ size, error rate and runtime.

Following this introduction, in Chapter 2, sequencing technologies and computational approaches in genome resequencing are introduced. In Chapter 3, one of these approaches, homology-guided assembly, is refined and adapted to the needs of resequencing projects with short reads at a low sequencing depth. This approach employs a reassembly step. In Chapter 4, we present algorithms to assemble short read data at a low sequencing depth.We extend these algorithms in Chapter 5 to fulfill the additional requirements that arise with our specialized homology-guided assembly approach. The presented assembly algorithms have been implemented in the tools LOCAS and SUPERLOCAS. The evaluations of both tools and a comparison to other assemblers are provided in Chapter 6. Observed problems, provided solutions and the experimental evaluations are discussed in Chapter 7, before an overall conclusion of this work is given in Chapter 8 .

LOCAS and SUPERLOCAS are open source projects that are distributed under the terms of the GNU General Public License. Both software tools can be down-
loaded from http://www-ab.informatik.uni-tuebingen.de/software/locas.

## 2. Introduction to Genome Resequencing

This chapter gives an introduction into sequencing technologies. We will present the traditional sequencing technology by Sanger as well as technologies of the second generation. Furthermore, we will discuss three strategies for genome resequencing and discuss their applicability to Second Generation Sequencing (SGS) data. In addition to the widely used mapping-consensus and de novo assembly approaches, we will introduce the more sophisticated homology-guided assembly approach.

### 2.1. Sequencing Technologies

To understand the inheritance of traits in organisms their genomes have to be studied. The genomes of many organisms are organized in chromosomes. A chromosome is a single strand of coiled DNA (deoxyribonucleic acid) with DNA-bound proteins, which stabilize its structure. DNA was discovered by Friedrich Miescher in Tübingen, Germany, in 1869. Its three dimensional structure was characterized by James D. Watson and Francis Crick in 1953. Chromosomal DNA consists of two chains of nucleotide molecules, i.e., adenine, guanine, cytosine, and thymine. Specific regions in DNA molecules, which are called genes, encode for RNA (ribonucleic acid). In a process that is called transcription, genes are read by the RNA polymerase to produce RNA molecules. If the gene codes for a protein, the product of transcription is a messenger RNA (mRNA), which is later translated into a protein. Otherwise, the transcription product is a non-coding RNA molecule which can have regulatory and other functions. With the regulation of their genes, organisms control their cellular or overall function. Thus, we can learn about genome function, developing diseases and evolution of species by analyzing and comparing their DNA sequences.

The first sequencing technology was invented by Frederick Sanger and others in the 1970's [SC75]. The process of DNA sequencing determines the sequence of nucleotides in a DNA molecule. Until the development of SGS technologies, sequencing of DNA had been a very expensive and complex process [Met09]. In 2005, the first new sequencing technology, Roche's FLX Genome Sequencer, was released [MEA ${ }^{+}$05]. In the following years, further technologies such as Illumina's Genome Analyzer Ben06, $\overline{\left.\mathrm{BBS}^{+} 08\right]}$ and Applied Biosystem's sequencer SOLiD [SPR $\left.{ }^{+} 05\right]$ became commercially available. The first system towards a


Figure 2.1.: Sanger Sequencing. (A) The initial reaction mix contains the singlestranded template DNA, dNTPs and in lower concentration ddNTPs with distinct fluorescent markers. DNA polymerase is added to start the PCR (not shown). After a ddNTP has been incorporated by chance, the reaction terminates. (B) The resulting sequence fragments have different length with distinct labels indicating their 3 '-base. (C) Finally, the sequence fragments are separated via electrophoresis in mass-produced, gel-filled capillary tubes and their sequences are automatically determined as output. These sequences are given as intensity curves of the base-specific colors. The curve of each base displays the intensity of the base-signal for each position in the fragment.
third generation of sequencing technologies was the Helicos' Genetic Analysis System $\left[\mathrm{HBB}^{+} 08\right.$.

### 2.1.1. Sanger Sequencing

In the 1970's, two sequencing methods were developed independently: The Maxam-Gilbert method MG80] and Sanger sequencing, which is also known as chain termination method. It was the more efficient and less toxic Sanger sequencing that became popular. Until today, the method has improved steadily by taking advantage of other inventions like the polymerase chain reaction ( PCR ) and fluorescent labeling. For determining the sequence of DNA fragments that exceed the length of a single sequencing run, a shot gun approach is used as follows (see Figure 2.1 A):

1. DNA is fragmented to form a library of single-stranded DNA fragments.
2. The fragments are subcloned into bacterial vectors. The vectors are inserted in bacterial cells for amplification. The amplified DNA fragments are used
as templates in the following sequencing process.
3. The fragments, deoxynucleotides (dNTPs) and primers that are complementary to the linked adapters are given into an assay.
4. Dideoxynucleotides (ddNTP), which are similar to dNTPs except for lacking the 3'-hydroxyl group, that are fluorescently labeled with base-specific colors are added in low concentration.
5. DNA polymerase is added to initiate the PCR starting at the DNA primers.
6. The PCR terminates after a ddNTP is incorporated by the DNA polymerase.
7. The resulting sequence fragments have different length and are labeled by different colors attached to their 3'-base.
8. The sequence of a template fragment is obtained by separating all sequenced fragments according to their length with a Capillary Array Electrophoresis (CAE) and identifying their labeled 3'-bases.

As a result, the nucleotide sequence of each fragment in the library is determined. These sequences are called reads. The sequence of each read is given by the bases that correspond to the highest peak in the intensity curve at the respective positions. In addition, quality values are calculated from the curve that reflect the error probability of each base in a read.

In order to gain information about the relative order of the generated reads, the method can be extended to produce mate-pairs, i.e., pairs of reads for which the orientation and approximate distance to each other are known.

### 2.1.2. Second Generation Sequencing Technologies

With the rise of a new generation of sequencing technologies, sequencing has become cheaper and less time consuming [Met09]. Due to the dramatically increased throughput of the sequencing technologies, more projects that study the genome variation within and across species or the transcriptome of a species can be realized.

The read sequences generated by the new technologies are shorter and tend to be more erroneous than Sanger reads. The higher error rate can be compensated to a certain extent by the higher amount of data that is available due to a higher sequencing depth. The shorter read length, however, yields several new issues and problems for the processing and analysis of sequencing data.

Like Sanger sequencing, most of the SGS technologies follow the sequencing-bysynthesis approach, i.e., they synthesize a strand of a DNA molecule according to a template strand and record the order of the incorporated nucleotides. Here, the recording becomes feasible using a light signal that is emitted upon incorporation and that is recorded by a camera. The whole cycle can easily be run in parallel,
synthesizing different fragments at the same time. The major difference to Sanger sequencing is the use of reversible termination for DNA synthesis.

In the next sections, we will present two widely used SGS technologies in detail, pyrosequencing by Roche/454 Life Sciences [LLT ${ }^{+} 03$, MEA $\left.{ }^{+} 05\right]$ and sequencing using cyclic reversible termination by Illumina $\mathrm{Ben06}, \mathrm{BBS}^{+} 08$ ]. Finally, we will briefly describe other recent sequencing technologies.

## Pyrosequencing (Roche/454 Life Sciences)

The FLX Genome Sequencer by Roche/454 Life Sciences is based on the pyrosequencing technology, which detects the release of pyrophosphates when a nucleotide is incorporated by the DNA polymerase. Each time a pyrophosphate is released, it is converted into visible light using a series of enzymatic reactions. The sequence of emitted light that codes for the nucleotide sequence of the synthesized template is recorded.

At first, the DNA of the target organism is randomly broken into fragments to create templates for the amplification. The main workflow continues as follows (see Figure 2.2):

1. Single-stranded fragments are ligated to universal adapters at both ends.
2. Each fragment is captured onto one bead (favoring one fragment per bead) in a water-oil-emulsion.
3. Amplification of each fragment by emulsion PCR such that populations of identical template fragments are bound to each bead.
4. Beads are given individually into arrays of wells (PicoTiterPlate).
5. Sequencing-by-synthesis of the template fragments using single-nucleotide addition:
a) One type of dNTPs is added per step.
b) From the synthesized dNTP molecule a pyrophosphate is cleaved that converts provided APS (adenosine-5'-phosphosulfate) to ATP.
c) With the help of Luciferase, ATP is transformed into visible light that is emitted proportional to the number of identical nucleotides that are added simultaneously.
d) For the next nucleotide, the remaining dNTPs and ATPs are degraded.

The templates are amplified since imaging systems have problems with the detection of single fluorescent signals. The light signal detected during the synthesis is a consensus signal that is emitted simultaneously by all identical templates. Due to incomplete extension or addition of multiple nucleotides to the identical templates, the fluorescent signal is dephased occasionally. The order of light peaks and their intensities determine the original sequence of the synthesized fragment.


Figure 2.2.: (A) Pyrosequencing - DNA Amplification Step. The DNA fragments are captured by beads and these bead-DNA complexes are encapsulated into single aqueous droplets. Within these droplets, the template fragments are amplified by emulsion PCR. Several thousand copies of the same template sequence are bound to each bead. (B) Pyrosequencing - Sequencing Step. A DNA fragment is synthesized from the single stranded DNA template by the DNA polymerase. During that process, dNTPs are added one at a time (here dGNTPs is added). With the incorporation of a nucleotide a pyrophosphate ( PPi ) is released. The provided sulfurylase quantitatively converts PPi to ATP. A light signal is emitted that is produced with the catalysator luciferase in presence of ATP. The signal is detected by a charge coupled device camera and represented as a peak in a pyrogram. The nucleotide degrading enzyme apyrase continuously degrades unincorporated dNTPs and ATP. In the next step, the process starts from the beginning by adding the next dNTP. Finally, the whole nucleotide sequence of the synthesized DNA strand is inferred from the signal peaks of the produced pyrogram. Image (A) is from Metzker [Met09] and image (B) is from Armougom and Raoult AR09

Homopolymer DNA segments, i.e., regions with multiple consecutive copies of a single base, will result in higher intensities depending on their copy number. Since this is difficult to measure exactly for longer homopolymer regions, the resolution of homopolymer DNA segments is often erroneous. The most common error type are insertions, the second most are deletions. The mean read length is 330 bp while 1.29 Gb can be produced per day with a single machine.

## Sequencing Using Cyclic Reversible Termination (Illumina)

Like the technology of 454 /Roche, Illumina employs the sequencing-by-synthesis approach for its sequencing system Genome Analyzer. Instead of adding just one type of nucleotide, all types are provided to the sequencing reaction at the same time. A reversible terminator at each nucleotide prevents the incorporation of several nucleotides per step. The nucleotides are labeled with different fluoroscentic signals such that their specific light spectrum can be recorded after incorporation. The method works as follows (see Figure 2.3):

1. Adapter linkers are ligated onto both ends of the DNA fragment.
2. Fragments are tethered in great distance to a glass plate by the flexible linker at their 5'-end and will eventually hybridize with primers linked to the plate that are complementary to the 3 '-adapter, forming a bridge on the glass plate.
3. Amplification via bridge PCR produces clusters of identical fragments on the plate.
4. Sequencing-by-synthesis with reversible termination:
a) dNTPs are flowed over the plate simultaneously and only one single nucleotide is synthesized since the 3 '-end of the dNTPs are blocked.
b) Not incorporated nucleotides are washed away.
c) Incorporated bases are detected via their fluorescent labels.
d) Fluorescent dye and 3'-block is removed and the process is repeated.

Substitutions are the most frequent error type of the Genome Analyzer. Also, an under-representation of AT-rich and GC-rich regions has been reported. The mean read length is about 75 bp or 100 bp .4 .5 Gb of reads can be produced per day with a single machine. Currently, the Genome Analyzer dominates the market of SGS due to its good trade-off between costs, reads length and accuracy.

## Remarks and Outlook

All SGS technologies can also provide mate-pair information, i.e., two reads whose approximate distance and orientation is known. The distance between them is


Figure 2.3.: (A) For the amplification with Illumina's Genome Analyzer, forward and reverse primers are covalently attached to a glass plate in the beginning. The singlestranded DNA templates are hybridized to adapters at both ends. The templates are attached to the slide by hybridizing one of their adapters to a complementary primer on the slide. The templates are extended such that they build double-stranded bridges with immediately adjacent primers on the slide. These bridges are denatured resulting again in single-stranded templates tethered to the slide. The process is repeated until a cluster of identical fragments is built for each template. (B) The four-color cyclic reversible termination method is shown, starting with the incorporation of nucleotides in the complementary strand to the template sequences, which are attached to the glass slide. Incorporated nucleotides are labeled with different dyes that are imaged after all unincorporated nucleotides have been washed off. Following imaging, the fluorescent dyes are cleaved and the 3 '-hydroxyl group is regenerated such that the synthesized sequence can be elongated. Then, the cycle repeats with the incorporation of the next labeled nucleotides that are blocked at their 3'-end. The image is from Metzker [Met09].
called insert size. To distinguish between pairs with a longer (at least 1 kbp ) and a shorter (at most 1 kbp ) insert size, the terms mate-pair or paired-end reads were introduced, respectively. We will use the term mate-pair in this work for both types.

In the following, we briefly describe other SGS technologies and recent developments towards a third generation of sequencing technologies. Their sequencing methods differ in the template preparation and the applied sequencing method.

Another SGS method is sequencing-by-ligation, in which DNA polymerase is replaced by DNA ligase [ $\left.\mathrm{SPR}^{+} 05\right]$. The method is commercialized in a sequencing platform, called SOLiD (support oligonucleotide ligation detection), by Applied Biosystem. The method became available in 2008 but is not used as often as the previously described technologies of Roche/454 Life Sciences and Illumina.

The sequencing methods are steadily improving with increased read lengths and decreasing sequencing costs. Furthermore, more mate-pair libraries with different insert sizes are provided. Assembly approaches benefit from various insert sizes and from longer read lengths, which will be discussed in Section 2.3. One technology that is already commercially distributed is HeliScope of Helicos BioSciences, which uses single-molecular templates instead of amplified templates [ $\mathrm{HBB}^{+} 08$ ]. This allows for an unbiased quantification of sequenced RNA molecules. The platform applies a one-color cyclic reversible termination method for sequencing.

Another promising method is real-time sequencing developed by Pacific Biosciences $\left[\mathrm{EFG}^{+} 09\right]$. DNA synthesis is performed in real-time and labeled nucleotides are measured at the moment of incorporation in the synthesized DNA strand. With a fixation of the DNA polymerase, the light signals are emitted within a reduced observation volume. Thus, the signals can be recorded in realtime and reversible terminators are no longer required.

The most recent technology is ion torrent. The technology uses the fact that during nucleotide incorporation a hydrogen ion is released. The template DNA fragments are hold in microwells of an array such that the process can be performed in parallel. The ion-sensitive layer and sensor, which are located beneath the array, detect the release of a hydrogen ion upon nucleotide incorporation. However, the methods still requires PCR amplification and terminates the sequencing process after a nucleotide is incorporated [STK10].

In addition, nanopore sequencing, which has been under development since 1995, is currently improved by Oxford Nanopore. As the technology of Pacific Biosciences, this technology uses also single-molecule DNA templates. In this sequencing method, nanopores are utilized to detect and analyze nucleotides of the templates. In one approach, individual nucleotides on the DNA template are identified as it passes through a protein nanopore. There are still some problems that have to be solved before this technology, which would be likely to be the cheapest of the third generation sequencing technologies, will become commercially available Rus09.

### 2.2. Mapping-Consensus Approach

One of the challenges introduced by new sequencing technologies is the efficient alignment of large amounts of short reads onto a reference genome. This process is also called mapping.

The mapping problem is certainly not new and there already existed many tools that perform mappings for Sanger data. Also, conventional software tools such as BLAST can be used for mapping to a certain degree. However, since it was not designed for mapping short sequences onto a single reference sequence, BLAST will take up to thousands of CPU hours to align the number of reads that are produced in a typical sequencing project [TS09]. Due to limitations of existing tools which result in long runtimes, the methods were adapted to the demands of the new data. Mainly, the decrease in read length and the much greater amount of data had to be considered, but also new sequence characteristics and specific error distributions.

New alignment tools follow more or less the following workflow: First, possible alignment positions of the reads in the reference genome are detected. Next, read sequences are aligned against these regions and the consensus sequence of overlapping aligned reads is calculated.

There exist two indexing strategies that can speed up the process of assigning reads to possible alignment regions: hash table indexing or indexing with the Burrows Wheeler Transformation (BWT) [FB09]. In the hash table approach, either the reference genome or the set of sequence reads are indexed using seeds or spaced seeds. While a seed is a sequence region that has to match exactly, a spaced-seed allows mismatches at specified positions. Thus, not all characters of the seed have to be compared but only the positions that are required to match. With a hash function, reads are associated to the seeds that match their sequence. For each seed, the associated read identifiers are stored in the hash table. The matched seeds between reference genome and read sequences represent potential alignment regions of the reads to the reference. By indexing the reads, the reads are associated with positions in the reference genome and can be quickly looked up with the help of the index. The same is possible for the reference genome if it is indexed. Then, the set of reads is used to quickly scan the hash table of the reference genome. Short read alignment tools based on hash tables are MAQ [LRD08], SOAP [LLKW08], ELAND [ $\mathrm{BBS}^{+} 08$ ], SHRiMP [RLD ${ }^{+}$09], ZOOM [LZZ ${ }^{+} 08$ ], BFAST HMN09], MOSAIK Mos and GenomeMapper [SHO ${ }^{+}$09]. In contrast, tools like Bowtie [LTPS09], BWA [LD10] and SOAP2 $\left[\overline{\left.\mathrm{LYL}^{+} 09\right]}\right.$ create a BWT of the reference genome and index this transformation using a suffix array. This index is called FM index or compressed suffix array. Possible alignment regions of reads in the reference genome are detected by scanning for seeds of the reads in the FM index. The FM index takes advantage from the compression of the reference genome by the BWT. The FM index is often smaller than the index of the original reference genome, while it still allows to search for substrings at the same level of speed. Consequently, short read mappers
based on the BWT are much faster than hash-based methods at the same level of sensitivity.

After detecting possible alignment positions, accurate alignments of the reads to the reference genome are calculated at these positions by a gapped or ungapped version of the Smith-Waterman algorithm. In addition, quality values of the sequenced bases can be taken into account. To obtain reliable alignment positions of the reads, a threshold for the number of allowed mismatches is defined. For each read, the alignments with the highest alignment score, representing the quality of the alignment, are considered as best alignments. If there exists only one best alignment for a read, the read can be uniquely assigned to the reference sequence. If there exist several best alignments, the read is marked as belonging to a repetitive region. An alignment of mate-pair reads to the reference sequence can only be classified as correct, if both reads align in a correct orientation to each other and show a distance that matches their insert size.

Finally, the consensus sequence is determined. Either the determination is an integrated part of the mapping software like in SOAPsnp [LF+ ${ }^{+} 9$ ] or it is handled by a separate software like SAMtools [LHW $\left.{ }^{+} 09\right]$. For reads that are uniquely aligned onto the reference sequence, the consensus sequence can be determined to detect reliable differences between the target genome and the reference genome such as SNPs and short indels. Quality scores of the consensus bases are taken into account. Thresholds for the reliability of bases in the consensus sequence can be adjusted to the type of read data used.

The mapping-consensus strategy has some limitations in the detection of longer insertions and highly polymorphic regions in the target genome. Using conventional mapping software, only a limited amount of these regions are detected depending on their length. Thus, more sophisticated approaches are required for covering long insertions or highly polymorphic regions. Moreover, rearrangements like reversals, i.e., regions in the target sequences that are reversed compared to the reference sequence, can not be found by mapping-consensus approaches.

### 2.3. De Novo Assembly Approach

In contrast to the mapping-consensus approach, de novo assembly does not utilize a reference sequence. Reads are assembled in order to reconstruct the original sequence of the target genome. The read sequences are overlapped and merged with each other into a colinear arrangement without any additional sequence information. In this process, mate-pair information can be utilized.

Initially, the de novo assembly problem was formulated as the shortest superstring problem Pop04].

## Definition 1. Shortest Superstring Problem (SSP)

For a given set $S$ of read sequences, the shortest string that contains each read of $S$ as substring is the shortest superstring.

The problem of finding the shortest superstring is known to be NP-hard, which means that for this problem no exact solution can be found in polynomial time using a deterministic algorithm, unless $\mathrm{P}=\mathrm{NP}$. This simplified definition of the assembly problem does not consider repetitive regions and sequencing errors. Thus, even the exact solution for the SSP might not correspond to a correct solution of the assembly problem.

Three approaches have been developed to approximate the assembly problem: A greedy approach, the overlap-layout-consensus approach, and the de Bruijn graph approach. Several tools based on one of these approaches have been designed to assemble Sanger reads. However, tools that have been developed for Sanger reads cannot be directly applied to short read data without adjusting their algorithms to the shorter read length, higher coverage and the specific error characteristics of SGS technologies

### 2.3.1. Greedy Assembly Approach

When the assembly problem came up, several greedy algorithms PSTU73, TY02, AS98, KS05] were developed that worked according to Algorithm 2.3.1.

## Algorithm 2.3.1: GREEDYASSEMBLYSANGER(readSequences)

```
contigs \(\leftarrow\) readSequences
while there exist two sequences in contigs that overlap with each other
    do \(\left\{\begin{aligned} \text { contigPair } \leftarrow & \text { randomly choose two sequences in contigs } \\ & \text { with best overlap }\end{aligned}\right\} \begin{aligned} & \text { newContig } \leftarrow \\ & \text { merged contigPair according to alignment } \\ & \text { contigs.delete }(\text { contigPair }) \\ & \text { contigs.add }(\text { newContig })\end{aligned}\)
return (contigs)
```

Due to the complex structure of most genomes and to errors in the read sequences, the genome sequence can only be approximated by a greedy algorithm. Nevertheless, most sequencing errors in the reads can be handled in the greedy strategy by allowing mismatches in the overlap alignments of reads. Unfortunately, there exists no extension to the algorithm to handle repeat regions that occur in the target sequence. Regions that are adjacent to such repeats are likely to be combined in a wrong order during the greedy assembly process, leading to false contigs.

```
Algorithm 2.3.2: GREEDYASSEMBLYSHORT(reads)
```

prefixTree $\leftarrow$ Prefix Tree for reads, 5'-prefixes of read sequences and
their reversed complements
contigs $\leftarrow$ empty List
newContig $\leftarrow$ empty String
while there exists a sequence in reads that is not contained in contigs
$\mathrm{do}\left\{\begin{array}{l}\text { newContig } \leftarrow \text { randomly choose sequence in reads that is not } \\ \text { contained in contigs } \\ \text { EXTENDContigAT3'EnD(reads,newContig,prefixTree) } \\ \text { newContig } \leftarrow \text { newContig.reversedComplement }() \\ \text { ExTENDContigAt3'End(reads,newContig,prefixTree) } \\ \text { contigs.add(newContig) }\end{array}\right.$
return (contigs)

```
Algorithm 2.3.3: ExtendContigAt3'End(reads, newContig,pTree)
    nextReads \(\leftarrow\) utilization of \(p\) Tree to find a set of sequences in reads such
    that their 5' ends match exactly to the 3 ' end of newContig
    by maximizing the length of the exact matching
while nextReads is not empty and contains only similar sequences
    do \(\left\{\begin{aligned} & \text { newContig } \leftarrow \text { extension of newContig by multiple alignment } \\ & \text { of nextReads }\end{aligned}\right\} \begin{aligned} & \text { reads.delete (nextReads) } \\ & \text { nextReads } \leftarrow \text { find a set of reads such that their 5 ends match } \\ & \text { exactly to the 3' end of newContig by maximizing } \\ & \text { the length of the exact matching using pTree }\end{aligned}\)
return (newContig)
```

With the rise of short read data, a similar greedy strategy has been developed, see Algorithm 2.3.2. To deal with the large number of reads, a prefix tree that organizes the read sequences by their first bases is built such that potential start regions of overlaps between reads can be detected efficiently. Sequencing errors in the read data are taken into account by favoring read sequences with a high sequencing depth for extending a contig. Mis-assemblies caused by repeats are avoided by cutting the assembly if overlapping reads do not show a similar elongation-sequence. Such reads could arise from different copies of a repeat. Often they match at one end, indicating the repeat region, but have dissimilar regions at the other end. Utilizing this approach often results in a large number of very small contigs and a long runtime, for example 6 h to 19 h for a single bacterial genome assembly. Variants of this algorithm are implemented in the assembly tools SSAKE [WSJH07], VCAKE [JRB ${ }^{+} 07$ ] and SHARCGS [DLBH07].

### 2.3.2. Overlap-Layout-Consensus Approach

In order to address problems in assembly like sequencing errors and the resolution of repeats, the local nature of the greedy strategy has to be overcome. A more sophisticated approach follows the overlap-layout-consensus paradigm. It has been introduced for Sanger reads by Peltola et al. [PSU84] in 1984 and further developed by Kececioglu and Myers KM95, Mye95 in 1995. Here, the overlap information between reads is represented in a graph structure, the overlap graph. In such a graph, each read is represented by a vertex and each overlap between reads is represented by an edge between the corresponding vertices, see Figure 2.4 C. With this representation, the assembly problem can be formulated as the problem of finding a Hamiltonian Path Pop04.

## Definition 2. Hamiltonian Path

In a given graph, a Hamiltonian Path visits each vertex exactly once.
The problem of determining the existence of a Hamiltonian Path is NPcomplete. Problems that are NP-complete lie in NP and any NP-hard problem can be reduced to any of these problems. For a problem that lies in NP a provided solution can be verified in polynomial time. For a problem that is NP-complete an exact solution cannot be found in polynomial time using a deterministic algorithm, unless $\mathrm{P}=\mathrm{NP}$.

Similar to the SSP, solving the assembly problem by finding a Hamiltonian Path does not consider sequencing errors and repeat regions in the target genome. However, with the overlap-layout-consensus approach, good approximations of the real world assembly problem can be obtained by finding paths in the overlap graph. Paths that are induced by sequencing errors or repeats have to be cut and perhaps re-linked in the graph. For the final paths, the represented consensus sequence is calculated and reported as contig. In general, the overlap-layout-consensus approach executes the following three steps:

1. Overlap phase: Overlap alignments between read sequences are determined and represented in a graph structure.
2. Layout phase: A path is selected representing an alignment that assembles the reads in a linear order.
3. Consensus phase: For the final path the consensus sequences, which correspond to the most likely original sequence of the target genome, is calculated.

This workflow is illustrated in Figure 2.4. In the overlap phase, pairs of overlapping reads are determined by calculating overlap alignments. In a naïve approach, all read sequences are compared with each other to detect all pairwise overlap alignments. To reduce the number of comparisons, a filtering step is often applied revealing pairs of reads that possibly overlap. Often, reads share an identical subsequence, a $k$-mer, if they overlap with each other. These $k$-mers are detected

A

| TACGC | GCTTT | CGCTCG | AGTGC |
| :--- | :--- | :--- | :--- |
| AGC | GCTT | TAGGC | GCATT |
| TACG | TTCGG | CGTCAG | CAGTGC |
| ACTTG | CGTA | TGCAG | TCGAAC |
| AGGTA |  |  |  |

B
TACG TCGAAC
TACG TCGAAC
cgCtcG AGTGC
cgCtcG AGTGC
GgTCAG GCTtTGACT
GgTCAG GCTtTGACT
CAGTGC ACTTG AGC GCTTT
CAGTGC ACTTG AGC GCTTT
tGCAG tacgC
tGCAG tacgC
AGGTA GCATT
AGGTA GCATT
TAGGC TTCGG
TAGGC TTCGG
CGTA
CGTA
C

E
tacg cgctcg agtgc CGTCAG GCTTTGACT ACTTG
tGCAG TACGC AGGTA GCATT
TACGCTCGTCAGTGCTTTGACTTGCAGGTACGCATTCGG

Figure 2.4.: The workflow of the overlap-layout-consensus approach is shown using a simple example. (A) Read sequences are obtained from a sequencing platform. In this example, the read lengths vary between three and five bp. (B) In the overlap phase, overlaps between the read sequences are determined. In a filtering step, which is not shown here, pairs of reads that share a common $k$-mer are determined. For these candidates, the pairwise overlaps are determined. (C) The overlap phase results in a representation of the overlap information as an overlap graph. (D) In the layout phase, cycles in the graph that arise from repeats, sequencing errors and polymorphisms are handled. Here, the overlap graph shows two cycles arising from sequencing errors in the reads CAGAGC and TATGC. These cycles are handled by deciding for one of their paths. Furthermore, short paths arising from reads that overlap with only one other read are deleted. (D) Finally, unique paths are extracted from the overlap graph. (E) In the consensus phase, for each extracted path the consensus sequence of the underlying read sequences is determined and reported as a contig.
using an indexing technique like a suffix-array. Only for pairs that share a $k$-mer, an overlap alignment is determined.

To further reduce the time for the calculation of the overlap alignments, a banded alignment algorithm can be applied. It reduces the time complexity of an alignment from quadratic to nearly linear time by avoiding alignments that have a longer gap in either sequence. This is managed by constraining the calculations of the dynamic programming matrix to a diagonal band. The position of the band can be determined by the positions of the equal $k$-mers that have been detected by means of indexing in the beginning of the overlap phase.

For the actual overlap alignment calculation, constraints are set such as the maximum number of mismatches, the minimum alignment length and gap bounds. Unfortunately, there still exist false overlaps due to erroneous read sequences or accidentally aligned reads that belong to different copies of a repeat. False alignments can be induced by repeats, since reads that contain the same part of a repeat sequence do not necessarily belong to the same copy of the repeat in the target genome. To reduce the number of false overlaps, quality values that are given for the read sequences can be used to penalize mismatches between high quality bases stronger than mismatches between bases of lower quality. Not all false overlaps can be detected with this approach and, thus, have to be handled later in the workflow. In addition, it has to be considered that read sequences that originate from the same region in the target genome are almost identical except for sequencing errors. If they do not have the same length, one sequence might be contained in another sequence. Thus, we have to merge these reads. Finally, the calculated overlap information is represented in an overlap graph.

In the layout phase, final paths are selected from the overlap graph. The paths represent alignments of reads in which the reads are linearly ordered. Different optimization strategies can be chosen to select edges for these paths, e.g., the score of the alignments, their quality or more sophisticated alignment statistics. The layout problem has been shown to be NP-complete for the different optimization targets [PSU84, KM95].

The size of the overlap graph tends to grow drastically, even for Sanger reads, to up to tens of thousands or tens of millions of vertices for bacterial or mammaliansized genomes, respectively. Nevertheless, there exist several implementations of the layout phase that calculate good approximations. Most of these greedy methods transform the overlap graph in a graph of lower complexity by simplifying subgraphs in the overlap graph for which the layout problem can be easily solved [Mye95]. Often, these subgraphs represent regions between repeats in the genome sequence. Then, more sophisticated approaches are applied to the reduced graph by taking advantage of mate-pair information. The graph can be further simplified by placing mate-pairs such that their distance and orientation in the graph is consistent with their insert size and their real orientation to each other. Variations of this idea are implemented in several assembly tools like the Celera Assembler [MSD+00] or Arachne [BJS ${ }^{+} 02$ ].

Often, several mate-pair libraries with different insert sizes are available, de-
pending on the technique the library was produced with. Repeat regions can only be spanned by mate-pairs that have an appropriate insert size. Thus, different mate-pair libraries are required for handling repeats of different sizes. In addition to mate-information, the sequence depth offers the possibility to detect subgraphs in the overlap graph that belong to repetitive regions. Usually, the sequencing depth at a repetitive region depends on the number of its copies in the target genome and is by this factor higher than the mean sequencing depth of all other regions in the genome. The reads of each copy of a repeat align to each other and, thus, will collapse into the same subgraph in the overlap graph. In order to optimize the runtime, assembly tools often skip the assembly of longer repeat regions by omitting all related overlap alignments.

In the consensus phase, the consensus sequence is calculated for the aligned reads that are represented by the final selected paths. The consensus sequence is determined from a multiple alignment that is constructed for the reads such that the overall alignment score is maximized. The multiple alignment is often only an approximation since an exact solution cannot be determined efficiently. One heuristic to create a multiple alignment uses the already provided pairwise alignments of reads. Often, only a subset of the pairwise alignments is used such that no redundant alignment information is contained. More sophisticated approaches calculate a multiple alignment of the reads iteratively by adding a read sequence to the multiple alignment in each step. The placement of the newly inserted read is guided by the already available pairwise alignments. A similar approach by Anson and Myers AM97] improves an initial multiple alignment of the reads by an iterative procedure. In each step, a read sequence is deleted from the multiple alignment and re-aligned again. The process terminates when the multiple alignment cannot be improved any further. Other algorithms take the overlap alignments of the reads as a first layout of the multiple alignment and solely optimize local regions that contain mismatches. In order to obtain an appropriate multiple alignment, the consensus is calculated for each position by choosing the base with the highest relative frequency.

Besides the already mentioned Celera Assembler and Arachne, there exist various other sophisticated assembly tools that follow the overlap-layoutconsensus paradigm like Atlas [HCD+04], CAP3 [HM99], PCAP [HWA+03], Phrap DLBM07, Phusion MN03] and for short read data Edena [HFF ${ }^{+}$08] and the here presented LOCAS. Until now, this approach has not been adapted to SGS data very often since the number of pair-wise comparisons in the overlap phase is huge due to the large amount of data. Furthermore, the reliability of short overlap alignments that are required for short reads is not very high. At present, the state-of-the-art approach for developing assembly tools for SGS data is the de Bruijn graph approach.


Figure 2.5.: An example de Bruijn graph assembly is shown. (A) Sequence reads are obtained from a sequencing platform. In this example, the read lengths vary between seven and nine bp. $(\mathrm{B}+\mathrm{C})$ In the next step, the $k$-mers, in this example 4 -mers, are hashed, $k$-mers and their overlaps are represented in a de Bruijn graph. (D) The graph is simplified such that each path that has no branching vertices is reduced to a single vertex. From now on, vertices can represent sequences of different lengths. (E) In the next step, the graph is reduced by handling cycles that arise from sequencing errors. In addition, short paths resulting from $k$-mers that do not overlap at both sides are deleted. Also, cycles induced by repeats are handled, which is not shown here. Finally, a graph is obtained that approximates the genome sequence. (F) The sequence is determined via the consensus sequences of the linear paths that can be extracted from the graph.

### 2.3.3. De Bruijn Graph Approach

Idury and Waterman IW95 were the first to introduce the de Bruijn graph approach for sequence assembly. All overlapping $k$-mers, i.e., $k$-mers that overlap exactly with a length of $k-1$, in the set of sequence reads are detected using an index structure. This information is converted into a de Bruijn graph by introducing a vertex for each $k$-mer and an edge between two vertices if the respective $k$-mers overlap in $k-1$ positions. Using this model, the sequence of the original genome can be approximated by an Eulerian Path in the de Bruijn graph Pop04.

## Definition 3. Eulerian Path

In a given graph, a Eulerian Path visits each edge of the graph exactly once.
The Eulerian Path problem can be solved in linear time and returns a solution to the assembly problem assuming error-free read sequences and a target genome without repetitive regions. In order to consider also repeats and sequencing errors in the assembly solution, a variation of the Eulerian Path has to be calculated. This path has to traverse subgraphs that represent repeats several times. Subgraphs that belong to sequencing errors must not be included in the final path. Furthermore, the problem of selecting such a path becomes even harder. For example, each sequencing error in a read leads to a number of false $k$-mers, which increases the number of vertices in the de Bruijn graph. It also may happen that $k$-mers that are not adjacent to each other in an input read are represented by connected vertices in the graph. Thus, incorrect sequence information is represented in the graph.

The first implementation of the approach was released by Pevzner et al. [PTW01b, PT01, PTW01a] addressing several of the above issues. In Figure 2.5, the workflow of the de Bruijn graph approach is illustrated. In addition, Pevzner et al. developed an error correction method. Input reads are corrected by counting the frequency of their $k$-mers in all read sequences and replacing less frequent $k$-mers by similar $k$-mers of a high frequency. Furthermore, reads are used to reduce the complexity of the de Bruijn graph. On one hand, edges between vertices that represent $k$-mers that are not present in one read sequence are deleted. On the other hand, small repetitive regions can be handled by utilizing original read sequences that fully contain these repeats. In addition, Pevzner and Tang developed a sophisticated method that handles longer repeats by using mate-pair information [PT01.

A key advantage of the de Bruijn approach is the construction time, which is linear in the number of reads, while the overlap-layout-consensus approach has a quadratic runtime using a naïve implementation.
The de Bruijn approach has been first adapted to SGS data in the software tool Newbler (Roche's 454 assembler), which assembles reads produced by the 454/Roche technology. Several assembly tools that are compatible with reads of the Illumina technology followed like VELVET [ZB08], EULER-SR [CP08], ABySS [SWJ+09], ALLPATH [ $\mathrm{BMK}^{+} 08$, MPG+09], SOAPdenovo [LLZ+$\left.{ }^{+} 09\right]$ and
recently Contrail [ $\mathrm{SSK}^{+}$]. They all use a de Bruijn graph but their approaches for error treatment and for taking advantage of mate-pair information differ.

### 2.3.4. Prospects of De Novo Assembly with Short Reads

The natural limits of a short read assembly under the assumption of error-free reads have been investigated by Whiteford et al. WHW ${ }^{+} 05$. Excellent results could be produced for bacterial genomes even with a read length of 30 bp . For Escherichia coli, $75 \%$ of the genome was covered by contigs with at least $10,000 \mathrm{bp}$ and $96 \%$ of the genes were assembled within single contigs. For eukaryotic genomes, $51 \%$ of the genome could be assembled into contigs with at least $10,000 \mathrm{bp}$ using reads of length 50 bp .

In de novo assembly of complex and large sized genomes, large amounts of memory are required in the assembly process. With the de Bruijn graph approach, which is used by most current assemblers, the data is presented in a compressed fashion. However, additional data structures are required for assigning reads to the graph, which produces a memory overhead for larger genomes. The high demand for memory has been addressed in more sophisticated assembly approaches such as SOAPdenovo by using compressed data structures that can be retained to disk. To take advantage of multiple computers, a parallelized, MPI-cluster-based approach is used by the assembler ABySS. Further, there exist homology-guided approaches that use a reference sequence to partition the assembly problem into smaller sub-problems in order to save memory. This approach will be discussed in Section 2.4 .

Repetitive regions still yield the main problems for assembly. Different libraries of mate-pairs are required to handle repeats of different sizes. Consequently, at least a portion of the read data should be provided with mate-pair libraries of short and long insert sizes. The quality of the assembly will benefit from this data. Nevertheless, the assembly depends strongly on the kind of target genome. While bacterial genomes have often only a small number of repetitive regions with a length of at most 200 bp , eukaryotic genomes such as the human genome are more complex. The repeat length of these genomes depends on the appearance of active SINE and LINE transposable elements, which have a length of 500 bp to 1 kbp and about 4 kbp , respectively. The longer insert sizes of mate-pairs that have recently been provided by the SGS technologies will facilitate de novo assemblies of large complex genomes.

### 2.3.5. Scaffolding

Contigs produced by de novo assembly need to be ordered and oriented to each other to obtain their correct position in the target genome. This is done in a similar fashion to the mapping-consensus approach in a process called scaffolding.

Constraints defined by given mate-pairs are used in the scaffolding process by ordering contigs according to adjacency information of their mate-pairs. The
orientation of mated reads to each other yields restrictions to the orientation of the respective contigs. With the approximate distance between two mate reads, the contigs can be ordered and their distance to each other can be determined. Often, multiple libraries with mate-pairs of different insert sizes are generated, which provides even more constraints.

Although some assemblers include scaffolding, there exist stand-alone scaffolding tools like Bambus [PKS04]. It was originally developed for Sanger reads but is also widely used for SGS data. The tool makes use of mate-pair information and can utilize a complete genome sequence of a related organism to guide the contig placement.

Further approaches for scaffolding are contig overlapping and the use of gene synteny. The first uses additional information on detected overlaps between contigs to order them and extract information on their orientation. Knowledge of gene synteny is used to scaffold contigs that contain co-located genes. Therefore, genes are detected within contigs that usually occur in clusters in most organisms. Contigs containing the same gene sequence or genes from one cluster are placed close to each other in the scaffolding solution.

### 2.4. Homology-Guided Assembly Approach

Similar to the mapping-consensus approach, homology-guided or comparative assembly approaches exploit available reference genomes from the same or closely related species. Often, different strains of the same species are sequenced in order to identify polymorphisms and indels [RSP ${ }^{+} 02$ ]. The comparative assembly strategy works best when the genomes of two species are more than $90 \%$ identical PS08].

Homology-guided assembly adapts from both, the mapping-consensus approach as well as de novo assembly. The traditional overlap-layout-consensus approach is transformed in a mapping-layout-consensus approach. The layout phase additionally handles indels and rearrangements that occur between target and reference genome. Usually, these regions complicate the mapping of the reads to the reference since reads may only partially match the reference genome or reads may match non-adjacent regions of the reference. The overall workflow is as follows:

1. Read mapping: Align reads to the reference genome and utilize possible mate-pair information.
2. Layout refinement: Rearrange reads to handle indels, divergent positions and genome rearrangements.
3. Consensus phase: Generate consensus sequence for reads of the final layout.
4. Scaffolding (optional): Orientate and order contigs.

Insertions appearing in the target genome are handled in the layout phase. Reads belonging entirely to these regions will not align to the reference genome while reads that align only partially with the insert region can align to the reference genome. The assembly will stop at the point of this insertion, resulting in two separate contigs. In the case of smaller insertions that have at most the length of a read, some reads from the edge of the insertion will align to the reference genome. These insertion regions can be resolved with the homology-guided assembly approach and are reported as a single contig.

An advantage of placing reads on a reference genome instead of overlapping them with each other is that more sequencing errors can be handled and, thus, a considerable lower amount of read data is required to perform assembly. Also, regions that lead to major problems in de novo assembly like repeats can be handled more easily. The ability to detect expansions and contractions of long tandem repeats is increased. Tandem repeats are repeated pattern sequences of at least two nucleotides that are directly adjacent to each other. Moreover, isolated repeats do not cause breaks in the assembly as they would do in a de novo strategy. Reads belonging to repeats are randomly assigned to one copy of the repeat to which they have a high quality alignment in the reference sequence [PS08].

One of the first comparative assemblers was AMOScmp [PPDS04]. It was first created for Sanger reads and later adjusted to SGS data (AMOScmp-shortReads, unpublished). Another tool developed for short read data is Crossbow [LSL+09], a software pipeline for whole genome resequencing analysis. It utilizes the short read aligner Bowtie and the genotyper SOAPsnp and applies them in a parallel fashion exploiting multiple computers and CPUs wherever possible.

## 3. An Extended Homology-Guided Assembly Approach (SHORE)

The homology-guided assembly approach uses a reference sequence to guide the assembly process. Homologous regions are assembled and short polymorphic regions and indels can be resolved with this approach, see Section 2.4. However, longer insertion and highly polymorphic regions still raise problems.

In this chapter, we introduce a sophisticated method that extends the traditional homology-guided assembly approach to additionally address the assembly of longer insertion and highly polymorphic regions. The main steps of the workflow are a mapping of all reads onto the reference and a pooling of all left-over reads, which are reads that could not be mapped onto the reference sequence. In the following, the mapped reads are assembled by incorporating left-over reads. This leads to a new kind of assembly problem, which we call reassembly problem. Two kinds of read sets have to be assembled. While the whole set of mapped reads has to be assembled following the ordering of their mapping positions, only some left-over reads have to be incorporated in the assembly. A left-over read is only incorporated if it has a high quality overlap with a mapped read in order to recruit only leftover reads that belong to the respective region. Though the mapped reads have already an order defined by their mapping positions they can be rearranged in the reassembly process. This happens if a deletion or small insertion occurred in the target genome regarding the reference genome or a better placement of a read becomes reasonable due to a replacement or an incorporation of other reads. We will discuss methods for reassembly in Chapter 4 and Chapter 5 , while we present the main workflow of the homology-guided assembly approach in this chapter.

### 3.1. Workflow

After the read data is filtered for erroneous reads, the high quality reads are mapped against a reference genome to receive a first ordering. Some reads belonging to homologous regions can contain a smaller number of SNPs and short indels and still map onto the reference genome, while reads that belong to highly polymorphic regions or insertion regions in the target genome will not align to the reference. This is illustrated in Figure 3.1.

In the following, mapped reads are reassembled in order to accurately reveal deletions and small insertions and additionally incorporate some left-over reads that belong to longer highly polymorphic and longer insertion regions. The left-


Figure 3.1.: The target genome differs from the reference sequence in one highly polymorphic region containing SNPs and one insertion region. The read sequences of the conserved regions are aligned to the reference genome, while the reads belonging to the polymorphic and insertion region do not align to the reference genome. They are pooled together with erroneous reads and repetitive reads in the set of left-over reads.


Figure 3.2.: Reads that are mapped to the reference genome are partitioned into blocks. Here, reads are pooled into block $i$ and $j$. All non-alignable reads are pooled as left-over reads. The left-over read set contains erroneous and repetitive reads as well as reads that belong to divergent regions. The region between the blocks $i$ and $j$ is highly polymorphic and, thus, no read of the target sequence was mapped to the reference in the respective region. In the next step, the blocks $i$ and $j$ are reassembled by incorporating left-over reads that overlap with reads from the block. In an ideal scenario, the assembled sequence covers the regions of the blocks as well as the highly polymorphic region between them.
over reads are a mixture of erroneous reads, repetitive reads and those that are referring to highly diverged regions and it is not obvious which read belongs to which of these classes. Unfortunately, the set of left-over reads can have the size of $5 \%$ to $25 \%$ of all reads.

It is self-evident that the reassembly problem and the incorporation of left-over reads in particular gets harder with increasing number of reads. To keep the amount of reads to be reassembled within a reasonable limit, the mapped reads are partitioned into regions of overlapping alignments, called blocks. The reads are assigned to their respective block and each block is reassembled separately. In detail, the mapped reads are partitioned using a static region size or dynamically by using regions with zero coverage or repetitive regions as natural borders. Two consecutive blocks are assembled together by incorporating the left-over reads that overlap with the reads of these blocks. An illustration of a reassembly of two blocks is shown in Figure 3.2. Afterward, the produced contigs can be further scaffolded. In the process of scaffolding, neighbored contigs can be merged within one scaffold using mate-pair information.

The whole approach is implemented in the short read analysis framework SHORE [ $\mathrm{OSC}^{+} 08,\left[\mathrm{SOO}^{+}\right]$that is specifically designed for resequencing projects with short read data. SHORE executes the following main steps:

1. Filtering: Trimming and quality filtering of reads.
2. Alignment: Reads are aligned to reference genome and left-over reads are pooled.
3. Partitioning: Aligned reads are partitioned into blocks of reads belonging to the same local region.
4. Reassembly: Assembly of the blocks to contigs by incorporating left-over reads.
5. Scaffolding: Merging and scaffolding of the contigs.

The pipeline includes several tools developed for short read data. In the alignment step, alignment tools like BWA [LD10], Bowtie [LTPS09] and GenomeMapper [SHO ${ }^{+}$09] are applied. GenomeMapper aligns reads simultaneously against multiple reference genomes after integrating these references in a single data structure. The other mapping tools, BWA and Bowtie, are discussed in Section 2.2. For the reassembly step, de novo assemblers like VELVET [ZB08], ABySS [SWJ ${ }^{+}$09] and EULER-SR [CP08] are supported as well as LOCAS and SUPERLOCAS, which are specifically designed to reassemble low sequencing depth data. In addition SUPERLOCAS is the only assembly tool that provides an efficient method for the incorporation of left-over reads. LOCAS and SUPERLOCAS will be presented in detail in Chapter 4 and Chapter 5. In the scaffolding step of SHORE, the scaffolding tool BAMBUS [PKS04] is utilized.

The presented methods have been mainly developed and implemented by Stephan Ossowski and Korbinian Schneeberger.

## 4. Short Read Assembly with a Low Sequencing Depth (LOCAS)

This chapter gives an overview of the workflow of the assembler LOCAS and implemented algorithms.

### 4.1. Overview

The assembly tool LOCAS is designed to assemble short to medium sized reads at a low sequencing depth. Therefore, the assembler extends the classical overlap-layout-consensus approach, which was originally developed to assemble Sanger reads. The overlap graph is reduced by a transformation into a path graph following the ideas of Myers et al. Mye95, MSD ${ }^{+} 00$, Mye05. In the path graph, regions that can be unambiguously assembled are merged and represented as one vertex.

The main steps of the workflow of LOCAS are as follows:

1. Preprocessing: Detection of pairs of reads that have an identical $k$-mers
2. Overlap phase: Calculation of overlap alignments for detected pairs and construction of the overlap graph
3. Layout phase I: Transformation of the overlap graph into a path graph
4. Layout phase II: Cycle handling and extraction of final paths
5. Consensus phase: Determination of consensus sequences as contigs

To adjust the general overlap-layout-consensus approach to short-read data of low sequencing depth, we modified the traditional algorithm that selects the final paths in the path graph in the layout phase II: In comparison to Sanger reads, the graph size is increased due to the higher amount of reads. In addition, the short overlap length in comparison to Sanger reads leads to more overlaps, including also false overlaps. This increases the graph size additionally and leads to a higher complexity of the graph. We modified the algorithm such that it handles the increased number of false overlaps and the larger graph as well as the relative increase of branches in the graph. Paths are selected in the final graph using a greedy strategy that aims at maximizing the total sequence depth and the total quality of overlap alignments of the final paths.

### 4.2. Preprocessing

After all read sequences have been loaded, identical read sequences are eliminated. Identical read sequences are detected with an enhanced suffix array of the SeqAn library [DWRR08]. The frequency of each read sequence is counted and one copy is kept for each sequence. Optionally, a filter for repetitive reads can be applied that deletes all reads that contain a $k$-mer that occurs more often than defined by a threshold in the original read set. The size of the $k$-mer and the threshold for the minimum frequency can be set by the user. Next, pairs of reads are detected that have the same $k$-mers. The $k$-mers are searched with an enhanced suffix array that is built for all reads. The detected read pairs are reported as candidate pairs that overlap potentially. The identical $k$-mers between candidate pairs are the seeds for an overlap alignment following on phase two.

### 4.3. Overlap Phase

Overlap alignments are calculated for each candidate read pair with a minimal overlap length allowing a maximal number of mismatches. Both values are input parameters to the assembly tool. The number of maximal mismatches is either static or it depends of the actual length of the alignment.

Unfortunately, the information to which DNA strand a read belongs to is not provided by current sequencing machines since the produced reads are sequenced randomly from both strands of the DNA. Thus, the overlap alignment of two reads is calculated by aligning the sequences directly to each other and by aligning the reversed complement of one sequence to the other sequence, which is called an alignment with similar orientation or dissimilar orientation, respectively. Usually, the alignment with the higher alignment score, which indicates a lower number of mismatches, is preferred.

The calculated overlap alignment information is represented by an overlap graph. Each read is represented by a vertex and each alignment by an edge. Two types of edges exist: An overlap edge corresponds to an overlap alignment. A containment edge represents a global alignment and indicates that one read is aligned over its full length to the other read. If these two reads differ in their length, one read is contained in the other read. A weight that corresponds to the length of the alignment is assigned to each edge. Further, a score is assigned that is equal to the alignment score and describes the quality of the alignment.

For each overlap edge, the attributes orientation and direction are stored. The orientation is set to true if the corresponding reads align in similar orientation or to false if they align in dissimilar orientation, meaning that one sequence is aligned to the reversed complement of the other. The direction is set to right if the first read is elongated at its 5 '-end by the second read. Otherwise, the direction is set to left. Thus, the overlap graph is implicitly a directed graph if we consider only overlap edges and leaving out the containment edges: the overlap edges of a


Figure 4.1.: (A) Eight reads are shown that align pairwise to each other. Except the fourth and the fifth read all reads are from the same DNA strand. Thus, the third reads aligns to the reversed complement sequence of the fourth read. The fourth and the fifth read align without building the reversed complement to each other. The reversed complement of the fifth read aligns with the sixth read. (B) For these reads and their alignments a seq-path is introduced in the overlap graph. The edge between the vertices of the third and the fourth read and the edge between the vertices of the fifth and the sixth read have a false orientation. For each of these edges the direction of the next edge is opposite to their direction.
vertex that are directed to the left correspond to ingoing edges and edges that are directed to the right to outgoing edges.

The consensus sequence of a path in the overlap graph is the consensus sequence of the aligned reads that are represented by the vertices along the path and the alignment information of the edges of the path. Since edges in the overlap graph are assigned with a direction and orientation, a path is not simply a list of edges that are connected with each other. For example, two edges that are directed to the right can only be part of a path if the orientation of the first edge is true and hence the underlying reads are aligned in the same orientation. The same holds for two left directed edges on a path. In contrast, if the orientation of the first edge is false, the corresponding reads align in dissimilar orientation and the direction of the second edge has to be opposite of the first edge. For an illustration, see Figure 4.1 .

We define a path that considers the orientation and direction of edges a seq-path. It is defined as follows:

Definition 4. A seq-path is a sequence of consecutive overlap edges in the overlap graph such that for each pair of consecutive edges $e_{1}$ and $e_{2}$ holds that the edges $e_{1}$ and $e_{2}$ have the same direction if the orientation of edge $e_{1}$ is true and the opposite direction if the orientation of edge $e_{1}$ is false.

After the graph construction, the number of edges is decreased by reducing the redundancy in the graph. For vertices that are connected with a containment edge and, thus, represent the same sequence information, an exemplar vertex is chosen and the other vertices are assigned to it. For vertices assigned to the exemplar vertex, all edges are deleted except the containment edge to the exemplar vertex. Thus, the exemplar represents now additionally the read sequences of its contained

```
Read 1: AGCTGCGATGCGATGCGTAGTCGTTG
Read 2: GATGCGATGCGTAGTCGTTG
Read 3: CTGCGATGCGATGCGTAGT
Read 4: TGCGTAGTCGTGCGAACGCTGCGAATG
Read 5: GTAGTCGTGCGAACGCTGCGAATG
Read 6: TGCGTAGTCGTTGCGAACGC
Read 7: GCGTAGTCGTTGCGAACGCTGCG
```



Figure 4.2.: Seven read sequences that are aligned to each other are shown. Most of the reads overlap with each other while read 2 , read 3 and read 5 , read 6 , read 7 align globally with read 1 and read 4 , respectively. The overlap graph of the reads is shown on the right. Each read is represented by a vertex and each overlap alignment by an overlap edge (solid). The global alignments are represented by containment edges (dashed). Read 1 and read 4 are exemplar vertices. For the other reads, all edges except the edge to the exemplar vertex are deleted (dotted).
reads.
The exemplar vertices are chosen using the following algorithm. A list $L$ of all potential exemplars is built. The read sequence of such a potential exemplar vertex has to be longer than each read sequence of the vertices that are connected to it with a containment edge. A score is assigned to each potential exemplar vertex in $L$ that is the average alignment score of its containment edges. $L$ is sorted according to this score. The vertex $x$ with the highest score is iteratively taken from $L$ and assigned as exemplar vertex to each vertex $v$ that has a containment edge to it and to that no exemplar vertex has been assigned until now. Further, the vertex $x$ and all vertices that have been assigned to it are deleted from $L$.

Consequently, for vertex $v$ an exemplar vertex $x$ is chosen that has the highest average alignment score of its containment edges and its read sequence is at least as long as the read sequence represented by $v$. For all vertices that are assigned to an exemplar vertex, all edges are removed except the edge to the exemplar vertex. See Figure 4.2 for an illustration of the reduction.

### 4.4. Reduction and Path Graph Construction

In layout phase I, the overlap graph is further reduced by deleting transitive edges that are defined as follows:

Definition 5. An overlap edge $e_{t}=(v 1, v 2)$ with weight $w_{t}$ is transitive if the following holds:

1. two edges $e_{1}=\left(v_{1}, x\right)$ and $e_{2}=\left(x, v_{2}\right)$ with weights $w_{1}$ and $w_{2}$, respectively, exist such that $w_{1} \geq w_{t}$ and $w_{2} \geq w_{t}$,
2. $e_{1}$ and $e_{2}$ are a seq-path,
3. the direction of $e_{t}$ is equal to the direction of $e_{1}$ and
4. the orientation of $e_{t}$ is true if the orientations of $e_{1}$ and $e_{2}$ are equal or the orientation of $e_{t}$ is negative if the orientations of $e_{1}$ and $e_{2}$ are not equal

For a transitive edge $e_{t}$ it holds that the edges $e_{1}$ and $e_{2}$ can exist in four different cases regarding their orientation and direction. These cases and the underlying read alignments are illustrated in Figure 4.3 .

```
Algorithm 4.4.1: DELETETRANSitiveEdges()
for each vertex \(v\)
    do \{sort edges adjacent to \(v\) in decreasing order of their weight
for each vertex \(v\)
```



```
for each edge \(e\)
    do \(\left\{\begin{array}{c}\text { if } e \text { is marked } \\ \text { then delete } e\end{array}\right.\)
```

A transitive edge represents redundant alignment information. Thus, each transitive edge $e_{t}$ can be deleted from the overlap graph. The information of each transitive edge $e_{t}$ is saved in form of a transitive edge weight of edges $e_{1}$ and $e_{2}$. The transitive edges are found and reduced using Algorithm 4.4.1. For each vertex $v$, the adjacent edges are sorted in decreasing order of their weight. Then, seq-paths that consist of two edges $e_{1}=(v, x)$ and $e_{2}=(x, w)$ are enumerated. Note that the seq-paths are enumerated in decreasing order of the weight of their edges. For each seq-path $p=e_{1}, e_{2}$, it is checked whether an edge $e_{t}$ with $e_{t}=(v, w)$ exists.


Figure 4.3.: If three read sequences show pairwise overlaps with each other, a transitive edge can occur in the overlap graph. (A) Four pairwise alignment settings of reads are shown that induce a transitive edge in the overlap graph. A read is drawn as an arrow pointing to right if the read sequence is aligned or as an arrow pointing to left if the reversed complement sequence of the read is aligned. For example, in the lower right alignment the first read is aligned to the reversed complement of the second read and the third read. The second and third read align to each other and thus also their reversed complements do. (B) For each alignment case, the corresponding sub-graph is shown. The three edges represent the pairwise alignments. The direction of all edges is right, which is indicated by an arrow, since all reads are elongated at their 5 '-end. The orientation is given by a label. In the lower right alignment case, two edges with false orientation appear in the sub-graph. These edges represent the alignments of the first read to the second and third read. Their orientations are set to false since the first read is aligned with the reversed complements both reads. The remaining edge, with true orientation, represents the alignment of the second and the third read.

If edge $e_{t}$ is transitive with respect to $e_{1}$ and $e_{2}$ following Definition 55, we mark $e_{t}$ as transitive and increase the transitive edge weight of $e_{1}$ and $e_{2}$. This procedure is repeated until we find an edge $e_{t}$ that has the same direction like $e_{1}$ but greater weight than $e_{1}$ or $e_{2}$. Then the next seq-path is considered for $v$. After all vertices are processed, marked edges are deleted.

The reduced overlap graph is transformed in a path graph. Therefore, all unique seq-paths of maximal length are determined in the overlap graph. A seq-path is unique if there exist no other seq-path that is adjacent to an inner vertex of the seq-path. For each unique seq-path of maximal length in the overlap graph, two vertices connected by an inner edge are introduced in the path graph. This structure composed of two vertices and an inner edge is called seq-vertex. The two vertices of the seq-vertex structure represent the ends of the unique seq-path in the overlap graph or, more precisely, the outer ends of the first and the last read sequence on the path. To both vertices of a seq-vertex structure a list of reads and a list of their pairwise alignments is assigned that originate from the seq-path in the overlap graph. To one vertex the original lists are assigned and to the other vertex the reversed lists are assigned. To reduce memory, only a link to the underlying read sequences and their alignments is stored for each seq-vertex. The consensus sequence of a seq-vertex is identical to the consensus sequence of the corresponding seq-path or to its reversed complement, depending on which


Figure 4.4.: An overlap alignment graph is transformed into a path graph. (A) The overlap graph and the aligned read sequences that are represented by the vertices $b$, $d$ and $e$ are shown. The overlap graph is transformed into a path graph, which is shown in (B). For each unique path in the overlap graph an inner edge is introduced in the path graph (drawn in solid). For example, the unique path between $b$ and $d$ in the overlap graph is represented by the inner edge $\left(b^{\prime \prime \prime}, d^{\prime}\right)$ in the path graph. If two vertices in the path graph represent two different ends of the same read, a real edge is introduced (drawn as dashed lines). An example is the real edge $\left(d^{\prime}, d^{\prime \prime}\right)$. Vertices $d^{\prime}$ and $d^{\prime \prime}$ represent the same read since they both correspond to vertex $d$ in the overlap graph. They represent different ends of the same read, since $d^{\prime}$ has an inner edge to $b^{\prime \prime \prime}$ representing an overlap alignment at the 3 '-end of the read and $d^{\prime}$ has an inner edge to $e^{\prime}$ representing an overlap at the 5 '-end of the read.
direction the seq-vertex will be traversed. Note that every overlap edge in the overlap graph is already a unique seq-path. Consequently, every overlap edge will be represented by a seq-vertex in the path graph.

To connect seq-vertices in the path graph, for each adjacency between unique seq-paths in the overlap graph a real edge is inserted into the path graph. A real edge is introduced between two vertices in the path graph if these vertices represent different ends of the same read, see Figure 4.4.

To consider only valid paths for the consensus sequence, we have to make sure that a read sequence that has been traversed from one side is not traversed again from the other side. Therefore, we define $c$-paths as follows:

Definition 6. A $c$-path is a sequence of consecutive edges in the path graph that alternates strictly between inner edges and real edges starting with a real edge.

In other words, a c-path is a sequence of seq-vertex structures alternating with real edges. The consensus sequence of a c-path is determined using the reads and the alignment information of the seq-vertices along the c-path. The read list of a c-path is determined by appending the read lists of the seq-vertices while the last read of each seq-vertex is omitted. Only for the last seq-vertex of the c-path the whole read list is added. The corresponding list of overlap alignments is received


Figure 4.5.: In the path graph, different cycle types can occur. (A) An undirected cycle is shown. The two c-paths connect the same vertices. If the consensus sequences of both c-path are similar to each other, the structure arises from a sequencing error or SNP. If the consensus sequences of both c-paths are dissimilar a false alignment is in most of the cases the reason. (B) A directed cycle that usually arises from repeats or polymorphisms is shown. The c-path can be traversed an infinite number of times and thus should be cut. (C) A composed structure is shown. An undirected cycle offers two alternative paths through the graph. In addition, two directed cycles exist due to the alternative routes. A repeat region is represented by the c-path that does belong two both directed cycles but not to the undirected cycle. If the undirected cycle is similar then the repeat regions occurs with two copies in the target genome. Otherwise, the cpaths of the undirected cycle represent the two region that appear between three copies of the repeat in the target genome. Nevertheless, both directed cycles have to be cut since they can also originate from sequencing errors and lead to errors in the assembly.
by appending the list of overlaps of the seq-vertices with each other. This is feasible since two seq-vertices connected by a real edge represent the same read, which is the first and last read of the second and first seq-vertex, respectively. The length of a c-path is the length of its consensus sequence. Further, the length of a c-path regarding to two selected reads $s$ and $t$ is defined as the length of the consensus sequence of the c-path between the reads $s$ and $t$.

### 4.5. Cutting Cycles and Similar Structures

In the next step, cycles in the path graph that arise from sequencing errors and repetitive regions in the target genome are handled. To this end, we distinguish between three different types of cycles. A directed cycle is a valid c-path that enables to traverse a vertex more than once. In fact, every vertex in the cycle can be traversed an infinite number of times. These cycles represent repeats and have to be cut since the consensus sequence of c-paths adjacent to directed cycles represent regions that originate from different regions in the genome. These regions should not be associated with each other in an assembly and, thus, connecting edges are deleted. An undirected cycle contains two distinct c-paths that
connect the same start and end vertices. This is called undirected, because both c-paths together create no c-path and hence cannot be traversed infinite times. Instead, it represents alternative routes through the path graph. The c-paths of an undirected cycle have either a similar or a dissimilar consensus sequence. The first kind of cycle is called similar undirected cycle and arises from sequencing errors or polymorphisms. The second kind of cycle is called dissimilar undirected cycle and arises from repeats or false alignments. For both cycle types, one of the c-paths has to be cut since the consensus sequence can contain only one of the alternatives. In Figure 4.5 all three cycles types are shown.

```
Algorithm 4.5.1: CalculateSpanningTree()
    PriorityQueue \(\leftarrow\) create Priority Queue of all real edges based on edge
                                    score
UnionFind \(\leftarrow\) create Union Find structure by defining each seq-vertex as set
SpaTree \(\leftarrow\) empty List of real edges
DisEdges \(\leftarrow\) empty List of real edges
while PriorityQueue not empty
```



Cycles are handled by creating a spanning tree in the path graph such that no directed and no undirected cycle is part of the solution. Consequently, c-paths belonging to distant regions in the target genome are disconnected. To determine the spanning tree, Algorithm 4.5.1 is applied to the path graph by selecting iteratively real edges. The algorithm is a variation of Kruskal's algorithm [KJ56 which finds a minimum spanning tree for an undirected weighted graph. First, real edges are scored by the quality of overlap alignments and sequencing depth assigned to the two seq-vertices connected by the real edge. Then, all real edges are enumerated in a decreasing order of their score such that regions of high sequencing depth


Figure 4.6.: A directed cycle is cut in a path graph. (A) A directed cycle with short dangling paths is displayed. (B) The cycle is shown after all short paths have been cut off and the cycle has been cut open at each branch vertex.
and of high quality alignments are preferred for the assembly. An edge is only selected if neither an undirected cycle nor a directed cycle is introduced in the current solution, which is checked by Algorithm 4.5.2 and 4.5.3. Algorithm 4.5.2 determines whether a given edge introduces an undirected cycle in the current spanning tree and returns eventually the cycle. If the returned cycle is dissimilar, the edge is marked. Algorithm 4.5.3 checks whether an edge introduces a directed cycle in the current spanning tree. Finally, the spanning tree, which is induced by the selected edges in the path graph, is reported by Algorithm 4.5.1.

In the following, we will discuss Algorithm 4.5.2 and 4.5.3 in more detail. Both algorithms are called with a spanning tree and an edge. Algorithm 4.5.2 determines the existence of an undirected cycle in the spanning tree that is introduced with the given edge. All seq-vertices with degree of at least three in the neighborhood of the given edge are determined where the neighborhood is restricted by a heuristic threshold of 1000 bp . For each pair of the found seq-vertices, c-paths are determined that connect both seq-vertices. If there exist two disjoint c-paths that connect both seq-vertices such that only one of them traverses the given edge, the two c-paths constitute an undirected cycle. The detected cycle is reported.

Algorithm 4.5.3 reports if a directed cycle is introduced in the spanning tree with the given edge. For this purpose, marked edges will also be considered as part of the spanning tree. This is done to detect more existing directed cycles in the path graph, even those that are part of an undirected cycle that has been cut already. As a consequence, read sequences from repetitive regions will be isolated. The c-path of each directed cycle is cleaned of all short dangling paths, which can be adjacent to vertices with degree larger than two, called branch vertices, see Figure 4.6. Then, the c-path is cut at all repeat branches. Repeat branches are branch vertices of the directed cycle that are adjacent to at least one longer c-path that is not part of the cycle. The directed cycle and the repeat branches are recorded for each cycle. The consensus sequence of a directed cycle represents the repetitive sequence and the sequence between the copies of the repeat in the target genome. In an ideal scenario, there exist two repeat branches on the c-path of the cycle that indicate the start and end of the repetitive region. C-paths that are adjacent to these repeat branches but are not part of the directed cycle represent
other regions that occur before, between or after the copies of the repeat in the target genome. Repeat branches can be easily detected under the assumption of error free reads and assuming that the copies of a repeat region in the target genome are identical. In practice, the detection is complicated by branch vertices that lie on the directed cycle and are adjacent to paths that do not belong to the cycle. However, these paths are often short such that the branch vertices can be distinguished from repeat branches. Unfortunately, directed cycles can arise also due to sequencing errors. Since we cannot determine the correct order of the paths that are adjacent or on the directed cycle, we simply cut the cycle and do not relink the adjacent paths. Such a remodeling becomes possible if additional information is available, for example mate-pair information.

Algorithm 4.5.2: GetUndirectCycle(verL, ver $R$, SpaTree)
branchVertices $R \leftarrow$ seq-vertices with degree $\geq 3$ near ver $R$ in SpaTree branchVertices $L \leftarrow$ seq-vertices with degree $\geq 3$ near ver $L$ in SpaTree for each pair $(x, y)$ with $x \in$ branchVertices $R$ and $y \in$ branchVerticesL

$$
\begin{aligned}
& \text { (path } 1 \leftarrow \text { c-path between } x \text { and } y \text { on SpaTree } \\
& \text { if path1 exists } \\
& \text { do }\left\{\begin{array}{c}
\text { then }\left\{\begin{array}{c}
\text { path } 2 \leftarrow \text { c-path from } x \text { to } y \text { on SpaTree via } \\
\text { edge }=(\text { ver } R, \text { ver } L)
\end{array}\right. \\
\text { if path } 2 \text { exists } \\
\text { then }\left\{\begin{array}{l}
\text { undirectedCycle } \leftarrow \text { merge path } 1 \text { and path } 2 \\
\text { return (undirectedCycle) }
\end{array}\right.
\end{array}\right.
\end{aligned}
$$

Algorithm 4.5.3: cutDirectCyc(verL, verR, SpaTree, DisEdges)
directedCycle $\leftarrow$ c-path from verL to VerR on SpaTree traversing at most one edge of DisEdges
if directedCycle exists
(branches $\leftarrow$ all seq-vertices on directedCycle with degree $\geq 3$
for each $b \in$ branches
then $\left\{\begin{array}{l}\text { do }\left\{\begin{array}{c}\text { longestPath } \leftarrow \text { longest c-path from } b \text { to a leaf in SpaTree } \\ \text { without edges of directedCycle }\end{array}\right. \\ \text { if length (longestPath) < tresholdMaxLength } \\ \text { then delete all real edges of the subtree of } b \text { without } \\ \text { considering edges in directedCycle } \\ \text { else delete all real edges adjacent to repeat branch } b\end{array}\right.$
else return (false ) $)$

By assuming seq-vertices as vertices and real edges as edges Algorithm 4.5.1 returns an acyclic graph, the spanning tree on the path graph.

After Algorithm 4.5.1 has been applied, we search for fragmented directed cycles. A fragmented directed cycle is a c-path that has the same start and end vertex but one edge of the c-path is missing. Such a c-path occurs if an overlap between reads has not been detected and the related real edge is missing in the spanning tree. As for directed cycles that are not fragmented, the consensus sequences of adjacent paths represent regions of distant locations in the target genome that should not be assembled to each other. Thus, fragmented directed cycles have to be cut at the corresponding repeat branches.

The algorithm to detect and cut repeat branches of fragmented directed cycles works as follows: The spanning tree is searched for repeat branches by searching for vertices that are connected to at least two longer c-paths. Such paths need to have a consensus sequence with a length of at least 125 bp . We found this threshold to be a good trade off between false positive and true positive identified repetitive regions. Edges adjacent to these vertices are deleted.

### 4.6. Resolving Repeats Using Mate-Pair Data

With the additional information provided by mate-pairs, some repeat induced cycles can be resolved in the path graph following the strategy of Pevzner and Tang [PT01]. At present, the approach is restricted to repetitive regions that occur only with two copies in the target genome.

The repeat sequence and the sequence between the two copies of the repeat in the target genome are represented by a directed cycle in the path graph. In particular, the repeat sequence is represented by a sub-path of the directed cycle, which is called repeat-path. A repeat-path is either a single seq-vertex consisting of repeat branches or a path of two repeat branches connected by a c-path.

The sequence regions before and after the repeat copies are represented by paths that are adjacent to the repeat-path but not part of the directed cycle. They are called framing-paths. An example of a repetitive region and the corresponding directed cycle is illustrated in Figure 4.7 A.

A directed cycle can be re-modeled such that it represents the original order of the sequence in the target genome. Therefore, the repeat-path has to be duplicated and re-linked, which is also illustrated in Figure 4.7. However, these new adjacencies have to be confirmed by mate-pairs in the directed cycle and the framing-paths that restrict the order of the paths with their insert size.

Without mate pair information, directed cycles are detected, short dangling paths are deleted and the cycles are cut using Algorithm 4.5.3. If mate-pair information is available, Algorithm 4.6.1 is called instead. Beforehand, the detected directed cycle is cut from all short dangling paths.

With Algorithm 4.6.1 all possible repeat-paths of the directed cycle are determined. For each of these repeat-paths it is investigated whether the adjacent


Figure 4.7.: (A) A directed cycle in a path graph is shown. The repeat region is represented by the repeat-path between the repeat branches $R_{1}$ and $R_{2}$. The sequence between the two copies of the repeat in the target genome is represented by the path between $B_{1}$ and $B_{2}$. The path from $A_{1}$ to $A_{2}$, which represents the sequence before the repeat region in the genome, and the paths between $C_{1}$ and $C_{2}, C_{3}$ and $C_{4}$, and $C_{3}$ and $C_{5}$, which represent the sequence behind the copies of the repeat region in the genome, are called framing-paths. (B) Short dangling paths in the directed cycle are cut off. (C) The directed cycle is remodeled. The repeat-path is copied and re-inserted as path between $R_{1}{ }_{1}$ and $R^{{ }_{c}}{ }_{2}$. All framing-paths of $R_{2}$ are disconnected from the vertex and linked to $R^{6}$. The vertex $B_{2}$ is disconnected from $R_{1}$ and linked to $R^{{ }_{1}}$.


Figure 4.8.: (A) For a path graph, a directed cycle with two assigned mate-pairs (red) is shown. The repeat-path of the cycle is between the repeat branches $R_{1}$ and $R_{2}$. The path between $B_{1}$ and $B_{2}$ represents the sequence between the copies of the repeat in the target genome. The framing-paths are the paths between $A_{1}$ and $A_{2}$ and between $C_{1}$ and $C_{2}$. The reads of the left mate-pair are assigned to the path between $A_{1}$ and $A_{2}$ and the seq-vertex of $B_{1}$, respectively. The insert size of the left mate-pair has approximately the same length as the path between them connecting consecutively $A_{2}$, $R_{1}, R_{2}$ and $B_{1}$. Thus, the mate-pair confirms this connection. The path that connects the right mate-pair by traversing consecutively the vertices $B_{2}, R_{1}, R_{2}, C_{1}$ and $C_{2}$ is confirmed if the insert size has approximately the same length as this path. (B) A fragmented directed cycle is shown. The repeat-path is between the branch vertices $R_{1}$ and $R_{2}$. The paths between $A_{1}$ and $A_{2}, A_{3}$ and $A_{4}, C_{1}$ and $C_{2}$ and between $C_{3}$ and $C_{4}$ are adjacent to the repeat-path. In addition, two mate-pairs (red) are assigned to these adjacent paths. The upper mate-pair assigns the path between $A_{1}$ and $A_{2}$ to the path between $C_{1}$ and $C_{2}$. The insert size of the mate-pair has approximately the same length as the path that connects them by traversing consecutively $A_{2}, R_{1}, R_{2}, C_{1}$ and $C_{2}$. This connection is confirmed by the mate-pair. The lower mate-pair confirms its connecting path that traversed consecutively $A_{4}, R_{1}, R_{2}, C_{3}$ and $C_{4}$.
paths of the repeat-path can be assigned to each other. Therefore, we search for reads in the framing-paths that mate with reads in the respective beginning of the directed cycle not considering the repeat-path. This is illustrated in Figure 4.8A. If the insert size of the mate-pair matches about the length of the repeat-path plus the distance to the mate-pair reads, one copy of the repeat-path can be assigned to the respective adjacent paths. If there are enough mate-pairs that confirm the assignment, the directed cycle is remodeled. Therefore, Algorithm 4.6.2 duplicates the repeat-path and re-links it according to the assignment.

```
Algorithm 4.6.1: RESOLVEDirectedCycle(directedCycle)
branches \(\leftarrow\) all vertices on directedCycle with degree \(>2\)
for each pair \(v_{1}\) and \(v_{2} \in\) branches that are the ends of a repeat-path
            (repeatPath \(\leftarrow\) repeat-path between \(v_{1}\) and \(v_{2}\)
        paths \(1 \leftarrow\) c-paths starting in \(v_{1}\) with each edge \(\notin\) directedCycle
        paths \(2 \leftarrow\) c-paths starting in \(v_{2}\) with each edge \(\notin\) directedCycle
        cycPath \(1 \leftarrow\) short c-paths starting in \(v_{1}\) with
                each edge \(\in\) directedCycle
        cycPath \(2 \leftarrow\) short c-paths starting in \(v_{2}\) with
                        each edge \(\in\) directedCycle
        MateCount \(1 c 2 \leftarrow 0\)
        MateCount \(2 c 1 \leftarrow 0\)
        for each mate-pair \(\left(m_{1}, m_{2}\right)\) with \(m_{1}\) assigned to paths 1
            and \(m_{2}\) assigned to cycPath2
```



```
        for each mate-pair ( \(m_{1}, m_{2}\) ) with \(m_{1}\) assigned to cycPath1
                and \(m_{2}\) assigned to paths 2
        do \(\left\{\begin{array}{l}\text { pathBetween } \leftarrow \mathrm{c} \text {-path connecting seq-vertex } \\ \text { repeatPath and cycPath } 1\end{array}\right.\) of \(m_{2}\) with
        if MateCount \(2 c 1 \geq \operatorname{minNum}\) and MateCount \(1 c 2 \geq \operatorname{minNum}\)
        then \(\left\{\begin{array}{l}\text { RemodelDirectedCycle(directedCycle, repeatPath) } \\ \text { return (true ) }\end{array}\right.\)
    return (false)
```

```
Algorithm 4.6.2: REMODELDIRECTEDCYCLE(directedCycle, repeatPath)
vertex \(1 \leftarrow\) start vertex of repeatPath
vertex \(2 \leftarrow\) end vertex of repeatPath
duplicatedRepeatPath \(\leftarrow\) repeatPath.copy ()
insert(duplicatedRepeatPath)
vertexDu1 \(\leftarrow\) start vertex of duplicatedRepeatPath
vertex \(D u 2 \leftarrow\) end vertex of duplicatedRepeatPath
for each edge \(e=(\) vertex 2 , otherVertex 2 ) with \(e \notin\) directedCycle
    do \(\left\{\begin{array}{l}\text { deleteEdge(e) } \\ \text { insertEdge(vertexDu2, otherVertex } 2)\end{array}\right.\)
dirEdge \(\leftarrow\) edge dirEdge \(=(\) vertex 1 , otherVertex 1\()\)
    with dirEdge \(\in\) directedCycle
deleteEdge(dirEdge)
insertEdge(vertexDu1, otherVertex1)
```

After Algorithm 4.5.1 has been applied, fragmented directed cycles are resolved by using mate-pair information. The procedure is similar to Algorithm 4.5.3. It is investigated whether adjacent paths of one end of the repeat-path can be assigned to adjacent paths of the other end of the repeat-path. If two reads of such paths, are mated in a way that their insert size matches approximately the distance between them when incorporating the repeat-path, they are assigned to each other, see Figure 4.8 B. If all adjacent paths can be assigned unambiguously and confirmed by a reasonable number of mate-pairs, the fragmented cycle is remodeled. Therefore, the paths that are assigned to each other are connected with one copy of the repeat-path. Thus, an alternative version of Algorithm 4.6.2 can be applied.

Finally, all fragmented directed cycles that could not be resolved by using matepair information are detected and cut by scanning for potential repeat-paths that do not lie on directed cycles as introduced in Section 4.5.

### 4.7. Contig Extraction

Since directed cycles and undirected cycles in the path graph were handled as described in Section 4.5 and Section 4.6 the resulting graph is a disjoint set of spanning trees, a spanning forest.

For each spanning tree in the forest, the longest path is determined to maximize the length of the consensus sequence. The longest paths in a spanning tree can be determined in polynomial time with the algorithm of Bulterman et al. $\left[\mathrm{BvdSZ}^{+} 02\right]$. First, the longest c-path starting at each leaf in each tree are determined and the end vertices are reported. In a second step, the longest c-paths starting at each end vertex are determined. These final c-paths are longest paths in the forest.

The consensus sequence is determined for each final path. Therefore, a multiple alignment is calculated for the read sequences assigned to each final path. The reads are ordered to a multiple alignment by considering their pairwise overlap alignments. The consensus sequence of the multiple alignment is determined by choosing the nucleotide with the highest relative frequency at each position in the alignment.

### 4.8. Software Architecture

The assembly tool LOCAS is written in C++ with use of the SeqAn library [DWRR08]. Figure 4.9 shows an UML diagram that presents the class hierarchy of LOCAS. The software operates in a serial manner. The class Assembler instantiates and calls consecutively the classes ReadCollection, Aligner, Reducer, Pather and ConsensusBilder. These classes represent different steps in the workflow of the software. Each class fulfills its function via the main function apply(), which calls private functions of the class. The class ReadCollection loads the read sequences, the class Aligner handles the construction of the overlap graph, the class Reducer transforms the overlap graph in a path graph, the class Pather determines the final paths in the path graph, and the class ConsensusBilder determines the contigs. Except for ReadCollection, the workflow classes instantiate and/or use an object of either the class AlignmentGraph, PathGraph or ContigCollection. All three classes do not represent steps in the workflow but rather blue prints of real data containing objects. The AlignmentGraph represents an overlap graph, the PathGraph represents a path graph and the ContigCollection a set of contigs. For each of the listed classes, only one instance exists during the workflow of the tool.

The ReadCollection holds several instances of the classes Mate and SingleRead. The class SingleRead is a blue print of a read. The attributes describe a read sequence with its nucleotide sequence, its id, its number of copies in the data set, its fasta entry and which reads are contained in it. The class Mate describes a mate-pair with the ids of the mate reads and the ids of the seq-vertices to that the mate reads are assigned later in the workflow.

The standard workflow of the tool starts with the main function of the ReadCollection. The read sequences and the mate-pair information are loaded from the input files. Each read is stored as a SingleRead object and for each mate-pair a Mate object is instantiated. Then, the set of SingleReads is reduced by calling private functions of ReadCollection which delete identical reads and assign contained reads to an exemplar read. After this step, the ReadCollection object is utilized in the workflow as a data bank of the reads and the mate-pairs.

In the overlap phase, the Assembler object instantiates an Aligner object. The main function of Aligner handles the construction of the overlap alignment graph that is represented by an AlignmentGraph object. The SingleRead objects of ReadCollection represent the vertices of the graph by their id. For each
 and Reducer. The class PathGraph, which is a blue print for a path graph, is modified by the class Reducer and Pather. The class instantiated by the class Assembler. The class AlignmentGraph, which represents the overlap graph, is modified by the class Aligner represent blue prints of mate-pairs and reads, respectively. The classes AlignmentGraph, PathGraph and ContigCollection are




overlap, an AlignInfo object is instantiated in the AlignmentGraph object. The AlignInfo class is a blue print for an overlap alignment between reads and, consequently, represents an edge of the graph. The attributes describe features of the overlap alignment like its length, its score, its number of mismatches as well as features of the edge like the direction, orientation and the ids of the connected vertices.

In layout phase I, an object of the class Reducer is instantiated in the Assembler object. The Reducer object has the right to modify an AlignmentGraph object to reduce the represented overlap graph. The actual reduction is performed by the main function of Reducer. Then, the reduced graph is transformed in a path graph. To this end, a PathGraph object is instantiated containing several Path objects that represent the vertices in the seq-vertices of the path graph and several PathConnection objects that represent the real edges. Each seq-vertex is represented by two Path objects with a consecutive id. The inner edge connecting them is not stored and exists implicitly.

The main workload of the tool is handled by the Pather object, which is instantiated by the Assembler object, in layout phase II. The Pather object has the right to modify the PathGraph object. Its main function calculates the spanning tree of the path graph in the PathGraph object. Further, the longest paths are calculated and stored as Path objects.

The Pather object hands over the Path objects containing the longest paths, to an instantiated ConsensusBuilder object. The ConsensusBuilder instantiates the ContigCollection object, which is only a container for Contig objects. For each Path object, a Contig object, which represents a contig, is instantiated. Each Contig object is responsible for extracting the contig of the assigned Path object. Finally, it contains the consensus sequence and the position-wise sequencing depth. The final set of contigs, which presents the final assembly solution, is collected and reported in an output file by the ContigCollection.

## 5. Extension of Homology-Guided Assembly (SUPERLOCAS)

In this chapter, we introduce algorithms for reassembly that are implemented in the software tool SUPERLOCAS.

In our approach reads are assembled by utilizing a mapping onto a reference genome. However, when using a mapping approach, regions of high divergence as well as long insertions can often not be mapped to the reference, leaving a set of left-over reads. These regions are reconstructed with SUPERLOCAS by incorporating high quality left-over reads in the assembly.

We developed SUPERLOCAS as an extension of the regular assembly algorithm implemented in LOCAS. SUPERLOCAS is adapted to the homology-guided assembly approach of the SHORE pipeline [ $\left.\mathrm{OSC}^{+} 08, ~ \mathrm{SOO}^{+}\right]$, which we introduced in Chapter 3. With SHORE, reads are mapped against a reference genome. The mapped reads are partitioned into blocks of given length and all left-over reads are pooled. Similar to LOCAS, SUPERLOCAS handles the reassembly step. It assembles each block individually while incorporating relevant left-over reads. In addition, the tool takes advantage of given mapping positions of reads.

### 5.1. Incorporating Left-Over Reads

In this section, we discuss the overall workflow of the assembly tool SUPERLOCAS.

The algorithm of SUPERLOCAS is an extension of the basic assembly algorithm that is implemented in LOCAS. In particular, SUPERLOCAS applies extended algorithms of LOCAS to calculate a pre-assembly of the left-over reads and to assemble mapped reads while incorporating a part of the pre-assembled left-over reads. The workflow is shown in Figure 5.1. First, an overlap graph based on the left-over reads is created, which is called left-over graph. The left-over graph is re-used in later steps of the workflow. Then, each block is assembled separately following the basic assembly algorithm with one additional operation: all connected components of the left-over graph whose reads overlap with reads of the current block are recruited and linked to the overlap graph of the block. The resulting overlap graph is processed with the standard algorithms to extract the longest paths and to determine the final contigs.

In the following, we will give more details of the workflow of SUPERLOCAS in Algorithm 5.1.1. First, overlap alignments are calculated for all left-over reads
A) $\qquad$ B)

C)

D)

E)
ACTCTAGTCTACTAGCGTGTCCGTGTC

Figure 5.1.: Workflow of SUPERLOCAS. (A) For the left-over reads, an overlap graph, called left-over graph, is constructed. (B) For the reads that are assigned to one block, another overlap graph is constructed. (C) Overlaps are detected between the reads of the block and the left-over reads. For each detected overlap, an edge is inserted between the graphs. (D) For each inserted edge, the adjacent connected components of the leftover graph are copied into the overlap graph of the block. (E) The extended overlap graph is processed with the standard algorithms of LOCAS. Final paths are extracted and the respective contigs are reported. The process from (B) to (E) is repeated for each block.
and represented in a left-over graph. Then, the following procedure is applied for each block: The overlap alignments between the reads of the block are calculated and the overlap graph is created. Next, overlap alignments between left-over reads and block reads are calculated. For each of these overlaps alignments, a new edge and a new vertex are inserted in the overlap graph representing the alignment and the left-over read, respectively. The new vertex is a copy of the vertex in the left-over graph and represents the same read.

In addition, all other vertices of the respective connected component in the leftover graph are copied into the overlap graph including all edges. This is done by traversing the connected components via a breadth-first search starting with the vertex that has been copied in the previous step. Note that each edge and each vertex of the left-over graph is copied at most once to the overlap graph. With this procedure the overlap graph of each block is extended such that overlapping left-over reads are also represented in the graph. Hence, some of the left-over reads are taken into account and can substantially elongate the resulting contigs.

```
Algorithm 5.1.1: ASSEMBLEWithLeftOverReads(leftis, blocks)
```

overlapsLeftis $\leftarrow$ calculate overlaps between leftis
graphLeftis $\leftarrow$ construct overlap graph for overlapsLeftis
while blocks not empty
(blockReads $\leftarrow$ blocks.getReads ()
overlapsBlock $\leftarrow$ calculate overlaps between blockReads
graphBlock $\leftarrow$ construct overlap graph for overlapsBlock
newOverlaps $\leftarrow$ calculate overlaps between blockReads and leftis
newEdges $\leftarrow$ construct edges for newOverlaps
do $\left\{\begin{array}{l}\text { newVertices } \leftarrow \text { vertices of newEdges in graphLeftis }\end{array}\right.$
for each v in newVertices
do $\left\{\begin{array}{l}\text { mark all edges and vertices visited during a breadth-first- } \\ \text { traversal starting at } v \text { in graphLeftis }\end{array}\right.$
graphBlock $\leftarrow$ copy newVertices, newEdges and all marked vertices
and edges into graphBlock)
return (graphBlock)

### 5.2. Making Use of Mapping Positions of Reads

In this section, we discuss extensions of the assembly workflow of LOCAS to make use of provided mapping positions of reads. These extensions are implemented in SUPERLOCAS. The read positions are used in the pre-processing as well as in the overlap phase of the workflow.

In the regular pre-processing of LOCAS, pairs of reads are determined that have an identical $k$-mer in their sequence. These pairs of read sequences, called
candidate pairs, overlap potentially with each other. Their common $k$-mer is used as seed for their alignment. This pre-processing step is extended SUPERLOCAS. In addition, to identical $k$-mers between read sequences, given mapping positions are analyzed to detect possible candidate pairs. Each pair of reads with a small distance to each other regarding the mapping positions is defined as candidate pair.

In the overlap phase, overlap alignments are calculated for each candidate pair. In the regular algorithm of LOCAS, the best alignment is calculated using the same alignment constraints like minimal overlap length and maximal number of mismatches for each candidate pair. However in case of SUPERLOCAS, five types of candidate pairs are distinguished:

1. both reads are block reads and have a small distance to each other
2. both reads are block reads, have a regular distance to each other and have an identical $k$-mer
3. both reads are block reads and have an identical $k$-mer while showing very distant alignment positions
4. both reads are left-over reads
5. one read is a left-over read and the other one is a block read

For each type, different alignment constraints are used and can be changed optionally by the user. Usually, more mismatches and a smaller overlap length are allowed for reads with a small distance to each other such that more overlap alignments can be detected in regions of low sequencing depth. To avoid false overlap alignments between distant reads, strict overlap constraints are set for these read pairs. With a reduced number of false overlaps, also the number of dissimilar undirected cycles decreases in the path graph. Overlap constraints for candidate pairs of type four and five are also very strict to avoid false overlaps of left-over reads with each other or with block reads.

### 5.3. Software Architecture

In this section, we give details about the architecture of the software SUPERLOCAS. The tool is written in C++ with use of the SeqAn library. Most classes are shared with LOCAS, while the classes Merger and AlignFinder are unique to SUPERLOCAS.

Figure 5.2 shows the classes of SUPERLOCAS in an UML diagram. The class Merger handles the workflow of the software by calling the class Assembler for the assembly step and calling the class AlignFinder to handle the incorporation of left-over reads. The class Assembler loads the read sequences and

Figure 5.2.: The class hierarchy of SUPERLOCAS is shown. The class Merger handles the workflow by calling the class Assembler that handles the regular assembly process and the class AlignFinder that handles the incorporation of the left-over reads in the assembly process. Except the classes Merger and AlignFinder all classes are shared with the software LOCAS.











constructs the overlap graph via the classes ReadCollection and Aligner, respectively. In addition, the class Assembler handles the transformation of the overlap graph into a path graph and its reduction, the determination of the final paths and the determination of contigs via the classes Reducer, Pather and ConsensusBilder, respectively. The classes AlignFinder, Aligner, Reducer, Pather and ConsensusBilder represent different steps in the workflow that manipulate objects of the classes AlignmentGraph, PathGraph and ContigCollection, which represent blue prints of the overlap graph, path graph and the set of contigs, respectively. The class ReadCollection is used to load the input reads and to store the read data for the rest of the workflow.

In Figure 5.3, the used objects of the software is shown. The software works in a serial manner, executing two main steps. In the first step, the left-over reads are loaded and overlap alignments between them are calculated. In the second step, each block is assembled individually by incorporating left-overs reads.

The first step handles the left-over graph construction and works as follows. The object :Merger instantiates the objects LeftOverRC:ReadCollection, LeftOverAG:AlignmentGraph and LeftOverAss:Assembler. The LeftOverAss:Assembler object calls LeftOverRC:ReadCollection to load the left-overs reads and instantiates the LeftOverA:Aligner object that creates the left-over graph. The left-over graph is stored as LeftOverAG:AlignmentGraph object. While the objects LeftOverRC:ReadCollection and LeftOverAG:AlignmentGraph are kept until the end of the overall workflow, the object LeftOverAss:Assembler is immediately deleted by :Merger.

In the second step, the overlap graph for each block is constructed, extended with left-over reads and contigs are reported. First, the objects BlockRC:ReadCollection, BlockAG:AlignmentGraph and BlockAss:Assembler are instantiated by the object :Merger. The BlockAss:Assembler object handles the following steps: The reads of the block are loaded by the object BlockRC:ReadCollection. The object BlockA:Aligner is instantiated to construct and modify the overlap graph of the block reads. The overlap graph is stored in the BlockAG:AlignmentGraph object.

Next, the object :Merger instantiates the object :AlignFinder, which detects overlap alignments between the left-over read set and the block read set, represented by the objects LeftOverRC:ReadCollection and BlockRC:ReadCollection, respectively. All left-over reads that overlap with the block reads are added to the object BlockRC:ReadCollection. Further, the overlap graph in the object BlockAG:AlignmentGraph is updated with the new overlap information by copying the corresponding vertices and edges from the LeftOverRC:ReadCollection and LeftOverAG:AlignmentGraph.

The object BlockAss:Assembler handles the last steps of the workflow. The objects :Reducer, :Pather and :ConsensusBilder are instantiated and executed iteratively. The object :Reducer transforms the overlap graph in the object BlockAG:AlignmentGraph into a path graph that is stored as :PathGraph ob-
ject. The reduction and determination of the final paths in the path graph are handled by the object :Pather. Finally, the object : ConsensusBilder determines and reports the consensus sequences of the contigs that are represented by the object :ContigCollection.

## 6. Evaluation and Comparison with Existing Assemblers

In this chapter, we present evaluations of LOCAS for de novo assemblies at a low sequencing depth. In addition, we evaluated SUPERLOCAS in various resequencing scenarios. Therefore, SUPERLOCAS was applied as part of the SHORE $\left.\mathrm{OSC}^{+} 08, \mathrm{SOO}^{+}\right]$framework to handle its reassemble step. For both tools, we present comparisons to current state-of-the-art assembly tools.

LOCAS and SUPERLOCAS were evaluated in three studies using short read data at low sequencing depths. In the first study, de novo assemblies of small genomic regions were simulated. The performance of LOCAS was compared to the short read assembly tools VELVET [ZB08, ZMMB09], EULER-SR [CP08], ABySS [SWJ+ 09] and SOAPdenovo [LLZ+09, LZR $\left.{ }^{+} 10\right]$. In the second study, we simulated a homology-guided assembly of a divergent strain of Arabidopsis thaliana. Since the other assemblers ABySS, SOAPdenovo and EULER-SR did not perform well enough for data with a low sequencing depth (shown in the first study), we only compared SUPERLOCAS and VELVET. In the third study, we evaluated LOCAS and SUPERLOCAS in a homology-guided assembly using Illumina reads from the resequencing project of $A$. thaliana, the 1001 Genomes Project (http://1001genomes.org/). In this study, we compared both tools with VELVET.

### 6.1. De Novo Assembly of Simulated Data

For the simulation studies of de novo assemblies, we generated Illumina GAIIx reads using METASIM [ $\left.\mathrm{ROA}^{+} 08\right]$ for the first and forth chromosome of $A$. thaliana Col-0. We used an error model for Illumina reads with a read length of 80 bp , which was estimated by resequencing the strain Col-0 and aligning the reads against the sequence of Col-0 [F Ott, pers. comm.]. Paired end reads were generated with an insert size of 300 bp and 200 bp , and a standard deviation of 30 bp and 20 bp for the first and fourth chromosome, respectively.

The simulated reads were assigned to the reference sequence corresponding to their origin positions and partitioned into blocks of length 10 kb . If two reads of the same mate-pair were assigned to different blocks, both reads were assigned to the block with the smaller index. Assemblies of the blocks, which correspond to local regions in the target genome, were performed separately using the assembly tools LOCAS, ABySS, EULER-SR, VELVET and SOAPdenovo. We ran all assemblers
using a wide range of parameter settings to show the achievable results with the respective assemblers.

For the performance analysis of the assembly tools, each local assembly was investigated separately. We used different measures to evaluate the assemblies. For each measure, the average value of all local assemblies was calculated. Measures that consider the length of the contigs are the $\operatorname{avg} N 50$ size, avgN90 size, the average mean, minimal and maximal contig size. In our study, the $N 50$ size is defined as the length of the longest contig such that all contigs of equal or longer length cover at least $50 \%$ of the positions of the block sequence. The N90 size is defined analogous to the $N 50$ size. The $\operatorname{avg} N 50$ size and the $\operatorname{avg} N 90$ size are defined as the average $N 50$ and $N 90$ size, respectively. For measures that consider the contig lengths, only valid contigs, which match the target sequence with at most $10 \%$ mismatches and have a minimal length of 100 bp , were considered. In addition, the average coverage $a v g C O V$ of the original block sequence with all valid contigs and the average error rate avgERR were determined. The error rate is the total number of errors divided by total length of all contigs of a block. The total number of errors comprises the number of mismatches in the alignment of all valid contigs plus the lengths of other contigs that could not be aligned.

The combination of $\operatorname{avg} N 50$ size and $\operatorname{avg} E R R$ rate showed to be a good estimate of assembly quality. Thus, we restricted the comparisons that are presented in the following to these two measures. For the other measures, see Chapter C.

### 6.1.1. Evaluation of Assembly for the First Chromosome of A. thaliana at a Sequencing Depth of 7.5x

For the first study, we used the first chromosome of $A$. thaliana Col-0 as target genome and simulated reads at a sequencing depth of 7.5 x . The results are shown in Figure 6.1. For $\operatorname{avg} E R R$ values lower than $1.5 \%$, LOCAS performed best with a maximum avg $N 50$ size of $4,558 \mathrm{bp}$. For an $\operatorname{avg} E R R$ higher than $1.5 \%$, VELVET performed best with a maximum $\operatorname{avg} N 50$ size of $5,500 \mathrm{bp}$. EULER-SR performed well in respect to the $\operatorname{avg} N 50$ size, but had high $\operatorname{avg} E R R$ values of 5 to $11 \%$. The $\operatorname{avg} E R R$ values of ABySS were with at most $1.2 \%$ very low, but the tool showed a low $\operatorname{avg} N 50$ size of at most $2,577 \mathrm{bp}$. The $\operatorname{avg} E R R$ values were even lower for SOAPdenovo, while the $\operatorname{avg} N 50$ size was the lowest for all assemblers with a maximum of $1,991 \mathrm{bp}$. We examined also CPU time and RAM needed to assemble the whole data set for each tool. The best performing method regarding CPU time was VELVET with 10 min in average, followed by LOCAS with 19 min , SOAPdenovo with 22 min and EULER-SR with 140 min . LOCAS and EULER-SR used only 18 MB of RAM, VELVET used 87 MB and SOAPdenovo used 236 MB .


Figure 6.1.: Performance comparison of low sequencing depth assemblies. Illumina GAIIx reads of the first chromosome of $A$. thaliana Col-0 were simulated at a sequencing depth of 7.5 x . The reads were assigned to the reference sequence corresponding to their origin position and partitioned into blocks of a length of 10 kb . The $a v g N 50$ size (average $N 50$ ) is plotted against the $\operatorname{avg} E R R$ (average error) for the assembly tools LOCAS, EULER-SR, ABySS, VELVET and SOAPdenovo. For each assembler, several runs are displayed corresponding to the different parameter settings. The data points of ABySS are drawn in orange, EULER-SR in green, LOCAS in red, VELVET in blue and SOAPdenovo in turquoise. Each point corresponds to a run.


Figure 6.2.: Performance comparison of assemblies with a sequencing depth of 5 x for the first chromosome of $A$. thaliana Col- 0 . The reads were assigned to the reference sequence corresponding to their origin position and partitioned into blocks of a length of 10 kb . The $a v g N 50$ size (average $N 50$ ) is plotted against the $a v g E R R$ (average error rate) for the assembly tools LOCAS, EULER-SR, ABySS, VELVET and SOAPdenovo. For each assembler, several runs are displayed corresponding to the different parameter settings. The data points of ABySS are drawn in orange, EULER-SR in green, LOCAS in red, VELVET in blue and SOAPdenovo in turquoise.


Figure 6.3.: Performance comparison of assemblies with a sequencing depth of 7.5 x for the fourth chromosome of $A$. thaliana Col-0. After the reads were assigned to their origin position in the reference sequence, they were partitioned into blocks of a length of 10 kb . The $\operatorname{avg} N 50$ size (average $N 50$ ) is plotted against the $\operatorname{avg} E R R$ (average error) for the assembly tools LOCAS, EULER-SR, ABySS, VELVET and SOAPdenovo. For each assembler, several runs are displayed corresponding to the different parameter settings. Each data point corresponds to one run. The data points of ABySS are drawn in orange, EULER-SR in green, LOCAS in red, VELVET in blue and SOAPdenovo in turquoise.

### 6.1.2. Evaluation of Assembly for the First Chromosome of A. thaliana at a Sequencing Depth of $5 x$

The second study was performed like the previous, while reads were simulated at a lower sequencing depth of 5 x . The results are shown in Figure 6.2, LOCAS performed best with an $\operatorname{avg} N 50$ size of $1,204 \mathrm{bp}$ and anavgERRof $1.4 \%$ in the best run. VELVET showed a maximum $\operatorname{avg} N 50$ size of $1,199 \mathrm{bp}$ with anavg $E R R$ of $2 \%$. For smaller $\operatorname{avg} E R R$ sizes of less than $2 \%$, the best $\operatorname{avg} N 50$ size of VELVET was $1,170 \mathrm{bp}$. EULER-SR showed an $\operatorname{avg} E R R$ that ranged between $8 \%$ and $14,4 \%$. Theavg $E R R$ values were low for SOAPdenovo while the maximum $\operatorname{avg} N 50$ size was 743 bp . ABySS showed the lowest $\operatorname{avg} N 50$ sizes in this comparison.


Figure 6.4.: Performance comparison of assembly with a sequencing depth of 5 x for the fourth chromosome of $A$. thaliana Col-0. The reads were assigned to their origin position in the reference sequence that was partitioned into blocks of length 10 kb . The avgN50 (average $N 50$ ) is plotted against the $a v g E R R$ (average error) for the assembly tools LOCAS, EULER-SR, ABySS, VELVET and SOAPdenovo. For each assembler, several runs are displayed corresponding to the different parameter settings. Each data point corresponds to one run. The data points of ABySS are drawn in orange, EULER-SR in green, LOCAS in red, VELVET in blue and SOAPdenovo in turquoise.

### 6.1.3. Evaluation of Assembly for the Fourth Chromosome of A. thaliana at a Sequencing Depth of $5 x$ and $7 x$

In order to validate the results of the previous studies, we performed a similar study by changing the target genome from the first to the fourth chromosome of A. thaliana. The reads were simulated at a sequencing depth of 5 x and 7.5 x . The results are shown in Figure 6.3 and 6.4. For a sequencing depth of $7.5 x$, LOCAS performed best with an $\operatorname{avg} N 50$ size of $4,384 \mathrm{bp}$ and an $\operatorname{avg} E R R$ of $1.4 \%$ in its best run. At the same average error range, VELVET showed an $\operatorname{avg} N 50$ size of $3,887 \mathrm{bp}$. VELVET showed a maximum $\operatorname{avg} N 50$ size of $4,043 \mathrm{bp}$ showing an $a v g E R R$ of $2.5 \%$. The $a v g E R R$ of EULER-SR ranged between $2 \%$ and $7.8 \%$. Its maximum $\operatorname{avg} N 50$ size was the lowest with $1,395 \mathrm{bp}$. The maximum avgN50 sizes of SOAPdenovo and ABySS were 1, 959 bp and $1,898 \mathrm{bp}$, respectively. Both assemblers showed again a low avgERR.

In the second study with a sequencing depth of 5 x , LOCAS was the best performing assembly tool regarding the $\operatorname{avg} N 50$ size and $\operatorname{avg} E R R$. It showed an $\operatorname{avg} N 50$ size of 1135 bp and an $\operatorname{avg} E R R$ of $0.095 \%$ in its best run. VELVET performed second best with an $\operatorname{avg} N 50$ size of 1072 bp and an $\operatorname{avg} E R R$ of $2 \%$ in its best run. The other assembly tools showed the same tendencies in their results as in the previous studies. EULER-SR showed high error rates ranging between $2.4 \%$ and $9 \%$ with a best avgN50 size of 566 bp. SOAPdenovo and ABySS showed again low $\operatorname{avg} N 50$ sizes while performing good considering the error rate. SOAPdenovo achieved in its best run an $\operatorname{avg} N 50$ size of 758 bp while ABySS showed an $\operatorname{avg} N 50$ of 768 bp in its best run. The avgERR of SOAPdenovo ranged between $0.15 \%$ and $2.7 \%$. For ABySS the avgERR ranged between $0.29 \%$ and $0.48 \%$.

### 6.2. Homology-Guided Assembly of Simulated Data

To evaluate performance in a homology-guided assembly approach, we simulated a resequencing study of an artificial $A$. thaliana strain using a sequencing depth of 7.5 x . First, we artificially generated a target genome by introducing SNPs, insertions and deletions into the reference sequence. The frequency of SNPs, deletions and small insertions was modeled according to a set of polymorphism from A. thaliana strains produced by the 1001 Genomes Project (www.1001genomes.org). This synthetic strain was used to simulate paired-end Illumina reads using METASIM. Paired-end reads were generated with an insert size of 200 bp and a standard deviation of 20 bp .

In the next step, reads were aligned to the reference genome Col-0 using SHORE $\mathrm{OSC}^{+} 08, \mathrm{SOO}^{+}$. A read is deemed alignable if the alignment contains a maximum of six mismatches and three gaps. Reads of a long insertion or reads spanning a position with a long deletion in the genome are usually not alignable. Of several alignment tools that are supported by SHORE, we preferred GenomeMapper [ $\left.\mathrm{SHO}^{+} 09\right]$ for this study because it allows for high edit distances,
allows gaps and has a high sensitivity.
Next, the chromosomes were partitioned into blocks of 25 kb for the reassembly step using SHORE. This was done using regions with zero coverage or repetitive regions as natural borders and by using a static maximum block size. Almost $2.5 \%$ of the reads were non-alignable and were defined as left-over reads. The left-over reads of all chromosomes were pooled since they could also not be separated in a real resequencing project.

The analysis was performed as for the first study in Section 6.1, with the following alteration: a contig was determined as valid if the global alignment to the target sequence had at most $10 \%$ mismatches and if the length of the contig was at least 500 bp . The measures were calculated not for each single block but for the pooled contigs of all 100 sequential blocks, called the 100-block. Thus, contigs were also considered in the analysis if they span two blocks with the help of left-over reads.

### 6.2.1. Evaluation of Homology-Guided Assembly for an Artificial A. thaliana Strain

Assemblies of the blocks incorporating the left-over reads were performed by applying the assembly tools SUPERLOCAS and VELVET. As VELVET does not provide a special mode for left-over incorporation, we used VELVET as follows: for each local assembly the complete set of left-over reads was given as an additional input. We omitted EULER-SR, SOAPdenovo and ABYSS due to their insufficient performance in the first study on data with low sequencing depth. In Figure 6.5, the $\operatorname{avg} N 50$ sizes and $\operatorname{avg} E R R$ values are shown for different runs of VELVET and SUPERLOCAS. SUPERLOCAS performed best regarding avgN50 size and $a v g E R R$. In addition, the results vary only slightly for different runs. We observed a maximum $\operatorname{avg} N 50$ size of $3,132 \mathrm{bp}$ and $2,446 \mathrm{bp}$ for SUPERLOCAS and VELVET, respectively. The error rates range from $0.17 \%$ to $0.21 \%$ for SUPERLOCAS and from $0.09 \%$ to $0.53 \%$ for VELVET. The average maximum contig size of SUPERLOCAS was larger (with up to $17,821 \mathrm{bp}$ ) in comparison to VELVET (up to $12,996 \mathrm{bp}$ ). The CPU runtimes per run ranged from 3h 12min for SUPERLOCAS to 7 h 51min for VELVET. SUPERLOCAS took 433 MB of RAM and VELVET took 224 MB . In addition, we examined the contigs of both tools regarding the appearance of insertion regions. These regions are present in the target genome but not in the reference genome. Most insertion regions with a length of at least 100 bp can only be assembled with the help of left-over reads. Figure 6.6 shows the number of insertion regions of different length that were assembled without errors by SUPERLOCAS and VELVET. Both tools performed in this task equally well, assembling a similar number of the insertions.


Figure 6.5.: Performance comparison of homology-guided assemblies on simulated data. We simulated a resequencing study of an artificial A. thaliana strain using a sequencing depth of 7.5 x . The simulated Illumina reads were aligned to the reference genome Col-0 and partitioned into blocks of 25 kb using SHORE. The assembly tools SUPERLOCAS and VELVET were applied to assemble the mapped reads of the first chromosome and the remaining left-over reads. The $\operatorname{avg} N 50$ size (average $N 50$ ) for the assembly tools SUPERLOCAS and VELVET (in left-over incorporation mode) is plotted against the $\operatorname{avg} E R R$ (average error). SUPERLOCAS is displayed in red and VELVET in blue.


Figure 6.6.: Number of detected insertion regions in a homology-guided assembly on simulated data. For the artificial A. thaliana strain in the simulated resequencing study, the total insertion regions in the target genome are plotted for different region lengths. In addition, the number of error-free regions assembled by VELVET and by SUPERLOCAS are shown.


Figure 6.7.: Performance comparison of reassemblies on real world data without utilizing left-over reads. Paired-end reads were produced by Illumina GAIIx with a length of 80 bp to a depth of 7.5 x for the first chromosome of $A$. thaliana Ler-1. Reads were aligned against the complete reference sequence (Col-0) and partitioned into blocks of length 25 kb using SHORE. LOCAS and VELVET are applied in paired-end mode for all blocks. The x-axis shows the $a v g N 50$ size (average $N 50$ ) and the y -axis the $a v g E R R$ (average error). The runs of LOCAS produced with different parameter setting are drawn in red and those of VELVET in blue.


Figure 6.8.: Performance comparison of reassemblies on real world data utilizing leftover reads. Illumina reads of the first chromosome of $A$. thaliana strain Ler-1 were aligned against the reference sequence (Col-0) and partitioned into blocks of length 25 kb using SHORE. Local assemblies were performed with SUPERLOCAS and VELVET by incorporating left-over reads. While SUPERLOCAS provides algorithms specifically adjusted to this task, VELVET had to assemble each block with the complete set of left-over reads. A boxplot of the $\operatorname{avg} N 50$ (average $N 50$ ) sizes of both assemblers is shown.

### 6.3. Application to Real Data

To test performance on real world data, we used sequence reads from the first chromosome of A. thaliana strain Landsberg erecta (Ler-1) produced within the 1001 Genomes Project WM09. Ler-1 was sequenced on the Illumina GAIIx with 80 bp paired-end reads to a depth of 7 x . Reads were aligned against the complete reference sequence and the first chromosome of the reference sequence was partitioned into blocks of at most 40 kb using GenomeMapper [SHO+09] and SHORE [OSC ${ }^{+} 08$ ].

For sequencing data of the A. thaliana Ler-1 strain, the original genome sequence was not available and, thus, the performance analysis differed in some points from the analysis of simulated data. As a proxy for the original sequence, we used the reference sequence. Assembled contigs of all blocks were pooled and aligned against the whole reference genome. If no left-over reads were provided for assembly, the performance was evaluated as for the simulated data. If left-over reads should be incorporated in the assembly, the evaluation differed. The error rate was calculated by considering only contigs that had a minimum similarity of $75 \%$ with the sequence of their 100 - block. All non-alignable contigs were not considered for analysis since these contigs do not have to be erroneous but can belong to other regions in the Ler-1 strain covered only by left-over reads.

### 6.3.1. Evaluation of Homology-Guided Assembly Without Incorporating Left-Over Reads

We applied both tools to assemble the reads of each block separately. Left-over reads were not provided to the assemblers. Instead of the $\operatorname{avg} E R R$, we estimated the average relative dissimilarity to the reference sequence over all blocks, denoted as $a v g D I S S$. For $a v g D I S S$ values higher than 1\%, VELVET performed best considering $\operatorname{avg} N 50$ size, while for $\operatorname{avg} D I S S$ values lower than 1\%, LOCAS showed the best $\operatorname{avg} N 50$ sizes, see Figure 6.7. We observed a maximum $\operatorname{avg} N 50$ size of $1,606 \mathrm{bp}$ and $1,526 \mathrm{bp}$ for VELVET and SUPERLOCAS, respectively.

### 6.3.2. Evaluation of Homology-Guided Assembly Incorporating Left-Over Reads

We then evaluated SUPERLOCAS and VELVET on real world data while incorporating left-over reads. For VELVET, each block was assembled with the complete set of left-over reads as in the second study. Contigs were determined as valid if they featured a similarity with the reference sequence of at least $75 \%$. We allowed this high percentage of dissimilarity since contigs that are constructed with the use of left-over reads often belong to insertion regions not represented in the reference genome. The avgDISS to the reference genome was not estimated since it would be increased by contigs that are build from left-over reads and represent
insertion regions. Consequently, the $\operatorname{avg} D I S S$ does not reflected the average error rate over all contigs. The $N 50$ sizes were higher for SUPERLOCAS with values consistently about 1500 bp . The N50 sizes of VELVET ranged between 901 bp and $1,435 \mathrm{bp}$, showing much higher sensitivity to parameter choice. A boxplot of the $N 50$ values of both assemblers is shown in Figure 6.8. Furthermore, SUPERLOCAS performed best regarding CPU runtime. One run of SUPERLOCAS was on average completed in 2 h 8 min , compared to an average running time of 7 h 32 min for VELVET. VELVET performed best considering RAM usage with only 1.73 GB , while SUPERLOCAS used 3.99 GB of RAM.

## 7. Discussion

In the first evaluation study, de novo assemblies of the first chromosome of $A$. thaliana at a low sequencing depth of 7.5 x were simulated. The assembly tools ABySS [SWJ ${ }^{+}$09] and SOAPdenovo [LLZ $\left.{ }^{+} 09\right]$ produced the lowest contig sizes in comparison to the other tools. Possibly, these short contig sizes occur since both tools are designed for a high sequencing depth. At least internal parameters of these tools have to be adjusted before they can be applied to data of low sequencing depth. The assembler EULER-SR [CP08] performed better considering contig sizes but showed very high error rates. The assembly tool operates with an initial step for error correction that substitutes $k$-mers in the read sequences that occur with a low relative frequency in the whole read set by highly similar $k$-mers with a high relative frequency. In case of low sequencing depth, this procedure could introduce errors in the read sequences since the relative difference of $k$-mer frequencies is very low. Thus, correct $k$-mers may be substituted by false $k$-mers. VELVET produced longer contigs sizes in comparison to LOCAS [KOS+ while showing higher error rates at the same time. These longer sizes may result from an improved repeat handling strategy that is implemented in VELVET [ZMMB09]. In contrast to other methods, the algorithm tries to resolve also repeat regions of higher complexity. The repeat resolution algorithm is applied iteratively to resolve repeats. Some repeats become only resolve-able if other repeats have been resolved already. Thus, more ambiguous regions can be spanned in the assembly. While longer contigs can be produced, the approach seems to introduce more errors into the assembly. In contrast, LOCAS achieved a good tradeoff between low error rates and high contigs sizes.

We validated our results from the first study by performing similar studies with an even lower sequencing depth of 5 x and on an additional chromosome, the fourth chromosome of A. thaliana. While SOAPdenovo and ABYSS showed error rates and contig sizes that differed by a constant factor between all three experiments, EULER-SR showed an even larger error rate for a sequencing depth of 5 x in comparison to a depth of 7.5 x . This increase in the error rate follows from the decreased amount of read data. As mentioned above, the error correction of EULER-SR relies on a high sequencing depth. Consequently, the performance of the correction will decrease with a low sequencing depth. In comparison to the other assemblers, the contig sizes of EULER-SR and VELVET decreased to a larger extend when moving from chromosome one to chromosome four. In contrast to the other assembly tools, LOCAS performed constantly regarding the contig size on both chromosomes. Thus, LOCAS seems to perform more robustly than VELVET when being applied to different target chromosomes. When we ran the
assembly tools with different sets of parameters, the results of LOCAS differ less than those from VELVET and ABySS. We conclude that LOCAS is less sensitive to the parameter choice. This is an important feature of an assembler since a manual parameter search is very time consuming and requires a certain expertise.

Considering runtime, VELVET was the best performing method in the first study. The other tools, including LOCAS, needed twice the time, expect from EULER-SR which needed 14 times as much. The different runtimes of VELVET and LOCAS are a result of their different assembly strategies. VELVET utilizes the de Bruijn graph approach that skips the calculation of pairwise overlap alignments between reads, while LOCAS calculates pairwise overlap alignments. These calculations increase the runtime of LOCAS significantly. The overlaps are represented in an overlap graph and since more overlaps are detected, the size and the complexity of the graph is larger compared to the corresponding de Bruijn graph. Consequently, the following procedures applied to the graph during the workflow require also more runtime. On the one hand, VELVET is superior regarding runtime. However, on the other hand is is very sensitive to different parameter settings. Hence, a lot of different settings have to be tested to assure that the best setting is found, which also consumes runtime. Considering RAM usage, LOCAS and EULER-SR performed best. In contrast, VELVET and SOAPdenovo required about four times and 11 times as much space, respectively. In LOCAS, local copies of objects are avoided leading to a low RAM requirement.

In the second study, which simulated a resequencing project, we compared VELVET and SUPERLOCAS [KOS ${ }^{+}$. SUPERLOCAS performed best considering the contig size and error rate. VELVET performed worse considering the contig size since it does not distinguish between left-over reads and reads that are assigned to blocks and, thus, treats these reads equally. Consequently, also erroneous left-over reads and false overlaps are introduced in the de Bruijn graph which leads to more branches and cycles in the graph. Finally, this results in shorter contigs. Due to its specialized method for incorporating left-over reads in the assembly, SUPERLOCAS produced longer contigs with a lower error rate. SUPERLOCAS does not treat reads equally, but uses different overlap alignment constraints for different reads, resulting in a more reliable incorporation of left-over reads. Further, repetitive left-over reads, which contain $k$-mers of a high frequency within the left-over read set, are discarded before they are considered for incorporation. This decreases the number of repetitive regions which often introduce errors in the assembly. Both assembly tools assemble an equal amount of longer insertion regions, which are regions that do not appear in the reference but in the target genome. These regions can only be assembled utilizing left-over reads. Thus, we can conclude that both tools are able to incorporate these reads in the assembly.

In a third study, we proved our previous results on real world data at a sequencing depth of 7x. We evaluated LOCAS like in the first study by assembling reads that had been assigned to blocks. SUPERLOCAS was evaluated like in the second study by incorporating left-over reads in the assembly of the blocks. First, we compared the performance of LOCAS and VELVET: Compared to VELVET,

LOCAS performed again very robust for different parameter settings. Similar to previous studies, LOCAS showed lower error rates than VELVET. In this study, the error rate is measured as the rate of the relative dissimilarity of contigs to the reference genome, which is approximately the sum of the error rate and the relative difference between target and reference genome. While VELVET showed larger contig sizes for high error rates, LOCAS experienced larger contigs for low error rates. Again, LOCAS achieved a better compromise between contig size and error rate. In the second part of this study, we performed assemblies of blocks by utilizing left-over reads and compared SUPERLOCAS and VELVET considering the produced contig sizes. SUPERLOCAS performed superior to VELVET for this special task. By including only high quality overlaps between left-over reads and reads of blocks, SUPERLOCAS retains the low complexity and size of its overlap graph. Thus, longer contigs can be reported. Similar to the previous study, SUPERLOCAS showed a robust performance for different parameter settings while VELVET's results strongly depend on the parameter choice.

In the second and third study, we also compared SUPERLOCAS and VELVET regarding their runtime. The runtime of VELVET was 2 to 3.75 times higher than the runtime of SUPERLOCAS. VELVET had to assemble all left-over reads over and over again for each block, while SUPERLOCAS provides a method to calculate a pre-assembly of the left-over reads, which can be later used for each block. Considering RAM usage, VELVET performed best, using only half of the RAM of SUPERLOCAS.

The presented results suggest that the overlap-layout-consensus approach implemented in LOCAS and SUPERLOCAS is better suited for low sequencing depth assembly than the de Bruijn paradigm used by VELVET, EULER-SR, SOAPdenovo and ABYSS. We optimized overlap alignments between reads to span even regions that are very sparsely covered with reads. However, by calculating exact alignments instead of matches of $k$-mers, the number of overlaps increases leading to a graph of higher complexity compared to the respective Bruijn graph. This high complexity can not be reduced by using a coverage-based cutoff used in de Bruijn graph approaches, which rejects regions from the assembly that are covered by a very low number of reads. The insufficient amount of reads permits the estimation of a reasonable value for a coverage-based cutoff. In addition, the probability of using false overlaps increases for alignment calculations that allow for several mismatches compared to exact matches of $k$-mers. Since optimal alignments are calculated, the construction of the overlap graph is slower than the construction of the de Bruijn graph. Nevertheless, for lower error rates, longer contigs and a higher overall coverage of the sequenced genome are the payoff for dealing with a more complex graph.

We believe that utilizing alignment positions of reads and incorporating left-over reads, as implemented in SUPERLOCAS, is a good compromise between resource heavy de novo assembly and simple homology-guided assembly approaches. Similar to de novo assembly, the integration of left-over reads allows for identification of highly polymorphic regions and insertions. In addition, our assembly approach
makes use of exact positions of aligned reads in a reference genome. This reduces the assembly complexity and the number of false overlaps. Further, we think that the assembly produced by our approach might be less affected by repetitive regions than de novo assemblies because some repeats are already detected during the alignment step. Since SUPERLOCAS distinguishes between left-over reads and aligned reads, it can incorporate of left-over reads more reliably than other short read assemblers. By creating an overlap graph for all left-over reads only once, SUPERLOCAS can re-use this graph for the assemblies of the blocks and, thus, performs much faster than other assemblers.

## 8. Conclusion

The study of sequence variations like SNPs, indels and longer variant regions plays an important role in the investigation of disease development and changes in physical characteristics of organisms. Since the introduction of new generation of sequencing technologies in 2005, the cost of resequencing has been reduced by an order of magnitude and the number of resequenced organisms has been increasing steadily.

The aim of resequencing projects is the detection of sequence variations between closely related species. While existing approaches are capable of detecting SNPs and indels, they do not address highly polymorphic regions and longer insertions sufficiently. With the aim of also revealing longer sequence variations, we investigated and extended the existing approach of homology-guided assembly.

We designed and implemented algorithms for resequencing projects of large genomes that are performed with short read data of low sequencing depth. In our homology-guided assembly approach, reads are aligned to a reference genome of a highly related organism. The reference genome is partitioned into blocks and reads aligned to one block are reassembled separately by incorporating left-over reads. Our algorithms for reassembly are based on an overlap-layout-consensus approach, which represents the input set of reads and their possible overlaps in an overlap graph. Since mismatches are allowed in the used overlap alignment, this approach is well suited for short read data of low sequencing depth. Our algorithms for reassembly are implemented in the assembly tools LOCAS and SUPERLOCAS.

LOCAS is specifically designed for de novo assemblies at a low sequencing depth and, thus, it is capable to assemble reads of local regions in the context of resequencing projects. SUPERLOCAS, the extension of LOCAS, allows for the execution of multiple reassemblies of consecutive blocks and handles the incorporation of a huge amount of left-over reads in the local assemblies. SUPERLOCAS was to the specific scenario of resequencing adapted. Alignment positions of reads on the reference genome can be utilized for the calculation of overlap alignments. This reduces the complexity of the assembly and the chance of false overlaps, which leads to longer and less erroneous contigs.

The performances of both tools were evaluated in two studies that simulated resequencing projects at a low sequencing depth of at most 7.5 x . Further, an additional study was performed using real world data from the 1001 Genomes Project. In these studies, local assemblies of blocks were performed. When SUPERLOCAS was applied, left-over reads were additionally incorporated into these local assemblies. We compared LOCAS and SUPERLOCAS with other state-of-
the-art assemblers for short read data. LOCAS and SUPERLOCAS achieved better results than the other short read assemblers or at least similar. For local reassemblies at a low sequencing depth, VELVET [ZB08, ZMMB09] and LOCAS performed best considering contig size and error rate. However, LOCAS seems to be less sensitive to the choice of parameters, while producing contigs that show a good trade-off between error rate and size. When incorporating left-over reads into the local reassemblies, longer insertion regions could be assembled with SUPERLOCAS and VELVET. However, SUPERLOCAS proved to be much faster and more robust to different parameter settings than VELVET. In addition, due to its ability to efficiently incorporate left-over reads, SUPERLOCAS produced longer contigs.

SUPERLOCAS has successfully been used for the assembly of various $A$. thaliana genomes such as Ler, C24, Bur-0 and Kro-0 in the context of the 1001 Genomes Project $\left[\mathrm{SOO}^{+}\right]$.

Within recent years, the sequencing technologies have steadily improved. The direction of this rapid development is not always easy to anticipate, e.g., three years ago, the short length of produced reads was a challenging task for assembly whereas today this read length has been already tripled for some technologies. Assembly algorithms that process this kind of data have to be steadily adjusted to the fast changes. At the same time, assembly algorithms will gain from improvements such as longer read lengths, which opens up new opportunities in assembly.

We assume that our method will become increasingly valuable with future improvements in sequencing technologies such as longer reads. Our overlap-layoutconsensus approach can benefit from longer reads since it is more robust to sequencing errors at the end of reads. Furthermore, computing overlap alignments rather than using exact matches of $k$-mers will become more important since longer sub-sequences have a higher probability of containing sequencing errors. In addition, an increased overlap length between reads will contribute to the reliability of left-over read recruitment. Finally, the potential of homology-guided assembly will grow steadily with increasing numbers of completely sequenced genomes.

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## A. Presentations

## A.1. Talks

- "Algorithms to Support Resequencing with Ultra Short Reads", BCI 2008, 9th September 2008, Trieste
- "LOCAS - a low coverage assembler for short reads", Short-SIG 2009 (special interest group meeting at ISMB), 28 th June 2009, Stockholm
- "LOCAS - a low coverage assembler for short reads", TüBiT 2010, 21st May 2010, Tübingen
- "LOCAS - a low coverage assembler for short reads", GCB 2010, 21st September 2010, Braunschweig


## A.2. Poster

- "LOCAS - A new low coverage assembler for short reads", presented at TüBit 2009, Tübingen
- "LOCAS - A new low coverage assembler for short reads", presented at ISMB 2009, Stockholm


## A.3. Articles

- "LOCAS - a low coverage assembly tool for resequencing projects", short paper, appeared in abstract book of GCB 2010
- "Homology-guided Assembly of the Four Diverse Arabidopsis thaliana Genomes Ler, C24, Bur-0 and Kro-0", under review at Plos Genetics
- "LOCAS - a low coverage assembly tool for resequencing projects", submitted to Bioinformatics


## B. Manual

## B.1. Introduction

LOCAS is a program to assemble short reads of second generation sequencing technologies. It explicitly handles low coverage data by allowing mismatches in the overlap alignment of reads.

An extra module, called SUPERLOCAS, provides some additional features for resequencing projects. In a resequencing project reads are mapped onto a closely related reference genome and a consensus from the mapped reads is calculated as an approximation of the new genome sequence. (Highly polymorphic regions and insert sites are not covered with this consensus.) SUPERLOCAS can be used to incorporate unmapped reads into the assembly of mapped regions and elongate this consensus. Further, SUPERLOCAS takes advantage of given mapping positions of reads. Both tools are written in C++.

## B.2. Availability

Binaries and source code can be downloaded from http://www-ab.informatik. uni-tuebingen.de/software/locas.

## B.3. Installing

We provide binaries for LOCAS and SUPERLOCAS that are compiled on a LINUX system (Redhat, 64-bit). Additionally, the source code is available.

## B.4. License Details

The source code is distributed under the terms of the GNU General Public License.

## B.5. Author

Juliane D. Klein

## B.6. Running LOCAS

You can run LOCAS from the command line as follows:

```
LOCAS -I input reads.fasta -O output folder -F fasta -L 23 -S 2
```

LOCAS will assemble all reads in the file "inputreads.fasta" by calculating overlap alignments with a minimal length of 23 and a maximum of 2 mismatches. The result is written to folder output-folder. LOCAS will create this folder if it does not exist.

## Required options:

$-I\langle$ string $\quad$ defines the full name (including location) of your read file
$-O\langle$ string $\quad$ the name of the new folder which LOCAS will create for its output
-F fasta or
-F fastq chooses between fasta and fastq file formats

## Additional options:

$-C\langle$ int $\rangle\langle$ int $\rangle \quad$ the first number defines the minimal length and the second number the minimal coverage of the contigs that should be reported (default: 00 )
$-S\langle$ int $\rangle \quad$ the maximal number of allowed mismatches in an overlap alignment between two reads (default: 4)
$-L\langle$ int $\rangle \quad$ the minimal allowed length of an overlap alignment between two reads (default: 27)
$-P$ kmer $\langle$ int $\rangle$ the length of the sub-sequence (kmer) which has to be equal in two reads before an overlap alignment is calculated (default: 13)

## B.6.1. How to choose the parameters kmer size and overlap length

First LOCAS searches for pairs of possibly overlapping reads. This is done by looking for equal kmers (sub-sequences of length k ) between two reads. After this filtering step, the real overlap alignments are calculated for all reads which share a kmer.

The parameter $-K$ controls the filtering step. The user can define for which length equal sub-sequences are detected between reads. With the parameter $-L$ the minimal length of an overlap alignment is set.

## B.6.2. Example of a LOCAS run

The data for an example can be found in the sub-folder "testset_locas". Open a shell and change into this folder. Then execute the following command:

```
LOCAS -I simulated_reads.fasta -0 my_locas_out -F fasta -L 21 -S 2
```

You can compare your results to those in sub-folder "locas_out". Now, you can experiment with the parameter a little. For example, you can discard some contigs by applying:

```
LOCAS -I simulated_reads.fasta -0 my_locas_out2 -F fasta
    -L 21 -S 2 -C 3 100.
```

Or you can change the minimal overlap length between reads by executing:

```
LOCAS -I simulated_reads.fasta -O my_locas_out3 -F fasta -L 19 -S 2
```


## B.7. Running SUPERLOCAS

SUPERLOCAS is especially designed for use in resequencing projects. Here all reads are mapped against the genome of a highly related species. Continuously mapped sub-regions can be defined as blocks. All reads can be assigned to one block or to a set of left-over reads.

Using SUPERLOCAS, you can reassemble the blocks and try to incorporate left-over reads. Reads from different blocks should be placed in different files, and the left-over reads should be placed in their own files, too.

Before you can start SUPERLOCAS, you have to create two special inputfiles. The SUPERLOCAS_Inputfile describes the input for SUPERLOCAS. The SUPERLOCAS_Outputfile describes the output for SUPERLOCAS. The first line in the SUPERLOCAS_Inputfile shows the names of all read files for the first block separated by a space character. In the second line you find all names of the read files of the second block and so on. In each line of the SUPERLOCAS_Outputfile you have to write the name of the output-folder of the corresponding block. For an example file, see the files "super_input_file" and "super_output_file" in the folder "testset_superlocas/myoutput".

SUPERLOCAS is started as follows:

```
SUPERLOCAS -I SUPERLOCAS_Inputfile -O SUPERLOCAS_Outputfile
    -LO left_over_file_1 left_over_file_2 -F fasta
```


## Required options:

$-I$ 〈string defines location and name of your SUPERLOCAS_inputfile
$-O\langle$ string $\quad$ defines location and name of your SUPERLOCAS_outputfile

- $F\langle$ fasta $\rangle$ or
$-F\langle$ fastq $\rangle \quad$ chooses between these file formats
$-L O\langle$ string $\quad$ defines left-over files
Kmer options (optional):
$-K m e r g\langle i n t\rangle \quad$ chooses kmer size which has to be equal in a read from the block and a read of the left-over set to calculate an overlap alignment (default: 30)
$-P$ kmer $\langle$ int〉 chooses kmer size which has to be equal in two block reads before an overlap alignment is calculated (default: 13)
$-K\langle$ int $\rangle \quad$ chooses kmer size which has to be equal in two left-over reads (default: 33)
Overlap length options (optional):
$-L m\langle$ int $\rangle \quad$ chooses minimal length of an overlap alignment between a block read and a left-over read (default: 30)
$-L t\langle$ int $\rangle \quad$ chooses minimal length of an overlap alignment between two block reads (default: 21)
-Llo $\langle$ int $\rangle \quad$ chooses minimal length of an overlap alignment between two leftover reads (default: 33)
Substitutions in overlap options (optional):
$-S m\langle$ int $\rangle \quad$ chooses maximal number of allowed mismatches in an overlap alignment between a block read and an left-over read (default: 1)
$-S t\langle$ int $\rangle \quad$ chooses maximal number of allowed mismatches in an overlap alignment between two block reads (default: 3)
-Slo $\langle$ int $\rangle \quad$ chooses maximal number of allowed mismatches in an overlap alignment between two left-over reads (default: 1)


## Additional options:

$-C\langle$ int $\rangle\langle$ int $\rangle \quad$ chooses with the first number the minimal length and with the second number minimal coverage of the contigs which should be reported (default: 00 )
$-D R\langle$ int $\rangle\langle$ int $\rangle \quad$ determines that all left-over reads are discarded which have more than a certain number of equal kmers in the set of left-over reads, the kmer size is defined with the first number and the second number defines the number of kmer matches (default: 21 500)

## B.7.1. Running SUPERLOCAS with mapping positions

If mapping positions are also available for reads you can switch on a mode of SUPERLOCAS that will take these information into account:
$-P \operatorname{pos}\langle i n t\rangle \quad$ defines kmer size as usual, but in addition an overlap alignment is also calculated if two reads are very close to each other with respect to their mapping positions
Further alignment constraints can be defined for very close or distant reads (optional):

| $-L t n\langle$ int $\rangle$ | defines minimal length of an overlap alignment between two block <br> reads which are close to each other (default: 11) <br> defines minimal length of an overlap alignment between two block |
| :--- | :--- |
| $-L t d\langle$ int $\rangle$ | reads which are distant to each other (default: 25) <br> defines maximal number of allowed mismatches in an overlap align- <br> ment between two block reads which are close to each other (default: |
| $-S t n\langle$ int |  |$\quad$| 2) |
| :--- |

## B.7.2. Understanding the parameters of SUPERLOCAS

SUPERLOCAS distinguishes between two types of reads: reads assigned to a block (because they mapped to the same region to a reference) and reads of the left-over set. The alignment constraints for these two types of reads differ and can be defined independently with the following options:

If two reads belong to a block then parameters $-L t\langle i n t\rangle,-P k m e r\langle i n t\rangle$, and $-S t\langle i n t\rangle$ define your alignment constraints. If both reads are left-over reads then parameter $-K\langle i n t\rangle,-L l o\langle i n t\rangle$, and - Slo $\langle i n t\rangle$ define the overlaps. If a block read is aligned to a left-over read then the constraints are set by - Kmerg $\langle$ int $\rangle$, $-L m\langle i n t\rangle$, and $-S l o\langle i n t\rangle$.

If mapping positions are available for the block reads then SUPERLOCAS can take them into account. This option can be switched on by applying the option $-P$ pos $\langle$ int $\rangle$ (instead of $-P$ kmer $\langle$ int $\rangle$ ) to define the kmer size. In this case SUPERLOCAS will not only look for equal kmers between reads to calculate an overlap alignment, but it will also try to overlap read with a very close mapping position. In this mode you can manipulate the overlap alignment constraints of two reads depending on their mapping positions. Two block reads can be classified as distant or close to each other with respect to their mapping position. In the first case the constraints for the overlap alignment are defined using -Ltd $\langle$ int $\rangle$ and $-S t d\langle i n t\rangle$, in the case of very close block reads with $-L t n\langle i n t\rangle$ and $-S t n\langle i n t\rangle$.

## B.7.3. Example of a SUPERLOCAS run

The sub-folder "testset_superlocas" contains the files of an example application. There are 16 blocks to assemble and 29199 left-over reads. A read file of single-end Illumina reads and one of paired-end Illumina reads belongs to each block.

You can start SUPERLOCAS by changing into the folder "testset_superlocas" and execute the following command:

```
superlocas -I myoutput/super_input_file
    -O myoutput/super_output_file -LO left_over_reads.fasta -F fasta
```

This should produce the same output as you can see in the folder output.
The two files "super_input_file" and "super_output_file" are the special input and outputfile you have to generate for use with SUPERLOCAS.

## C. Supplementary Tables

| OカヤてZ | LZT | LT0800＊0 | Z9L200＇0 | 679186＇0 | 976 | 6202 | 8LEE | $\angle \nabla 99$ | £SI | $\begin{array}{r} \varepsilon \\ \mathcal{L}^{\prime} \tau \tau \tau \\ \hline \end{array}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| LZOZZ | $8 \downarrow$ T | ャ6800＇0 | ZS6Z00＊0 | ZLZZ86＊0 | てヤ8 | L06T | ¢80¢ | 8LEG | 0¢T | $\begin{array}{r} \mathrm{L} \\ 8 \cdot \angle \triangleright Z \tau \end{array}$ |  |
| 69力tZ | OST | ST0600＇0 | E8LZOO＇0 | ${ }^{\text {®GST86＊0 }}$ | ZTOT | S6ZZ | ZヤLE | 6009 | 8ST | $\begin{array}{r} \dagger \\ \text { } \cdot 9 \tau S \tau \\ \hline \end{array}$ |  |
| 960ZZ | 697 | L600＇0 | 986200＇0 | 9LST86＇0 | 976 | ع60Z | ITちE | ITLS | โEโ | $\begin{array}{r} 8 \\ \text { て'9 \& } \\ \hline \end{array}$ | 乙 S－6T 7－¢โ：дəш丬 |
| 0عSIZ | 06T | T690T0＇0 | t06200＊0 | 6โヵT86．0 | SLII | 8ャ92 | 802t | SIt9 | ZLI | $\begin{array}{r} 6 \\ \log 97 \\ \hline \end{array}$ |  |
| 乙0\＆てZ | IOZ | 8T6010＊0 | SttE00＇0 | 608286＊ | Z90才 | カレもて | 8T8E | $\varepsilon 809$ | LET | $\begin{array}{r} \text { L } \\ \text { G. } 8 \mathrm{~L} \downarrow \end{array}$ | 乙 S－LT 7－\＆I：дəш丬 |
| ع99L乙 | TLZ | 6LOtTO＇0 | Z90E00＇0 | $68086{ }^{\circ} 0$ | D92T | ع68Z | OTSt | 6699 | ع8T | $\begin{array}{r} 9 \\ \angle .9 z<\tau \end{array}$ |  |
| 68GZZ | 292 | 98દとโ0＊0 | tLEEOO＇O | 89عE86＊0 | LZIT | 8992 | L80t | StE9 | 0ヵT | $\begin{array}{r} \text { Z } \\ 9 \cdot \operatorname{sst} \\ \hline \end{array}$ | 乙 S－ST 7－¢โ：גəШห |
| 8102Z | 0＜t | ع0દてZO＊0 | S9EE00＇0 | 8ヵてT86＊0 | EIIT | It92 | 960t | ヤ0t9 | L9T | $\begin{array}{r} \mathrm{S} \\ 0 . \mathrm{SSI} \end{array}$ |  |
| 692\＆Z | t 2 t | Z89IZO＊ | LLE00＇0 | LS8E86＇0 | $8 \downarrow 6$ | Stez | OヤLE | 7809 | LET | 60＇T8ZT |  |
| T0ETZ | カヤて | †06800＇0 | L8Z00＇0 | L66086 ${ }^{\circ}$ | LZ6 | 980Z | 988を | 8999 | SSI | I6＇6でT |  |
| LZとT乙 | £SI | 8SZ600＇0 | †88200＊0 | L8ヵT86＇0 | 6T0T | てTEZ | ZSLE | 6209 | 6SI |  |  |
| †9\＆IZ | 96T | 9SOLTO＇0 | tS6Z00＊0 | 29ET86＊0 | ZLIT | ヤL92 | 9عてt | てとャ9 | DLT | $\begin{array}{r} z \\ \varepsilon \cdot 089 \tau \\ \hline \end{array}$ |  |
|  | $6 \angle Z$ | tS97T0＇0 | S0E00＇0 | 88626 ${ }^{\circ}$ | LGZT | 6ع6乙 | 8SSt | $6 \varepsilon \angle 9$ | Z6T | $\begin{array}{r} 8 \\ \text { で } \begin{array}{r} 8 \\ \hline \end{array} \\ \hline \end{array}$ | ャ S－ST 7－¢โ：дəшィ |
| T0912 | ع6t | 66LEZO＇0 | L6ZE00＇0 | S8T8L6＊0 | 6LIT | 8SLZ | 0عてカ | 1879 | 08T | $\begin{array}{r} \mathrm{g} \\ \mathrm{~S} \cdot \mathrm{~s} 9 \mathrm{I} \end{array}$ |  |
| IIV | paddewun |  | 10113 | әбеләлоว | 06N | GLN | OSN | xew | u！w | ueaw |  |


səIQEL



| 9906T | TEヵ | 8T6Z820＇0 | GLZS0900＊0 | 906826＊ | Oカt $\tau$ | 6GSE | $\begin{array}{r} \dagger \\ \tau S \subseteq \end{array}$ | $\begin{array}{r} 9 \\ \tau G L \end{array}$ | Lてt | $\begin{array}{r} Z \\ \varepsilon \cdot \varepsilon \varepsilon 8 \end{array}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 8806T | $66 \varepsilon$ | LSLZ9Z0＇0 | 6ESZLSO0＇0 | LZTOE6＊0 | 09力 $\tau$ | 6GSE | $\begin{array}{r} 6 \\ 8 \triangleright G \end{array}$ | OG ${ }^{6}$ | 60t | 6L＇ZT8Z |  |
| G6S8T | $\varepsilon$ | $\begin{array}{r} 9 \\ +6008000 \div \\ \hline \end{array}$ | LLL09000＊ | $\angle \triangleright Z$ O6＇0 | カワて | ZOG | عโ6 | 8 8 | 60T | $\begin{array}{r} 8 \\ 08 \cdot 969 \\ \hline \end{array}$ |  |
| 0Lち8โ | T9G | ZLLL9E0＇0 | 8G6T7LOO＇0 | 606968＇0 | †98 | ZOtZ | $\begin{array}{r} 8 \\ \varepsilon 6 \varepsilon \end{array}$ | $\begin{array}{r} L \\ \downarrow 乙 9 \end{array}$ | TLZ | 6T＇โヵてZ |  |
| 0Lъ8โ | 9SG | 七98t980＇0 | E8S8ELOO＇0 | 906968＇0 | †98 | 00ヤZ | $\begin{array}{r} 9 \\ \varepsilon 6 \varepsilon \end{array}$ | ¢ | TLZ | $\begin{array}{r} 8 \\ \text { G•8とてZ } \end{array}$ |  |
| 8078 | ISS | 6TヵT9E0＇0 | LZETELO0＇0 | T98968 ${ }^{\circ}$ | G98 | G6EZ | 8T6E | $\begin{array}{r} 9 \\ \searrow 乙 9 \end{array}$ | 0LZ | $\begin{array}{r} \text { Z } \\ 9^{\prime} \text { ZとてZ } \end{array}$ |  |
| Lてヤ8T | L97 | EOt80E0＇0 | tS8tS900＊0 | 8S6S68＇0 | 992 | £દટ乙 | $\begin{array}{r} \varepsilon \\ \triangleright 9 \varepsilon \\ \hline \end{array}$ | $\begin{array}{r} 2 \\ 209 \\ \hline \end{array}$ | S6T | $\begin{array}{r} 9 \\ 6.7 \angle 6 \tau \end{array}$ |  |
| 9919 | 8 | T8Lt0T00＇0 | $\begin{array}{r} \dagger \\ \text { 亡Z9Z9000*0 } \end{array}$ | 60908L＇0 | 6 | 乙८โ | OヤZ | 986 | T0T | $\begin{array}{r} L \\ 98 \cdot \mathrm{G} \\ \hline \end{array}$ | $\varepsilon \wedge о{ }^{-}$dхә－$\varepsilon \tau$ ：дәшя |
| 2906T | EST | GL8LOTO＇0 | †ZヤLLZOO＊ | L08SZ6．0 | 6乙\＆ | 8SIT | てT0Z | ITZヵ | 0ヵT | $\begin{array}{r} Z \\ \varepsilon^{\prime} \angle \triangleright \tau \tau \\ \hline \end{array}$ | оұпе лоэ${ }^{-}$dxə－ع乙 ：дәшя |
| てT9LI | ZZL | L99SSt0＇0 | LEtOG900＊0 | Z99ZS8＊0 | TST | عャ8 | $\begin{array}{r} 9 \\ \sqcap \varsigma \tau \\ \hline \end{array}$ | $\begin{array}{r} 9 \\ 8 \triangleright \varepsilon \\ \hline \end{array}$ | 乙てT | $\begin{array}{r} 2 \\ 2 s .696 \\ \hline \end{array}$ |  |
| 98t6 | 6ST | ES9TIO＇0 | L80LtE00＇0 | LZ6St6＊ | عદG | LLDT | $\angle$ | $\varepsilon$ $99 t$ | 9\＆โ | $\begin{array}{r} 6 \\ \tau \cdot 0 \varepsilon \varepsilon \tau \\ \hline \end{array}$ |  |
| S876 | 6ST | عとt9lT0＇0 | LZT9ヵE00＊0 | 88St6＇0 | عદऽ | LLtT | $\angle$ | Z | 9عโ | $\frac{L}{L}$ |  |
| †8ャ6 | 6ST | I6E9IT0＇0 | ZOLStE00＊0 | 8T8St6．0 | عદG | LLDT | $\begin{aligned} & L \\ & \angle \varepsilon 乙 \end{aligned}$ | 2 | 98T | 9＊6ZとT |  |
| \＆ZS6T | SIT | Lてヤ80600＊0 | $\varepsilon$ ¢ 89 TE00＊0 | 866 $2 ⿰ ㇒ ⿻ 土 ㇒ 6^{\circ}$ | LES | عLヵT | $\begin{array}{r} Z \\ \angle \varepsilon 乙 \end{array}$ | $\varepsilon$ SSt | $\downarrow \subset \tau$ | $\begin{array}{r} 6 \\ 6 \cdot \varsigma \tau \varepsilon \tau \end{array}$ |  |
| †ZS6โ | 68 |  | 660E8Z00＊0 | ZOGLD6＇0 | ع67 | 切T | $\begin{array}{r} 8 \\ 0 \varepsilon 乙 \end{array}$ | $\begin{array}{r} \mathrm{S} \\ 6 \nabla t \end{array}$ | LZT | $\begin{array}{r} \varepsilon \\ \nabla \cdot \tau \succ Z \bar{\tau} \end{array}$ |  |
| †Eャ6T | 8て乙 | عL9GT0＇0 | 69T98E00＊0 | 6Z8tt6＇0 | †SL | G26T | 6TIE | O | ャ9 | $\begin{array}{r} t \\ \text { Z.9 } \\ \hline \end{array}$ |  |
| 七\＆ャ6โ | LZZ | 8tESST0＇0 | Z8St8E00＊0 | 698tt6 0 | GSL | GZ6T | 8TIE | 2 | t9 | $\begin{array}{r} \varepsilon \\ \angle \circ \neg \angle 9 \tau \end{array}$ | IT＾0Ј dxə－IZ ：：әш» |
| ESt6T | 902 | LEEとヤT0＇0 | عL6ELE00＇0 | 988St6 ${ }^{\circ}$ | LSL | LZ6T | ャ | S | 29T | $\frac{L}{6 \cdot \tau \angle 9 \tau}$ |  |
| T686โ | 692 | L889LI0＇0 | 66TEZヤ00＊0 | 688Et6．0 | 086 | 9でて |  | 9 979 | 七Z乙 | $\begin{array}{r} 9 \\ 2.8 \vdash 0 z \end{array}$ |  |


| L676T | StI | 8Tヵ80T0＇0 | 8โてT七E00＇0 | L9t976＇0 | 98G | 6Lt | $\begin{array}{r} 6 \\ \angle \varepsilon Z \end{array}$ | $\begin{array}{r} \varepsilon \\ 99 t \end{array}$ | S¢T | $\begin{array}{r} \dagger \\ \nabla \cdot \angle ट \varepsilon \tau \end{array}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| tS68T | t | 8S6LET00＇0 | IちGITIO0＇0 | ヤLL6T6＇0 | ¢\＆โ | $\varepsilon \angle t$ | $\varepsilon 88$ | $\varepsilon$ 02 | 90T | $\begin{array}{r} \text { Z } \\ 68 \cdot \mathrm{Tg} \end{array}$ |  |
| SEt6T | 8 8て | 9TE9ST0＇0 | 68EL8E00＇0 | 888t76 0 | †SL | SZ6T | 6TIE | 685 | 79 | $\begin{array}{r} 6 \\ +9297 \\ \hline \end{array}$ |  |
| SEャ6T | 8Z2 | Z8Z9ST0＇0 | St0L8E00＇0 | L8tt6＇0 | tSL | GZ6T | 6TIE | 6¢S | ャ9 | $\begin{array}{r} L \\ \varepsilon .9 \angle 9 \tau \end{array}$ |  |
| SEヤ6T | 8Z2 | 9Z9ST0＇0 | SZ898E00＇0 | SS8tヤ6＇0 | †SL | SZ6T | 6TIE | $\begin{array}{r} 6 \\ 6 \varepsilon \varsigma \end{array}$ | ャ9 | $\begin{array}{r} \dagger \\ \text { て. } 9 \angle 9 \tau \end{array}$ |  |
| ャ6ヤ6T | T9T | SIT9IT0＇0 | 80Z68E00＊0 | ع0Z8ャ6＇0 | 092 | 6Z6T | $\begin{array}{r} \nabla \\ \tau \tau \varepsilon \end{array}$ | 9 ${ }_{6}$ | 8ST | $\begin{array}{r} \mathrm{g} \\ \angle .7 \mathrm{I} 9 \end{array}$ |  |
| 0ZS6T | 00T | LE92800＇0 | 6ZとITE00＇0 | GZ8t6＇0 | $\tau 99$ | Z08T | 8G62 | ¢ ${ }_{\text {¢ }}$ | 98T | 68＇โ8ヵT |  |
| 8768T | G | ELStZTOO＇0 | $\begin{array}{r} \mathrm{T} \\ 6 \angle 9860000^{2} \\ \hline \end{array}$ | 9LOLZ6＇0 | †ST | t99 | $\begin{array}{r} L \\ \angle O L \\ \hline \end{array}$ | 88 | 80T | $\begin{array}{r} \dagger \\ 66 \cdot \varepsilon \varepsilon 9 \\ \hline \end{array}$ |  |
| T6E6T | 692 |  | ャعโをてャ00＊0 | 88Et6＇0 | 086 | 9Tち乙 | $\begin{array}{r} \varepsilon \\ 06 \varepsilon \\ \hline \end{array}$ | 9 979 | 七て乙 | $\begin{array}{r} L \\ \tau \\ \hline \end{array}$ |  |
| T6E6T | 892 | 909 ${ }^{\circ}$ T0＇0 | カ8LIZヤ00＊0 | 688をt6＇0 | 186 |  | $\begin{array}{r} \varepsilon \\ 06 \varepsilon \\ \hline \end{array}$ | 9 979 | 七て乙 |  |  |
| 60t6T | เ\＆乙 | 6TGZ9T0＇0 | LItOZtO0＇0 | ELStt6 ${ }^{\circ} 0$ | 086 | 6 TもZ |  | $\varepsilon$ 979 | LてZ | $\begin{array}{r} 9 \\ 0.0+0 z \\ \hline \end{array}$ |  |
| 0976T | †LL | 82882T0＇0 | 66ヶ68800＇0 | $\angle \triangleright T \angle \nabla 6^{\prime} 0$ | 086 | $60\rangle Z$ | $\begin{array}{r} 9 \\ 06 \varepsilon \\ \hline \end{array}$ | 0 ¢T9 | 902 | $\begin{array}{r} \angle \\ \angle .200 Z \\ \hline \end{array}$ | L лоэdxə－6I ：дәшх |
| †GZ6T | GSE | †9StEZ0＇0 | ZST90G00＇0 | 8L8LE6＇0 | †てZT | 980ع | $\begin{array}{r} \varepsilon \\ \tau 8 t \end{array}$ | $\varepsilon$ $\varepsilon 69$ | Tદє | $\begin{array}{r} 9 \\ \text { L'乙TSZ } \\ \hline \end{array}$ |  |
| †SZ6T | GSE | LヵStEZ0＇0 | L86GOG00＇0 | SL8LE6＇0 | †ZてT | 980ع | $\begin{array}{r} \varepsilon \\ \tau 8 t \end{array}$ | $\varepsilon$ $\varepsilon 69$ | Tદદ | $\begin{array}{r} L \\ \tau \cdot 2 \tau \subseteq Z \end{array}$ |  |
| ESZ6T | GSE | ع09tEZ0＇0 | LЪG90G00＇0 | G8LLE6＇0 | †ZてT | L80E | $\begin{array}{r} \mathrm{G} \\ \mathrm{I} \mathrm{t} \end{array}$ | 郆 | Tદ | 6て＇ZISZ |  |
| †GZ6T | £ระ | S69EEZO＇0 | 8Z\＆90G00＇0 | TS8LE6＇0 | GZZT | S80¢ | $\begin{array}{r} 9 \\ 18 t \\ \hline \end{array}$ | $\varepsilon$ $\varepsilon 69$ | $0 \varepsilon \varepsilon$ | $\begin{array}{r} \tau \\ 90 \text { TGZ } \\ \hline \end{array}$ | عโ＾оЈ ${ }^{-}$dxə－$\angle \tau:$ ：дәшя |
| 8SZ6T | $8 \downarrow \varepsilon$ | 8St0EZO＇0 | L68T0G00＇0 | †G08E6＇0 | GZZT | †60ع | 818t | $\varepsilon$ $\varepsilon 69$ | $0 \varepsilon \varepsilon$ | $\begin{array}{r} 9 \\ 08092 \\ \hline \end{array}$ |  |
| 91E6T | 782 | IEZヤ6T0＇0 | 860LLtO0＇0 | TSOTV6．0 | $6 ヵ$ CT | 80TE | ZZ8t | S +69 | 8ZE | $\begin{array}{r} \tau \\ 0.0092 \end{array}$ | 6 ＾оэ $^{\text {d }} \mathrm{dx}$－ $2 \tau:$ ：дәшя |
| てヤ88T | t | を的 ${ }^{9}$ | $\begin{array}{r} 8 \\ L \varepsilon 6890000^{\circ} \\ \hline \end{array}$ | عtELT6＇0 | ع8โ | T69 | $\begin{array}{r} 8 \\ 0 \varepsilon \tau \\ \hline \end{array}$ | $\varepsilon$ $\chi \downarrow \varepsilon$ | 0LT | 9T＇62L |  |


| โt8ヤโ | $\angle 9$ | t0LSEt00＇0 | 97zع8ャ000＇0 | 2t6ETLOO | 0 | $80 \tau$ | 892 | OヵIT | T0T | 89L＇z82 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 8Z¢st | Lع | S0¢88200＇0 | عとL66ち000＇0 | 6LLLTL＇O | 8 | $8 \downarrow \tau$ | 乙て¢ | ¢sZt | TOT | 889＇T0¢ |  |
| ع८\＆9 | $9<\tau$ | ャ698tio 0 | t0t69t00＇0 | †890 $2 L^{\circ}$ | $L$ | 882 | 989 | 9002 | SOT | \＆st＇zてS |  |
| 8992T | $\varepsilon 6$ | 96629900＇0 | TStLStoo 0 | 9206T8＇0 | ャ9 | 26t | $\llcorner\varepsilon 6$ | ¢z¢z | $90 \tau$ | てS0＇t99 |  |
| TS69T | SSI | L9206600＇0 | 698tıt00 0 | 880T620 | $0 \varepsilon$ | 907 | 乙て8 | L8ะて | LOT | \＆¢ะ＇9z9 |  |
| 8セELL | 8 TL | SZTELL00＇0 | TŞzetoo 0 | †LELO8＇0 | $8 \checkmark$ | ع¢t | 878 | 00ヶ2 | $90 \tau$ | عย9．8T9 |  |
| IIV | peddewun | 1011 | 1019 | әбеләлоэ | 06N | GLN | OSN | xew | u！w | บеәพ |  |



| 8888T | 689 | 709290＊0 | SEOEO＊ | 7S\＆Z68＊0 | 8 89 | 08ヵて | てZで | 乙Z99 | $\varepsilon 0 \varepsilon$ | 9でG6てZ | $\varepsilon z:$ ıәшя |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| †898 | OZS | ZTOESO＇0 | St8920＊0 | 90ZLO6＊ | 8 Z8 | ヤ0＜Z | てStワ | St99 | $6 \triangleright \varepsilon$ | LでもLEて | Іて：ıəШ४ |
| 06L8T | ャ89 | 88TIS00 | 七દโદて0＊0 | عLIZT6 0 | 006 | 乙とLZ | ヤ8tt | 7899 | $6 \varepsilon \varepsilon$ | てでヤL\＆て | 6T：১əшィ |
| T6L8T | ヤてL | 9EESO＇0 | 6†9020＊0 | 82LIT6＊ | 6 I6 | 96SZ | 6とદ† | †099 | $\varepsilon 0 \varepsilon$ | 6L｀T6Zて | LT：dəu＊ |
| 七ZS8T | S\＆II | ヤ0とTLO＇0 | LOL8T0＇0 | とャ6968＇0 | I89 | SZZZ | 6LLE | てヵT9 | S\＆Z | TS＇SEOZ | St：Jəu＾ |
| 8SSLT | 90ZZ | 989ZZT＇0 | L6S8T0＊0 | عLt8 ${ }^{\circ}$ | OヤZ | とャてT | LSEZ | Lt9t | †9โ | TL｀SOちT | عт：дәшу |
| IIV | paddemun | 10ג1ヨ 1ełol | 1018 | әбеләлоว | 06N | GLN | OSN | xew | u！${ }^{\text {N }}$ | ueวw | $\begin{array}{r} \text { s6u!⿰丬夕S } \\ \text { дәұәшe»ed } \end{array}$ |



| \＆LZ6T | SLI | てヵてZT0＊0 | LOE9TE00＊0 | ZSO†E6＊0 | GZS | G09T | $\begin{array}{r} 0 \\ 0 \angle 2 \end{array}$ | $\begin{array}{r} \varepsilon \\ \mathrm{TOS} \end{array}$ | 997 | $\begin{array}{r} Z \\ L \cdot \varepsilon s t \tau \end{array}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| てヤて6โ | ZTZ | Z66LヵT0＇0 | ZSLOLE00＇0 | 6LT9E6＊ | てヤL | Gt0Z | $\begin{array}{r} L \\ 6 \varepsilon \varepsilon \end{array}$ | $\begin{array}{r} 9 \\ \nabla \angle S \end{array}$ | 602 | $\begin{array}{r} \mathrm{G} \\ 0.08 \angle \mathrm{I} \end{array}$ |  |
| とヵt6T | 8LZ | カナT68โ0＇0 | 9ZOttナ00＊0 | 891E6＇0 | $\angle 68$ | $0 \angle \nabla 乙$ | $\begin{array}{r} 6 \\ \angle 0 t \\ \hline \end{array}$ | ¢ | 782 | $\begin{array}{r} \varepsilon \\ 9.060 Z \\ \hline \end{array}$ |  |
| ZZL8T | ZLt | ZT86620＇0 | 80Z7SSO0＇0 | عદОLT6＇0 | 七て8 | てヤとて | $\begin{array}{r} \varepsilon \\ Z 6 \varepsilon \end{array}$ | $\begin{array}{r} 8 \\ \angle \tau 9 \\ \hline \end{array}$ | S82 | $\begin{array}{r} \mathrm{T} \\ 9 . \mathrm{S} \angle O Z \end{array}$ |  |
| 98t6 | 6ST | 9TS9TIO＇0 | Lヵ69tE00＇0 | IT6St6．0 | દદร | $\angle L \bullet \tau$ | $\begin{array}{r} \angle \\ \angle \varepsilon \tau \\ \hline \end{array}$ | \＆ | 98T | T＇0\＆\＆ | LI лоэdxə－ع乙 ：дәшя |
| L8t6 | SSI | SSttilo＇o | LGZStE00＊0 | عZ6St6＊0 | દદร | $\angle L \bullet \tau$ | $\begin{array}{r} \angle \\ \angle \varepsilon z \\ \hline \end{array}$ | $\begin{array}{r} 2 \\ 99 t \end{array}$ | 98L | $\begin{array}{r} \mathrm{S} \\ 6.8 乙 \varepsilon \tau \end{array}$ | IT＾оэdxə－ع乙 ：дәшя |


| Z00¢ | IZ | L9088T00＇0 | 98tL6E000＇0 | 8LL6TL＇0 | 0 | I6 | $66 \tau$ | 998 | TOT | 960＇\＆と乙 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ZL89 | $\tau$ | 9T60tt00000 | 80g $627000^{\circ} 0$ | 8TES8で0 | 0 | 0 | 8 | I6Z | IL | LS8＇EIT |  |
| 乙セOSI | LI | てヤ6LヤT00＇0 | 60Zとદદ000＇0 | \＆ZOTZL＇0 | 0 | $\varepsilon 6$ | TOZ | 298 | T0I | SSt＇tez |  |
| ヤ8¢ャ $\tau$ | $9 \varepsilon$ | カナLT8て000 | LOLZE0000 | \＆8て00＜0 | 0 | LL | ع8โ | 608 | TOT | 196＇sてZ |  |
| 6988T | 02 | 99TSLT00＇0 | 996ヶ0L000＇0 | عยโ8t6 0 | SLI | 889 | ع80T | 8TLZ | عIT | ャT9＇t69 |  |
| SSIII | 0 | 68T9T800000 | S 26620000 | LL8TちG 0 | 0 | 0 | $\angle 6$ | $6 \angle\rangle$ | 66 | ع89＇ELT |  |
| 6906T | $\varepsilon \varepsilon$ | EOSG6Z00＇0 | E0LLITOO＇0 | 896926．0 | 002 | LOL | ZLII | SE8Z | 91T | $\downarrow$ T8＇ZGL | $0=$ 0＇z＝0 9L＝q 9＝u 6T：dəш＞ |
| 2096I | $0 \varepsilon$ | ع696LZ000 | 8ع6LZTO0＇0 | IELOG60 | ع8t | 662T | ちてTZ | らちてヤ | ยとโ | 9L＇G6IT |  |
| 6008T | てt | 七Z890800＇0 | L09ST8000＇0 | ๖6とLL80 | 887 | 676 | I69T | てعLE |  | TS＇E0IT |  |
| S088T | ヶ9 | 8TOSt00＇0 | 6 6¢LZT000 | عऽt806．0 | 81E | t02T | 8902 | てOZヤ | 8\＆T | 七で七\＆てT |  |
| T928T | tG | †T96800 0 | Z08996000＇0 | $\angle 888{ }^{\circ}$ | 817 | IT9 | Z80T | GLLZ | カIT | L9G＇LTL |  |
| 06L $\downarrow$ | $\varepsilon$ | TعE0EL000＇0 | 98LG9t000＇0 | SE8TZL＇0 | 0 | Z01 | Z乌己 | 980T | EOT | Sts＇E6Z |  |
| 967 $2 \tau$ | $\varepsilon \downarrow$ | LITE000 | 96L829000＇0 | TG92980 | โ9 | LIG | †86 | てヤ92 | カIT | 6L8．969 |  |
| 08T8T | £ | 9ZSSSZ00＇0 | 66¢ $02000^{\circ} 0$ | 9てZS¢8＊0 | SIT | L6G | G90T | 8GLZ | عII | 290＇L0L |  |
| GZLLI | 62 | LLt9LS00＇0 | L892T00＇0 | T92T980 | $\varepsilon L$ | †89 | $690 \pm$ | StLZ | 8IT | SEL＇09L |  |
| 9788T | $\angle 9$ | てヤ68Lヤ000 | 8SETET000 | 665ET6．0 | してE | L9IT | 986T | 机切 | $\downarrow$ ¢ | でてLIT |  |
| 8L98T | 切 | T0680800＇0 | G66T88000＇0 | 809806．0 | 20\＆ | 92IT | عと6 | \＆GOt | 乙とI | S8＊8EIT |  |
| 99E8T | STL | こ8TてT0＇0 | E09 ${ }^{\text {a }}$ T000 | GS9988＇0 | ZLZ | 892T | 68 โZ | 98をt | Z8T | OZカT |  |
| 88โ6T | とIL | LLEOLOO＇O | LLS6†T000 | Lヵてヤて6．0 | 98t | StSI | LLSZ | 98Lt | †GI | と6＇ZLヵT |  |
| GZSLI | ZL | L8ZLOS00＇0 | LEZL68000＇0 | T9LZS80 | ヶG | SLt | 206 | EOGZ | 60T | 69t＊LZ9 |  |
| 8L08T | 乙8 | ع8ELS00＇0 | Scsztoo 0 | てعELL8＇0 | ¢97 | $\varepsilon 98$ | $\varepsilon \dagger G \tau$ |  | 62T | โعS＇966 | $\tau=$ t＇$=009=q 9=u$ ¢T：dəш» |
| 999LI | S8 | 6966LS00＇0 | 80¢عT6000＇0 | てもEtS80 | 七9 | 685 | 600T | LL92 | てIT | てt9＇t0L |  |
| 976LI | 七9 | ITナtナt000 | $9609880000^{\circ}$ | でTてL8．0 | LST | ¢ 88 | 809I | 667 ¢ | LZT | $996 . \downarrow \angle 6$ |  |
| 8808T | S9 | 9T8tナt000 | Sع88000＇0 | LOちS ${ }^{\circ} 8^{\circ} 0$ | I6 | SS6 | LTLT | LT8E | LEI | 七6．と80T | $\tau=\partial \chi^{\prime} \tau=00 \varepsilon=q 9=u$ St：dəur |
| $\angle 8 \angle 8$ | 乙 | T962T800000 | عt6ZSS000＇0 | と6と8てt＇0 | 0 | 0 | SE | 90t | I6 | SSt＇ESI |  |
| 9708T | 291 | GLZヤOT0＇0 | LS9G9T00＇0 | てS9L98＊0 | LL | ST9 | LOLT | LI82 | LIT | $696{ }^{\circ} \downarrow$ LL | $\tau=$ 0 0＇乙＝0 09＝q 乙＝u st：dəu» |
| 6086โ | 00T | 6GLEt9000 | عโtt¢ST000 | LZ9Zて60 | 6切 | とち¢ | 8ててて | โ6\＆ャ | $68 \tau$ | T0＇G82T |  |
| عと88 | $\varepsilon$ | 8ZLZ06000＇0 | عSLZ6S000＇0 | LSSOEt＇0 | 0 | 0 | Lع | โとャ | I6 | 190．99I |  |
| てع6Ъ $\tau$ | 乙\＆ | 9IZ6GZ0000 | L98268000＇0 | 989TL＇0 | 0 | 98 | 68T | ST8 | TOT | IZL＇GZZ |  |
| LZESI | LI | 七6T9ST00＇0 | 869Zャ00000 | عยISEL＇0 | I | 66 | †0Z | 898 | 00T | TSع＇てE乙 |  |
| TL8G | $\tau$ | 8T60tt00000 | 60GL6Z000＇0 | GTES8て＇0 | 0 | 0 | 8 | 162 | TL | 9ャ8＇としL |  |
| $\varepsilon \dagger 9 \mathrm{~s}$ | 0 | ヤ999tt00000 | St69tを000＇0 | てSItLで0 | 0 | 0 | 8 | 9LZ | 89 | てぃ6゙LOL |  |
| 088ヶT | 乙\＆ | 89L8tZ00＇0 | عてt02\＆000＇0 | 6と\＆もTL＇0 | 0 | 七8 | L8I | ย18 | 00T | 97t＇szて |  |
| †LZSI | $\varepsilon t$ | 990ちE00＇0 | TLOT09000＇0 | z9LSELO | $\checkmark$ | $0 \downarrow \tau$ | 81E | LSZT | TOT | L80＇90E |  |
| عヶ9 | 0 | $\varepsilon 999 t \downarrow 000^{\circ} 0$ | $\varepsilon ャ 69 \downarrow$ ¢000＇0 | GSTちLで0 | 0 | 0 | 8 | $9 \angle Z$ | 89 | 6ヶ6 20 T |  |


| 0ع6†T | 乙て | ヤ8LZZ0000 | S $\angle 789 \angle 000^{\circ} 0$ | LZS80L＇0 | 0 | 96 | †Tع | ISET | ZOT | 七\＆t＇6をย | I＝ə 0＾$\tau=009=q$ 乙＝u ¢T：dəmy |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 88t8T | カII | 9てヤITLO0＇0 | ع8โ0LT000 | โt60680 | L®I | 2L9 | TLIL | T062 | SIT | ST6．GLL |  |
| LOZST | てヵ | G676TE00＇0 | ZLT68ャ000＇0 | S8SてEL＇0 | $\nabla$ | 8\＆โ | †Tع | て乌てT | LOT | Z0L＇t0\＆ |  |
| 69T6T | SOL | て9EャL900＇0 | โ0ع8ヤT00＇0 | 28t 2160 | 6乙を | てIII | てL8T | Lャ6\＆ | เ\＆โ | くガ0としT |  |
| カTG8T | S SL | 9ャ096600＇0 | 9068LT00＇0 | SS0S880 | 6と乙 | OIII | L $\dagger 6 \mathrm{~T}$ | と80t | OSI | てL＇9とてT |  |
| 9LIT | 0 |  | 69ZてZT0000 | L80ELSO 0 | 0 | 0 | 0 | 七L | LZ | عย0＇$\tau$ |  |
| カTL8T | 8S | S88SEャ000 | 9SE8ZT000 | ヤLヤLO6＇0 | $\varepsilon \angle Z$ | $6 \angle 6$ | โ697 | EZLE | 七てT | ¢8．900T |  |
| てع99โ | I $\varepsilon$ | عZS8ヤて0000 | ع8LャZS000＇0 | ヤSçscio | しT | ¢¢I | ¢ $¢ \varepsilon$ | 08てT | TOT | ع66．90ع |  |
| 0ヶL8T | $\llcorner\varepsilon$ | 6Z6TLZ000 | StSc980000 | ャع6てT60 | 8乙を | OZZT | LSOZ | 66Tヵ | $6 \downarrow$ T | て8＇と๕てT |  |
| T996T | 67 | 696ちtع0000 | LZ80LI00＇0 | †8096．0 | $\downarrow$ ¢ | 9とヶ $\tau$ | 08ع乙 | 6LSt | 62T | 6カ＊092T |  |
| LSI8T | $L Z$ | sعદz0Z000 | 9GZ9S000＇0 | 8TSS880 | $\varepsilon 6$ | S9S | 866 | てT92 | \＆II | LSZ＇T89 |  |
| GZ98T | LI | sعszてT000 | †L9009000＇0 | 98806．0 | 862 | 0عII | 6T6T | L00t | カカT | 8t＇z9tu |  |
| 6988L | 09 | 9Z9†てヤ000 | عとLOTOO＇0 | 七ع0ع680 | 901 | LZ9 | L90T | ع692 | LIT | LOt＇0EL | I＝ə 0＇Z＝0 9L＝q 9＝u 6T：dəшห |
| ع\＆L6I | I $\varepsilon$ | T0908Z0000 | 9267ET00＇0 | L8T9960 | Lャ9 | Lて9I | LL92 | て88t | \＆ヤT | S66TヤT |  |
| T608T | $8 \varepsilon$ | TL608Z000 | L0806 $0000^{\circ} 0$ | $68088{ }^{\circ}$ | カ七乙 | LZIT | S66I | OカIt | GSI | てS＇L92T |  |
| 88てIT | 0 | 七ع98ES00000 | ILZL8ち0000 | E8STSG0 | 0 | 0 | T0T | ZSG | 00T | S86．06T |  |
| てとち9 | SI | ZTZTLTOOO | LT60G $2000{ }^{\circ} 0$ | てعOZLL＇0 | 0 | 8てZ | LT9 | TG6T | SOT | とعと＇90G |  |
| L68LT | 00I | SS89ャ9000 | T8E力TIT00＇0 | 6989980 | L9I | $\varepsilon 96$ | 8G $\angle T$ | Lع8\＆ | LヵT | 七S＇ELIT |  |
| てZ6LT | S9 | ヤOZLナtロ0＇0 | 6†9LL8000＇0 | I8LZL80 | LST | 988 | 9T9T | Lع9E | $\downarrow \varepsilon \tau$ | 6で0801 |  |
| T908T | $\angle 6$ | L8ESE9000 | 90TLITO0＇0 | $687 \angle L 80$ | 8LT | $6 \angle 6$ | ても $2 \tau$ | 88LE | カナI | 6．1をIT |  |
| ع86LT | 99 | ITSヤEャ0000 | 七9899 $2000{ }^{\circ} 0$ | L6ES 280 | 9IZ | 660T | TG6T | ャ60t | LSI | で「らもてT |  |
| 698LT | $\varepsilon \varepsilon \tau$ | TSEL9800＇0 | $\angle \nabla \angle 9 力 T 00^{\circ} 0$ | L8LG980 | 82 | 029 | 6てIT | てT8Z | OZT | カナ＇カ6L |  |
| 七0t9 | SI | $\angle カ ナ 9 \angle T 000$ | 七S6ESL000＇0 | LTE8SL＇0 | 0 | 9＜L | 609 | 9GLT | 701 | $\downarrow$ ¢6＇t切 |  |
| 8ちG0T | $\varepsilon$ | 698EOT00＇0 | عTE8EL000＇0 | 8S9ETS＇0 | 0 | 0 | 乙8 | 七七 | L6 | $\downarrow$ ¢S＇6LT |  |
| GてTt | $\dagger$ | てS0ヶ98000＇0 | 89Z9LS000＇0 | $688989{ }^{\circ}$ | 0 | 99 | 8LI | S9L | TOT | てIt＊ 0 こ |  |
| ع098T | 92 | SELIZZ00＇0 | $6 \varepsilon \angle \nabla 8 \angle 000^{\circ} 0$ | S $29668{ }^{\circ}$ | ธ\＆乙 | $8 \angle 8$ | TSST | $\tau \sqcup \subseteq \varepsilon$ | カIT | $66 \varepsilon^{\prime} 068$ | $0=ə て ゙ \tau=00 \varepsilon=q 0 \tau=u$ ¢T：dəш» |
| 9T6ET | $L$ | 乙ES00T00＇0 | 8L6ちZち000＇0 | ZS6LL90 | 0 | 09 | L8T | 七七8 | TOT | ととt＇9bて |  |
| 乙とโ8โ | 02 | 866ヤ8ヤ000 | 8G9zع6000＇0 | 685T880 | OZT | 209 | 080T | ヤLLZ | てIT | Lて＇とTL |  |
| 9L98T | 工 | Z6S9TE000 | 6Z9ャع6000＇0 | TL09060 | STE | 90IT | 0T6T | カt0t | GZT | L＇980T |  |
| ヤ809 | $\varepsilon \tau$ | てS988T00＇0 | LLE688000＇0 | 6LOLTLO | 0 | 001 | ع6乙 | 092T | TOT | 909＇LTE |  |
| Z68LT | TSI | 89SLE6000 | SZOLITO0＇0 | 6S0ع980 | 七L | 66 S | 8801 | て6LZ | 9 9 | ع8L＇E9L |  |
| SャてT | 0 | 七StヶLT000＇0 | ع9T80t0000 | $689090{ }^{\circ}$ | 0 | 0 | 0 | 62 | 乙て | ¢ャعと＇દย |  |
| TOTST | LI | 8TG9ST000 | L9Tち0ヤ000＇0 | LLEカてL＇0 | 0 | S6 | $\varepsilon 02$ | 898 | TOT | 880＇s๕て |  |
| て\＆Z6โ | 06 | 99T9SS00＇0 | 66SOLTO0＇0 | โをもくて60 | $\angle 6 \varepsilon$ | 682T | 08ヶて | 七\＆\＆t | เยโ | 6L＇TGZT |  |
| SLIT | 0 | $9 \downarrow \angle \downarrow T 000^{\circ} 0$ | sてIZてT000＇0 | 678ZLS0＇0 | 0 | 0 | 0 | 七L | น乙 | 9600＇t $\varepsilon$ |  |


| 0T98โ | 乙® | LTE9LZ00＇0 | 67600T00＇0 | S6tto6．0 | TGZ | โE6 | 689T | 2998 | SIT | 9GS＇EZ6 | 0＝ə て＇$\tau=009=q 0 \tau=u$ ¢T：」əш» |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| カャてT | 0 | L6TもLT0000 | 906L0t000＇0 | LES9090＇0 | 0 | 0 | 0 | 82 | てZ | ¢T0ع＇દย |  |
| TL6LT | $\angle \nabla$ | L6E9sE00＇0 | てع9ャ60000 0 | とてZヤL80 | \＆รI | โع8 | 9TSI | LESE | てZI | 966 ＇عと6 |  |
| Lて68โ | 29 | L96tto000 | 69LてعT0000 | 826LI6＇0 | してカ | と切 | $96 \varepsilon 乙$ | 66St | てヵて | て6＇8ャ¢ | $0=$ て＇T＝0 89＝q 9＝u LT：১əшィ |
| 6ヤを8T | S9T | 2092860000 | GZャS66000＇0 | sعZ88．0 | 892 | LZZT | 6とIZ | 60\＆ャ | $\varepsilon \angle L$ | 9L＇LLEL | $\tau=$ て＇$\tau=0$ ¢ |
| 68921 | 66 | 86898900 0 | 8080عT000 | 乙S6S8．0 | $\angle 9$ | 99s | ¢ZOT | 8692 | $\varepsilon \tau \tau$ | 86＇stL | โ＝ə 0＇乙＝0 09＝q 9＝u ¢T：১əшィ |
| ع0L9］ | StI | 69t88600＇0 | $6898 \mathrm{STO} 0^{\circ} 0$ | LぃES8L＇0 | $9 \tau$ | $90 \varepsilon$ | SS9 | LZOZ | カ0T | T0ヶ＊ 8 TS |  |
| S8t8i | $6 \angle T$ | 9TOLOTO 0 | 98S6ST00＇0 | 921988＇0 | 86T | TL6 | 069T | عZLE | OヵT | 8で0ITI |  |
| TLE9T | 8 | 8てT二巾T000 | S0ヶt¢6000＇0 | SSOZLL＇0 | 0 | SLI | L9t | てع9โ | EOL | 890＇E0t | $0=$ 0＊$\tau=0$ 89＝q 乙＝u LT：১əш» |
| てZ99T | $\varepsilon \downarrow \tau$ | ZZ66S600＇0 | 万9998T0000 | 9ZSI8LO | $9 \tau$ | T0\＆ | 679 | \＆ZOZ | ヤOL | LZ8＇GIS |  |
| 8で0T | I | L0\＆T6L000＇0 | LT6099000＇0 | 9t780s 0 | 0 | 0 | 82 | LL $\dagger$ | $\angle 6$ | S6＇ZLT |  |
| ILZSI | LI | てZ8LヵT000 | 6ZSOSE000＇0 | 8TぃてEL＇0 | I | 86 | Z0Z | 998 | 00T | S80＇てとて |  |
| St6ヤT | IZ | S $297 \angle T 00^{\circ} 0$ | โャع6โع000＇0 | 8Z0 LTLO | 0 | 06 | 86I | 七¢8 | TOL | ป七8＇てとて |  |
| ても98T | 97 | 99StTE0000 | T08ャع8000＇0 | 60t8060 | Stて | $\varepsilon 66$ | 969 T | T0LE | S\＆I | てع＇OGOL |  |
| てSt6T | $8 \varepsilon$ | ع6Z962000 | ZOZSOT000 | L8SSt60 |  | 291T | LZ6T | OZOt | 92T | てO＇もLOL |  |
| 89LST | I | 9LャT9000＊0 | てャ08TS000＇0 | 8ع00LLO | 0 | SSI | てTE | LSIT | EOL | ع68＇とてE |  |
| 七\＆88T | 8T | 6658T00＇0 | عL08ャ8000＇0 | で916．0 | 181 | $9 \angle 9$ | SカIT | てI8Z | 9IT | S8600ヶL |  |
| عL88T | $\varepsilon 乙$ | I6IZ000 | て0TEL6000＇0 | 808LI6．0 | $\varepsilon \downarrow \varepsilon$ | ャ9TI | 8L6T | カ60t | 乙८โ | 七L＇EsIT |  |
| 8L68T | 乙て | てع99IZ0000 | 七92686000＇0 | sozz6．0 | Stワ | カ0ヤT | 8LEZ | 9LSt | 8\＆โ | と＇ヵてとし |  |
| 0026T | 09 | S88Stャ0000 | ع\＆と8ヵt000 | L98926 0 | カ0t | S8ZT | 6とtて | 8Sてt | OヶT | \＆9＇t92T |  |
| T97LT | 68 | てヤZOT900＇0 | S6EIIT000 | 882878．0 | 89 | $\tau \downarrow$ ¢ | ヤてOT | 6L92 | 8IT | 8SS＇67L |  |
| 89781 | 69 | S88700＇0 | Scsil00＇0 | Sع8S880 | てZし | 679 | てヤして | とャ8乙 | $67 \tau$ | E6E＇LLL |  |
| ع006T | 18 | STSTES00＇0 | 8L6ZZT000 | 七ع92T60 | 8で | ท6ヤT | T\＆GZ | 6S $\angle$ t | $\angle \downarrow \tau$ | T6＇SカヤT |  |
| LLSLI | $\varepsilon 9$ | 902TSt00＇0 | L90288000＇0 | 6ヵZ9S8＊0 | 29 | 乙८૬ | T00T | 6S92 | SIT | 86S＇LOL |  |
| 6T8LT | 8 t | 8ヵZદてを6000 | カ0ヵZ6S000＇0 | 8998980 | 切 | LS8 | 69ST | 98SE | 乙と亡 | て＇900T |  |
| E88LI | $6 \varepsilon$ | てヵ06LZ00＇0 | 七Z6090000 | I7LTL80 | S81 | 286 | 6LLT | £88ะ | StI | カS＇してTT |  |
| Z6SLT | LG | どャ60ヤ0000 | SStてt8000＇0 | L6t9980 | 69 | ع99 | LヤOT | 8TLZ | LII | 6Z6＇とヤL |  |
| TLS81 | 86 | S8829900＇0 | ヤ6StヶT000 | 七268680 | $6 \downarrow \tau$ | 9TL | 8てZT | 8962 | OZT | 29＊ 18 | $0=$ 0＇乙＝0 89＝q 乙＝u LT：̇əшィ |
| 8Lて8T | $6 \angle T$ | 9LLSOTO 0 |  | ع0LZ88＇0 | ZOZ | 8GOT | 098T | 乙06を | †SI | カでヤててT |  |
| ZSGOT | $t$ | ELOGL6000＇0 | T0TSES000＇0 | LEtワTS＇0 | 0 | 0 | 8 L | L8G | 66 | SZ9＊88T |  |
| 8GZ8T | ヤ8 | 98906S00＇0 | 802TET000 | 818988．0 | SZT | 619 | 960T | S6LZ | てII | L9ガヤてL |  |
| TStLT | 8LI | LSS06L00＇0 | 6StGST000 | 891780 | 6 t | Ett | 098 | 80ヵて | 901 | T＇\＆て9 |  |
| Z9ESI | てI | Z8902T000 | 97SOLE000＇0 | L099ELO | 乙 | TOL | SOZ | 898 | 00T | L8t＇とを乙 |  |
| TGOLI | 9ST | TLヵTOTO＇0 | عLOG9T00＇0 | カ七ES6L＇0 | $0 \varepsilon$ | 9 ¢ | 乙८8 | โ6๕Z | LOT | S6L＇089 |  |
| S068 | $\varepsilon$ | 6ヶL6GL000＇0 | LSt $288000^{\circ} 0$ | 9TStEt＊ | 0 | 0 | $0 \varepsilon$ | 92t | 七6 | TEs＇09T |  |


| 6988T | てZT | 七\＆TE9L00＇0 | عL8TヵT00＇0 | 6SS688＊0 | 20\＆ | 062T | \＆દટ乙 | てZカヤ | 92L | عL＇GてヤT |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| عGLLI | 81T | 8LI8EL00＇0 | โ9868600000 | عLIL98＇0 | 92 | ع09 | 60LT | て6LZ | $6 \tau \tau$ | てZ8＇18L |  |
| 989力 T | $\angle \varepsilon$ | Ls 2 ¢6Z000 | LTL968000＇0 | ع8zol＇o | 0 | 8 L | 七8T | てT8 | TOT | Lて＇9てZ |  |
| ヤL8ヵT | 69 | StSst0000 | LG686S000＇0 | L989TLO | 0 | 0LT | ILZ | 切し | TOT | てT6＇と8乙 |  |
| LLZ8T | てt | 6L0Zと00＇0 | ع62688000＇0 | ع08688＇0 | 62T | \＆ऽ9 | くヵIT | TL82 | 9IT | てZ8＇Z9L |  |
| くてIt $T$ | $\checkmark$ | エLてTも60000 | 8G978¢000＇0 | †06989 0 | 0 | $\angle 9$ | 18T | 882 | TOT | LL8＇ととて | 0＝ә 0＇T＝0 09＝q 9＝u ¢T：১əшィ |
| S\＆z8T | 87 | عZ068ع0000 | I6L98L000＇0 | StS8880 | S6 | 8LS | 2TOT | 8292 | カII | Stt＇069 |  |
| 9868T | L $\varepsilon$ | ZS6882000 | 68LTZ6000＇0 | てZОLZ6．0 | 6LI | 679 | $660 \pm$ | 9عLZ | $\varepsilon I \tau$ | S9．00L |  |
| \＆G¢8T | OZ | L8609T00＇0 | ZLOG6S000＇0 | S89t06．0 | ャยて | †96 | 9G9T | †G98 | $\varepsilon \varepsilon \tau$ | I9＇szot |  |
| L09IT | 0 | Z8L6Z9000＇0 | 乙عと08ャ000＇0 | ITL99 0 | 0 | 0 | てII | عऽऽ | 00T | عL6．06T |  |
| 7888T | 67 | L6L67E000 | 9tr60T000 | 8ZSLT60 | $08 \varepsilon$ | LてET | LOZZ | 9SEt | T9T | L＇นヤعโ | I＝ə て＇$=09$ 9L＝q 9＝u 6T：dəш》 |
| 698LT | 08 | 298E9S00＇0 | 80LZET000 | ZL9980 | 62 | S8S | カ901 | 00LZ | 617 | Tع＇8SL | L＝ə 0＇Z＝0 9L＝q 乙＝u 6T：dəш＞ |
| 8G98T | LS | てヤL9をヤ $00^{\circ} 0$ | 90ヵLET000 | ZSTE060 | 8ST | 689 | 08LT | ع982 | $6 I T$ | \＆てt＇98L |  |
| 七6て6T | $\angle 8$ | 866ELSOO＇0 | 960TST000 | SLITE60 | OSS | 6T9T | 00LZ | 8067 | \＆ऽI | 89＇TOST |  |
| \＆ヤL9T | 0I | 86ちE9T00＇0 | S9tS66000＇0 | 七0698L＇0 | I | LIZ | 299 | $\varepsilon 6 \angle T$ | EOL | 乙て＇とSt |  |
| 0898T | $\varepsilon t$ | S0LtをE 000 | ヤOヤZOT000 | 769806 0 | L92 | \＆ャ0T | عT8T | $688 \varepsilon$ | SZI | $6 \cdot \angle \triangleright 0 \tau$ |  |
| G66LI | 89 | โヵTESヤ000 | ャ88\＆Z6000＇0 | S909 ${ }^{\circ} 0$ | TOZ | \＆ャ0T | 688T | OtOt | $8 \downarrow \tau$ | てで08しT |  |
| T9L8 | 67 | SS06SE00＇0 | عZZ90T000 | 9StてT60 | $\angle \downarrow \varepsilon$ | てヤてT | عยI乙 |  | 8てT | T6． 28 IT |  |
| 9ITSI | 乙 | 9Z8L98000＇0 | 9tLL990000 | 9Z6ヵEL＇0 | 0 | 601 | عと乙 | عと6 | ZOT | て8て＇892 |  |
| 6LS8T | 七乙 | 60ع0Z00＊0 | 90tSEL000＇0 | ヤLSt060 | 992 | LTOT | 29LT | عદ8ะ | GZT | 90＇ャてOT |  |
| 6078 | 89 | TعE00S00＇0 | 6Z062T000 | 8068680 | 9\＆ | ヤ＜9 | 0＜IT | S682 | LII | てZT＊6LL |  |
| ITLST | I $\varepsilon$ | ヤ9769Z00＇0 | 886てع9000＇0 | S6E9SL＇0 | てI | 6SI | てヵ¢ | ヤ62T | TOT | 886．60ع |  |
| ヤOヤOL | I | T6T9290000 | L9098t000＇0 | ESZ80s＇0 | 0 | 0 | 七L | ヤOS | 66 | 8t9＊08T |  |
| LOESI | $9 \varepsilon$ | †T96LZ00＇0 | 8LTOG0000 | 98TLELO | S | StT | $6 乙$ ¢ | 8LZT | TOL | てャ9．0ヶを |  |
| SLIT | 0 | 9ヵLヵT000＇0 | sZIZZT000＇0 | 6ち8ZLSO0 | 0 | 0 | 0 | 七L | IZ | 9600＇tを |  |
| 8G68 | $t$ | ST0tT6000＇0 | 七ع89をカ000＇0 | LTOLEt＇0 | 0 | 0 | 乙¢ | LSt | ャ6 | LZ9＇E9T |  |
| カヵてT | 0 | L6TヤLT000 0 | 906L0T000＇0 | LES9090＇0 | 0 | 0 | 0 | 82 | てZ | ST0ع＇\＆と |  |
| 7928T | 0t | 8七¢ZOE0000 | 七七L6T6000＇0 | ILICT6．0 | $98 \varepsilon$ | 乙દยโ | I92Z | 9カャワ | LEL | 9でて8てT |  |
| 9968T | 82 | 690GOG00＇0 | 6880T00＇0 | 9919T6．0 | OSE | 6\＆ZT | Z802 | てもてヤ | OヵT | 9900ヶてT |  |
| 0\＆tSI | $\varepsilon \tau$ | 9LS82T0000 | s9tてtt000＇0 | L86EL＇0 | 乙 | ع0L | LOZ | 7L8 | 00I | 8てT「†をて |  |
| عTS8T | S $\varepsilon$ | ع86Z62000 | $\varepsilon ャ L \varepsilon 86000^{\circ} 0$ | عてT006．0 | SOZ | S08 | 0てヤT | TSE\＆ | $\varepsilon \tau \tau$ | てとt゙LE8 |  |
| 6206I | 乙6 | StT8T900＇0 | TLTOGT00＇0 | 乙ZOZ6：0 | ¢98 | ZLZT | 91tZ | 89で | $\varepsilon \downarrow \tau$ | 6．992T |  |
| Z68LI | 67 | 9826980000 | G6TZZ6000＇0 | 98S0L80 | てZし | ZZL | LてET | OZてE | $97 \tau$ | Sとt＇6を8 |  |
| ع608T | 09 | G9S8Zt0000 | 88ャ8と6000＇0 | ع186L8＇0 | TOT | 七ZS | SS6 | 8LGZ | 60T | 666．6Z9 |  |
| G6GSI | $6 \varepsilon$ | T9090800＇0 | 98LtI9000＇0 | LZ609L＇0 | 8 | OGI | 9 9¢ | 092T | TOT | โع0＇${ }^{\circ} 0 \varepsilon$ |  |


| エヤナくL | 6 S | 9L6てTち000 | 60TS89000＇0 | てZ68ヤ8＊0 | 乙S | S9t | 268 | L8ヤて | 601 | て88＇して9 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| عらヤ8i | 98 | LEI8G9000 | 989s86000＇0 | L929680 | $\varepsilon ャ \tau$ | 669 | 602T | てG6Z | $6 I T$ | عL＇ヤ08 |  |
| G98LT | 0t | 6LSL6Z00＇0 | StOs0L000＇0 | L0t6980 | てカて | 78L | ¢ $¢$ ¢T | ヤธ七\＆ | OZT | LLて＇868 |  |
| 26L8T | $\angle t$ | عLE9t¢00＇0 | 乙6乙とIT000 | STZET60 | て8乙 | SLOT | じ8T | 乙\＆8ะ | てぃ $\tau$ | しヤてとをIT |  |
| 8899 | 0 | LS0688000＇0 | 888028000＇0 | 2008SL＇0 | 0 | OZT | とて乙 | 七S8 | TOT | とて8＇6ヵて |  |
| T808T | SIT | $\angle \triangleright 980 \angle 00^{\circ} 0$ | ع6ムヵโIT000 | ¢ $七$ SOL8 0 | てて乙 | 08TT | 91ヶて | 8て\＆ャ | L9T | 90＊ โ8عโ |  |
| LL99I | 0 | 9ャLEL8000＇0 | 969628000＇0 | 七عZ6SL゙0 | 0 | عટT | Lع乙 | ¢ ¢6 | TOT | 919＊092 | $0=$ 0＇t＝0 9L＝q 9＝u 6โ：১əшィ |
| ع08ヵ $\tau$ | $\checkmark$ | عLIE6L000＇0 | 80098t000＇0 | L8LZてL゙0 | 0 | カ0T | 69Z | S901 | EOL | 6L 862 | L＝ə 0＇$\tau=0$ 89＝q 9＝u LT：১əш» |
| S6LLI | てt | LL980E00＇0 | ع8tL69000＇0 | 8t9980 | $81 \tau$ | 869 | Z6ZT | 8LTE | SII | L6て＇928 |  |
| T¢ع8โ | カ9T | T8ヵ $2 \mathrm{t} 600{ }^{\circ} 0$ | 9609LT000 | عZऽโ88＊0 | 68 T | $\angle \downarrow 6$ | ع99T | LOLE | 8\＆ | 060T |  |
| 8T98T | てZT | ESE86L00＇0 | 89ZSST000 | ZS9968．0 | てヤI | 689 | 06 IT | 6T62 | $97 \tau$ | โち8．98L |  |
| てT88T | LS | SES0とヤ00＇0 | 9862T00＊0 | 982IT6 0 | 8\＆ะ | S $\angle 1 T$ | Z002 | 60tt | 8ZT | しT゙6てIT | $0=ə$ て＇$\tau=009=q 9=u \mathrm{st}$ ：১əш» |
| 9で8 | 82 | 998TEZ0000 | ع8ZS9L000＇0 | LZLS680 | 86T | ع8L | 68\＆โ | $60 \varepsilon \varepsilon$ | ยાL | \＆GL＇əて8 |  |
| I898T | 工t |  | 699IZ6000＇0 |  | 192 | TS6 | 999T | 089\＆ | てZI | 89＇¢86 |  |
| 988¢ | LE | 978S6Z0000 | 9عtャ09000＇0 | S960tL＇0 | G | 67 T | ૬\＆ะ | T6ZT | IOT | L®G＇عाع |  |
| 66LST | Z | 9L089000＇0 | てZとttS000＇0 | でLILLO | 0 | 6ST | 七て¢ | 00ZT | EOL |  |  |
| L 798 L | LZ | 9GOtZZOO＇0 | 60L89 $0000^{\circ} 0$ | 978L06．0 | 0乙を | 0975 | 266T | てSIt | LZI | 8L＇6てII |  |
| S068 | $\varepsilon$ | 6ヶL6S $2000^{\circ} 0$ | 8StL8E000＇0 | عTSカEtio | 0 | 0 | $0 \varepsilon$ | 92t | ャ6 | LZS．09T |  |
| โとヤIT | 乙 | 92890T00＇0 | Lg $1880000^{\circ}$ | عャ8¢Sc＇0 | 0 | 0 | SOT | 929 | 66 | 80G＇E6T |  |
| \＆ऽZ8T | 82 | 6669ZZ0000 | 6ZSttL000＇0 | 862688＊0 | TOL | $\varepsilon 09$ | TGOT | TL92 | $97 \tau$ | ZOZ＇LTL |  |
| 99TST | 乙S | 9と9E0ャ000 | 9L6T6S000＇0 | GLLOELO | 乙 | 6 LI | 9LZ | カナIT | IOT | 99L＇t8Z |  |
| ZSGLT | $\varepsilon 6$ | ع688900＇0 | 七9 $\dagger$ ¢ T000 | 8ヵて七七8＊0 | 19 | 08t | 026 | LOGZ | 901 | 七ST＇ES9 |  |
| 606S | 乙 | S96ELS000＇0 | てぃて6โE000＇0 |  | 0 | 0 | 6 | $80 \varepsilon$ | IL | 602＇91T |  |
| 00881 | 66 | 60909900＇0 | ヤくヵて七T000 | GZ0988＊0 | 七て乙 | 880T | St8T | L98E | TSI | 98．96IT |  |
| DOTST | IS | 8L6S8E00＇0 | LZ\＆̧ $2 ⿰ 0000^{\circ} 0$ | 998LZL＇0 | 乙 | 8LT | $\varepsilon L Z$ | OヵIT | TOL | 899．082 | $0=$ 0＇z＝0 9z＝q 9＝u عt：dəшห |
| $\angle 8 \angle 8$ | 乙 | T962T8000 0 | عT6ZSS000＇0 | て6と8てtio | 0 | 0 | ¢ $\varepsilon$ | 90t | I6 | $6 ⿰ 巾$ 6＇EsI |  |
| 99TLL | カ¢โ | ヤLヤL8000 | 6S8StT000 | でLL6LO | $6 \varepsilon$ | $\varepsilon \varsigma t$ | 268 | โ8ヤて | 601 | 86t＇ヶ99 |  |
| TLI6T | ع8 | S0tSTS00＇0 | S6680T00＇0 | と攷6 | T9力 | L6t $\tau$ | 0TGZ | 802t | $6 \downarrow \tau$ | ャ6＇Lてヤて |  |
| ヤT6\＆โ | $L$ | 6St6ャ6000＇0 | L89LIち000＇0 | S9ELL90 | 0 | 09 | 七81 | 078 | IOT | 9ZS＇でて |  |
| OもEII | $\dagger$ | G6LZL6000＇0 | z09929000＇0 | 8TGZSc＊0 | 0 | 0 | EOL | 989 | 00T | てSL＇t0Z |  |
| ヤOヤOL | I | ع6T9Z9000＇0 | z909Et000＇0 | ZSZ8090 | 0 | 0 | 七L | 七09 | 66 | L09．08T |  |
| ع9ャ6 | $\varepsilon \tau$ | ZL88ST00＇0 | STL668000＇0 | Lャ99ヶ60 | 68t | 6乙\＆โ | 00Z2 | T98t | 8てT | 60＇18IT |  |
| 七LI8T | 62 | ヤ8ELSG0000 | E9TLZT000 | L60T880 | LOZ | STOL | 962I | L068 | O†T | St゙8てIT | $\tau=$ て＇$=009=q 9=u$ ¢T：dəu＊ |
| 9918L | 8ST | てع62T6000 | G97660000 | 6TL8L80 | \＆6I | 8Z0T | 6T8T | 9L8E | OSI | ャ8＇88LT | $\tau=$ t＇$\tau=0$ t |
| 6008T | $8 t$ | てع6โちع00＇0 | 90t9zLO00＇0 | 7869 280 | 86 | $\varepsilon$ LS | カャ6 | T992 | $80 \tau$ | โと9＇ャて9 |  |


| Parameter <br> Settings | Mean | Min | Max | N50 | $\mathbf{N 7 5}$ | $\mathbf{N 9 0}$ | Coverage | Error | Total Error | Unmapped |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Kmer： $13-\mathrm{M} 0$ | 384.79 | 104 | 1540 | 471 | 273 | 82 | 0.87947 | 0.000472357 | 0.0011617 | 12 |
| Kmer： $13-\mathrm{M} 1$ | 447.511 | 106 | 1796 | 586 | 342 | 112 | 0.893773 | 0.000646363 | 0.00112631 | 8 |
| Kmer： $13-\mathrm{M} 2$ | 498.883 | 107 | 2077 | 700 | 404 | 135 | 0.904168 | 0.000782716 | 0.00189791 | 20 |
| Kmer： $13-\mathrm{M} 3$ | 500.571 | 107 | 2090 | 703 | 406 | 136 | 0.904755 | 0.000772936 | 0.00189871 | 21 |
| Kmer： $15-\mathrm{M} 0$ | 487.034 | 108 | 1950 | 665 | 392 | 134 | 0.910935 | 0.000535884 | 0.00102203 | 8 |
| Kmer： $15-\mathrm{M} 1$ | 688.446 | 116 | 2718 | 1051 | 622 | 223 | 0.926615 | 0.000652513 | 0.000949038 | 5 |
| Kmer： $15-\mathrm{M} 2$ | 921.761 | 123 | 3635 | 1598 | 940 | 338 | 0.937523 | 0.000702016 | 0.00102623 | 6 |
| Kmer： $15-\mathrm{M} 3$ | 931.618 | 123 | 3681 | 1624 | 957 | 344 | 0.938597 | 0.000712872 | 0.00103654 | 6 |
| Kmer： $17-\mathrm{M} 0$ | 507.594 | 108 | 2012 | 712 | 425 | 150 | 0.92204 | 0.000629373 | 0.000922506 | 5 |
| Kmer： $17-\mathrm{M} 1$ | 788.243 | 119 | 3007 | 1243 | 750 | 282 | 0.938112 | 0.000705106 | 0.000839215 | 2 |
| Kmer： $17-\mathrm{M} 2$ | 1075.43 | 130 | 4096 | 1929 | 1157 | 441 | 0.94794 | 0.000732059 | 0.000950511 | 4 |
| Kmer： $17-\mathrm{M} 3$ | 1093.6 | 130 | 4181 | 1991 | 1183 | 454 | 0.949321 | 0.000738146 | 0.000951649 | 4 |
| Kmer： $19-\mathrm{M} 0$ | 501.361 | 108 | 1987 | 706 | 421 | 153 | 0.927751 | 0.000703507 | 0.00100412 | 5 |
| Kmer： $19-\mathrm{M} 1$ | 801.098 | 120 | 3041 | 1276 | 782 | 292 | 0.944447 | 0.000778647 | 0.000954282 | 3 |
| Kmer： $19-\mathrm{M} 2$ | 1043.5 | 130 | 3961 | 1851 | 1111 | 424 | 0.952787 | 0.000787422 | 0.000975081 | 3 |
| Kmer： $19-\mathrm{M} 3$ | 1059.86 | 131 | 4026 | 1897 | 1136 | 437 | 0.954249 | 0.000805661 | 0.000980857 | 3 |
| Kmer： $21-\mathrm{M} 0$ | 486.973 | 108 | 1921 | 683 | 410 | 154 | 0.930678 | 0.000789377 | 0.00110459 | 6 |
| Kmer： $21-\mathrm{M} 1$ | 788.043 | 119 | 3017 | 1261 | 780 | 289 | 0.948229 | 0.000869027 | 0.0010005 | 2 |
| Kmer： $21-\mathrm{M} 2$ | 954.212 | 125 | 3645 | 1644 | 1003 | 379 | 0.954463 | 0.000876887 | 0.00101017 | 2 |



| 乙てtst | $\varepsilon$ | 8T06000＇0 | 乙88z89000＇0 | LT6GELO | 0 | ItI | Lヵて | TL6 | $20 \tau$ | عTs＇t ${ }^{\text {cz }}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| TL99 | $\tau$ | 86t巾\＆S000＇0 | L6zs98000＇0 | T9tGLて＇0 | 0 | 0 | 8 | 682 | 89 | でぐ60T |  |
| ISZLI | LET | SL9ET600＇0 | Tع897000 | T9208＊ | 0 | t9t | 806 | TOS2 | $60 \tau$ | LZO＇ZL9 |  |
| 6\＆18โ | $\angle 6$ | ¢zozع900＊0 | L080ztoo | ع $28088^{\circ} 0$ | $8 \varepsilon \tau$ | t9tt | 9502 | เとで | ¢9T | ャく＇tıET |  |
| 916LT | $\varepsilon L$ | It8S9t00＇0 | 8ZS8EL000＇0 | 992ZL80 | L9 | $0 \bullet 6$ | 889¢ | โ $\varepsilon$ Lย | นヵโ | t9860T |  |
| $9806 \tau$ | 26 | ¢8STLS00＇0 | TSc90t00＇0 | 2692T60 | ¢Tع | ャ80 | Lヤ8T | $9 \varepsilon 6 \varepsilon$ | เદ | 66．01TI |  |
| 9986โ | てT | 8SGLDT00＇0 | عT0¢88000＇0 | G96Tt60 | 968 | 92tt | ع＜8t | †968 | GZT | 89\％6tot |  |
| †098 | $06 \tau$ | Sogttioo | LLTS9T00＇0 | 8L66880 | \＆¢乙 | 6 TIT | 886โ | 8\＆てt | 9ST | 99＇TLZT |  |
| †ててTし | 0 | T6L6T8000＇0 | z9Zヤ8L000＇0 | عって9tGo | 0 | 0 | 66 | tos | 66 | 6Lع＇6LT |  |
| 8でot | I | S0\＆t6 0000 | St6099000＇0 | STt809 0 | 0 | 0 | 82 | LLD | 26 | ¢\＆6＇ZLT |  |
| 88Z9T | ZLI | Ltttuo | 886カカT00＇0 | 69999 ${ }^{\circ}$ | $L$ | 282 | $0 \varepsilon 9$ | t002 | SOT | 乙てع＇6TS |  |


| 00L6LIZ | TSZ66 | $\begin{array}{r} \tau \\ \varepsilon 0 \varepsilon \Delta \nabla 00 \end{array}$ | $\begin{array}{r} 9 \\ \text { IZLLTOO:0 } \end{array}$ | 8LS9980 | 97t | SI8T | 260E | $68 T \angle T$ | 009 |  | T S－LZ 7－โZ：дəш丬 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ITZ6LIZ | ท86SII | $\begin{array}{r} 9 \\ \text { EOZTSOO } \end{array}$ | 6LTOO＇0 | 9S09S80 | でヤ | 808T | દ80ع | 88TLT | 009 | $\begin{array}{r} Z \\ \nabla \cdot Z \varepsilon \varsigma Z \end{array}$ | І S－SZ 7－โZ：১əшィ |
| 96E6LIZ | 0ヤ8TST | $\begin{array}{r} 9 \\ 08 \mathrm{~S} 90 \\ \hline \end{array}$ | $\begin{array}{r} \mathrm{G} \\ \downarrow \varepsilon \varepsilon 8 \tau 00 \cdot 0 \end{array}$ | LţGS8 0 | $86 \varepsilon$ | $608 \tau$ | ZLOE | L8ZLI | 009 | †ZらZ |  |
| 8عIE8โ乙 | 8606TE | 6T0ET＂0 | $\begin{array}{r} \tau \\ 8 \varsigma \subseteq 6 T 00: 0 \end{array}$ | GL8tG8 0 | Z6E | Z8LI | 990E | 99TLL | 009 | S＇L6†て |  |
| 0I6G8I2 | LOGSEE | ZE9SET＂0 | $\begin{array}{r} L \\ \angle 266 T 00 \circ 0 \end{array}$ | Lt6tG8 0 | Z6£ | 08LT | OG0E | 99TLL | 009 | L8tて | T S－6T 7－โZ：১əшィ |
| ع80ع8โ乙 | LT66TE | SESOET＇0 | $\begin{array}{r} \mathrm{G} \\ 0 \varepsilon 96 \tau 00: 0 \\ \hline \end{array}$ | LL8tG8 0 | 26£ | 08LT | $970 \varepsilon$ | 99TLL | 009 | $\begin{array}{r} L \\ \tau \cdot \tau 6 \dagger Z \\ \hline \end{array}$ | T S－LT 7－โZ：дəшィ |
| 89L08LZ | LIIIIT | とโもT6ヶ0＇0 | $\begin{array}{r} \mathrm{G} \\ \mathrm{~S} 16 \angle 100 \cdot 0 \\ \hline \end{array}$ | t0E9S8 0 | 20t | 2T8T | 880ع | TEt 2 T | 009 | $\begin{array}{r} 8 \\ \text { c' } \downarrow \varepsilon \varsigma \\ \hline \end{array}$ | T S－LZ 7－6T：дәшя |
| ع6T08LZ | Z0T6ET | $\begin{array}{r} \angle \\ \angle \angle \nabla 0900^{\circ} \\ \hline \end{array}$ | $\begin{array}{r} \varepsilon \\ \tau \angle \mathrm{t} 2 \mathrm{O} \\ \hline \end{array}$ | 8TSSS80 | $66 \varepsilon$ | †08T | †LOE | 9769I | 009 | $\begin{array}{r} \mathrm{L} \\ \text { I'zzs } \\ \hline \end{array}$ | T S－SZ 7－6T：дəшィ |
| ZSt6LIZ | ع0ヤ68โ | $\begin{array}{r} \varepsilon \\ \text { sعZ080.0 } \end{array}$ | てち888T00＇0 | I8ちG8 0 | $96 \varepsilon$ | T08T | 890ع | 9769T | 00G | $\begin{array}{r} Z \\ 6 . \partial \tau G Z \end{array}$ |  |
| 88TL6TZ | てヤ6SZ9 | દEEşZ＇0 | 6L886T00＇0 | 680tG8 0 | T6ะ | ELLI | $670 \varepsilon$ | S069T | 009 | $\begin{array}{r} Z \\ \nabla 99 ヶ Z \\ \hline \end{array}$ | T S－TZ 7－6T：дәшя |
| 6St6ャZZ | LヵLSt9T | て98とても＊ 0 | GZEEZ00＇0 | LTGZS8 0 | $\varepsilon 8 \varepsilon$ | 92LT | 9862 | TOTLI | 009 | $\begin{array}{r} 8 \\ 0 \\ 0 \\ \hline \end{array}$ | T S－6T 7－6T：גәшя |
| 8606ヤてZ | 6ESOTLL | E6ZとEt＇0 | S92EZ00＇0 | 89tZS8 0 | Z8ะ | 9TLT | †L62 | TOTLI | 009 | $\begin{array}{r} \mathrm{G} \\ \angle 0 \varepsilon \varepsilon 乙 \\ \hline \end{array}$ | T S－LT 7－6T：дәшィ |
| IIV | pəddemun | $\begin{aligned} & 10 \text { 10ヨ } \\ & \text { ןełol } \end{aligned}$ | 10113 | әбеләлоว | 06N | GLN | OSN | xew | u！ | ueәN | $\begin{array}{r} \text { s6u!ఘəS } \\ \text { ләұәшe»ed } \end{array}$ |



| LTL6T |  | LTSSIT00＊0 | LTE686000＇0 | T9EtS6＊ | ૬Zદ | 028 | LてカT | しЪてを | IZT | L86 ¢ ${ }^{\text {¢ }}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ち0L6T | 乙 | L6090T00＇0 | LL86T6000＇0 | ヤ七8\＆S6．0 | 乙て\＆ | S98 | 0てカI | てとてを | IZT | ع96．878 |  |
| Lع96T | $\varepsilon$ | T0890T00＇0 | 80TS06000＇0 | SعL6ヤ6．0 | ELZ | عદL | S6IT | 6982 | 8LT | ち9809L |  |
| 6Zと6T | L | 9L9ZZT00＇0 | 七0TSt8000＇0 | 996TE6＊0 | \＆SI | 968 | 299 | St8I | LOT | カZS＇EL | $0 \mathrm{~W}-\varepsilon 乙:$ ：$\partial \mathrm{W}$ |
| †TL6T | 乙 | LSSZOTOO＇0 | Z8ZZ68000＇0 | 8ESSS6＊0 | S8E | LTOT | ャ99 | $699 \varepsilon$ | GZT | ヤ0L＇と96 | $\varepsilon W-\tau Z: \pm \partial \omega\rangle$ |


| OtOGZLE | †089 | $\begin{array}{r} \nabla \\ \tau \varepsilon \varsigma \varepsilon 600 \end{array}$ |  | 8T98LL＇0 | 0 | ZSL | 80GI | ZTEL | 00G | عโદโ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 6とヵZ69E | LもELT | $\begin{array}{r} 6 \\ \dagger Z 896000 \end{array}$ | $\begin{array}{r} \varepsilon \\ \mathrm{G} 6 Z 6 \vdash 00^{\circ} 0 \end{array}$ | Z9ELLL＇0 | 0 | カヤL | TOST | てTEL | OOG | ZTET | ャ S－IT 7－عโ：১əшя |
| IIV | paddewun | 10גコ | 1011ヨ | әбеләлоว | 06N | GLN | OGN | xew | u！w | ueәN |  |



| ITEセE6T | 9TSt69ヵT | 66St88＇0 | عとโぃZT00＊0 | ET086S＇0 | 0 | 0 | $\angle 99$ | ZS99 | 009 | $\begin{array}{r} \varepsilon \\ 8 \cdot \downarrow 90 \tau \end{array}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| LLE9Z0E | StTOLLSZ | Z0T968＇0 | S698SE00＇0 | †GS608＊ | 0 | TLOT | 8Z8T | てヵてII | 009 | $\begin{array}{r} Z \\ 6.6 \Omega \varepsilon \tau \end{array}$ | L＾о才 dxə－ع乙：дәшя |
| 9008E0E | 996ヵZ8SZ | LL6G68＇0 | ¢عE08E00＇0 | ZGZET8＊0 | 0 | ع60t | †¢8โ | 8ヵカIT | 009 | $\begin{array}{r} \mathrm{G} \\ \text { 乙. } 9 \varepsilon \text { I } \end{array}$ |  |
| 888โ96T | โ69288ヵT | S6E8880 | カIIITOO＇0 | E96L09＇0 | 0 | $\varepsilon t$ | 969 | 19＜9 | 00G | $\begin{array}{r} L \\ \tau \cdot 650 \tau \end{array}$ |  |
| 98TE80E | †T60SS92 | s $2 T \angle 68^{\circ} 0$ | 908S9E00＊0 | で9028＊0 | ع8T | SLZT | ち8โて | StロてT | 009 | $\begin{array}{r} \varepsilon \\ 8 \cdot \varsigma \subseteq \dagger \tau \end{array}$ | L＾о才dxə－IZ：дəшя |
| ESLL60E | LL89T992 | 866968＊0 | 8ャE6E00＇0 | Z8L9Z8＊0 | L8T | 90\＆โ | IZてZ | Z0GZT | 009 | $\begin{array}{r} 8 \\ 0 . t 9 力 t \end{array}$ |  |
| 80LSOtT | 9GSGZEIT | عદ8688＇0 | $\begin{array}{r} \text { Z } \\ \text { GS006000 } \end{array}$ | LE9ZEt 0 | 0 | 0 | 9＜T | 900t | OOS | $\begin{array}{r} L \\ \tau 6.898 \end{array}$ |  |
| 9†E60TE | LZT0T892 | 9L680 | ST68ヵS00＇0 | 660908 0 | SET | 8TZT | OLTZ | IT6IT | Z09 | $\begin{array}{r} \tau \\ 6 \cdot \angle \nabla \nabla \tau \end{array}$ |  |
| S6TGZTE | ことてOT0Lて | 2Z8L68＊ | †9899S00＊0 | 6L0力T8＇0 | 9力T | 08ZT | LLIZ | 68LII | TOS | ع9力 $\tau$ |  |
| عI9GZ | 8T9899 | †8ZZS6＊0 | L8TZT00＇0 | $\begin{array}{r} \tau \\ \varepsilon \angle T S 800 \circ \\ \hline \end{array}$ | 0 | 0 | 0 | †L8 | TOS | GZ＇189 |  |
| 68SE8LT | LTG9STLT | TSS906＊ | て997t900＊0 | ESELt＇0 | 0 | 0 | L6Z | ャてカヤ | 009 | $\begin{array}{r} \varepsilon \\ 89.8 \tau 6 \end{array}$ |  |
| ESETS8T | 七ZLEE9LT | 8SSS06．0 | 七6LLS900＇0 | 6T09670 | 0 | 0 | L9E | ャEOS | 009 | $\begin{array}{r} \varepsilon \\ \varepsilon 8^{\prime} 乙 \varepsilon 6 \end{array}$ |  |
| IIV | peddewun |  | 10лコ | әбеләлоэ | 06N | SLN | OSN | xew | U！W | ueәN | sбu！\＃əs ләґәшелед |



| ¢ZSETちE | 9ャ08 | T809900＊0 | と99Tャ00＊0 | T8E9ZL＇0 | 0 | I8S | IZZT | S8Z9 | 009 | SSZT |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 928L9ヵ¢ | \＆G8ZT | $\begin{array}{r} 6 \\ \varepsilon 988 \angle 000 \end{array}$ | $\begin{array}{r} L \\ \text { Z60Zャ00.0 } \end{array}$ | 89Z\＆とL＇0 | 0 | S09 | 08ZT | S8Z9 | 00G | L8ZT | s S－¢－7－¢T：дәшя |
| ャL89くゅE | ST69 | $\begin{array}{r} 8 \\ \text { S80 } \end{array}$ | $\begin{array}{r} L \\ 8 \tau \varepsilon \tau \circ 000 \end{array}$ | $6 \triangleright 8 \downarrow$ L ${ }^{\circ}$ | 0 | てT9 | ZLZT | S8Z9 | 00G | ヤ8ZT |  |
| 8عદS8t¢ | 6808 | $\begin{array}{r} 2 \\ \text { I6Z } 9000 \end{array}$ | $\begin{array}{r} \tau \\ \downarrow \varepsilon 乙 乙 \succ 000 \end{array}$ | tZZLEL＇0 | 0 | 2T9 | ZLZT | S8Z9 | 009 | LLZT |  |
| 869LTSE | LZOカT | $\begin{array}{r} \stackrel{\rightharpoonup}{7} \\ \hline 78 \angle 1800 \circ \\ \hline \end{array}$ | S\＆Zでヤ000 | TLヵTナL＇0 | 0 | L29 | 09ET | 970 | 009 | عโદโ | G S－TZ 7－عT：дәш才 |
| L8TGZSE | E6S8 | $\begin{array}{r} \mathrm{G} \\ 29 \mathrm{f} 900 \cdot 0 \end{array}$ | 9ちで七00＇0 | ع0\＆ZtL＇0 | 0 | 889 | LSET | 970 | 00G | LIET | ャ S－TZ 7－عโ：дәшィ |
| 乙S06ESE | Z629 | $\begin{array}{r} \varepsilon \\ \angle T \angle T 900^{\circ} \end{array}$ | $\begin{array}{r} z \\ +\nabla 92+00 \circ 0 \end{array}$ | 988StL＇0 | 0 | カャ9 | $97 ¢ \tau$ | 970 | 00G | E0\＆T |  |
| †0¢69SE | OZELT | $\begin{array}{r} \angle \\ \angle L I T 6000^{\circ} \end{array}$ | $\begin{array}{r} 2 \\ 960 \varepsilon t 00 \cdot 0 \end{array}$ | Z8Z0SL＇0 | 0 | tS9 | TOtT | 970 | 009 | 9Z\＆โ | G S－6T 7－عT：дәшя |
| 乙6E06SE | T09ヵT | $\begin{array}{r} 6 \\ \angle Z 0 \dagger 800 \cdot 0 \\ \hline \end{array}$ | $\begin{array}{r} \angle \\ z 0<\varepsilon+00 \cdot 0 \end{array}$ | †EtSL＇0 | 0 | $0 \angle 9$ | T6ET | 970 | 009 | 9TET | ع S－6T 7－عT：дәшя |
| LL6979E | ZSS6I | 68t9600＇0 | ZOTEャ00＇0 | L66GL＇0 | 0 | $\angle 89$ | ヤくヤT | ع976 | 009 | $9 \downarrow$ ¢ | S S－LT 7－عโ：גəШ丬 |
| 8T0979 | 0679 | $\begin{array}{r} 9 \\ 6898800 \cdot 0 \\ \hline \end{array}$ | $\begin{array}{r} 8 \\ \text { z9LEt00'0 } \\ \hline \end{array}$ | ZLEt9L＇0 | 0 | 669 | カSカT | ع976 | 009 | عยદโ | $\varepsilon$ S－LT 7－عT：дәшя |
| SEZ889¢ | Z0LST | 8TZL800＇0 | $\begin{array}{r} \tau \\ 9 \tau 0 \mathrm{St} 00 \cdot 0 \end{array}$ | EG69L＇0 | 0 | 92L | 9ZSI | 9926 | 00G | LSET | S S－ST 7－عT：дәшィ |
| 89ST0LE | $6 カ \square<\tau$ | $\begin{array}{r} \tau \\ \varepsilon \triangleright 0 z 600 \cdot 0 \end{array}$ | $\begin{array}{r} 9 \\ \angle \varepsilon \varepsilon S t 00.0 \end{array}$ | StELL＇0 | 0 | 0EL | TOST | 9926 | 009 | $\varepsilon \downarrow \varepsilon \tau$ | ع S－ST 7－عT：дәшя |
| 0＜tヵTLE | L908T | $\begin{array}{r} \tau \\ \mathrm{S} 169600{ }^{\circ} \\ \hline \end{array}$ | $\begin{array}{r} \tau \\ \varepsilon \triangleright \angle 8 t 00 \cdot 0 \end{array}$ | ttGLL＇0 | 0 | $\angle \nabla L$ | LTST | ZTEL | 00G | 8TET | S S－ET 7－عT：дәш» |
| L86TZLE | T9SIZ | 6LSGOTO 0 | $\begin{array}{r} 6 \\ \text { 1928 } 0000 \\ \hline \end{array}$ | 80t8LLO | 0 | $87 L$ | 88ヤT | ZTEL | 00G | Z0\＆T |  |
| ZSZITLE | L908T | $\begin{array}{r} \mathrm{T} \\ 060 \angle 600 \cdot 0 \\ \hline \end{array}$ | LI888ヤ00＊0 | 8STGLLO | 0 | trL | 8TST | ZTEL | 009 | 91ET | S S－IT 7－عT：дәшィ |
| ESZ6TLE | 0ZIZZ | LヵZLOTO＇0 | $\begin{array}{r} \varepsilon \\ 0 \tau \square 8 \vdash 00{ }^{\circ} \end{array}$ | 8SZ8LL＇0 | 0 | $97 L$ | 88ヤT | ZTEL | 009 | 662T |  |
| 8ヤE8LSE | 90ヤてT | $\begin{array}{r} 9 \\ 8989 \angle 00^{\circ} \end{array}$ |  | Z660SL＇0 | 0 | T99 | TOもT | 9702 | 00G | †Zとโ | ャ S－6T 7－عโ：дəш» |
| 098LE9E | 629ヵT | $\begin{array}{r} \mathrm{S} \\ 9082800 \cdot 0 \end{array}$ | $\begin{array}{r} \varepsilon \\ 9 Z 6 乙+00{ }^{\circ} \end{array}$ | LELT9L＇0 | 0 | †69 | TんカT | ع976 | 00G | てฤ¢โ | ャ S－LT 7－عT：дәш» |
| LEt869E | T0\＆ET | 88LT0800＇0 | $\begin{array}{r} \tau \\ \varepsilon \\ \hline \end{array}$ | G6TLL＇0 | 0 | て\＆L | 6TST | 9976 | 009 | £S¢T | ャ S－ST 7－عT：дәш» |


| 6TE0Tぃ | S6ES | $\begin{array}{r} 9 \\ 76 T \angle S 00 \cdot 0 \end{array}$ |  | SE8SZL＇0 | 0 | 289 | 0TZT | S8Z9 | 00G | $6 ヵ$ CT |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 8ZヤGLEE | 9999 | tヵS9S00＇0 | $\begin{array}{r} \varepsilon \\ 2886 \varepsilon 00^{\circ} 0 \end{array}$ | 6ャOZL＇0 | 0 | 799 | LLIT | S8Z9 | 00G | โદてT |  |
| ZS999ヵを | ャTZ9 | S6L6S00＇0 | LL6Tt00'0 | E09EL＇0 | 0 | ャโ9 | LSZT | S8Z9 | 009 | ELZT |  |
| LTLTStE | S89G | $\begin{array}{r} 9 \\ \text { L9999000 } \\ \hline \end{array}$ | $\begin{array}{r} 6 \\ \downarrow \varepsilon ャ 0 ャ 00 \cdot 0 \\ \hline \end{array}$ | 6GZZEL＇0 | 0 | 269 | $\angle \triangleright Z \tau$ | S8Z9 | 00G | GGZT |  |
| Z976ESE | 099G | T68L900＇0 | $\begin{array}{r} 9 \\ 0 Z 0 Z \vdash 000 \end{array}$ | LOt $97 L^{\prime} 0$ | 0 | $8 \vdash 9$ | 8عદ | 970 | 00G | 962T | 乙 S－TZ 7－عโ：גəш» |
| 88GLOGE | St8G | $\begin{array}{r} 8 \\ 89 Z \angle S 000 \end{array}$ | $\begin{array}{r} \varepsilon \\ 00 \angle 0 \triangleright 00^{\circ} 0 \end{array}$ | GL8TtL＇0 | 0 | 979 | Z0\＆โ | 970 | 00G | 6LZT |  |
| †68ヶ6¢ | 七Z68 | $\begin{array}{r} 6 \\ 09 Z 89000 \end{array}$ | $\begin{array}{r} \varepsilon \\ 909 \varepsilon \vdash 00^{\circ} \end{array}$ | tGLtGL＇0 | 0 | $9 \angle 9$ | ย8ะโ | 970 | 00G | ZTET | 乙 S－6T 7－عโ：」əш» |
| \＆ZZS9SE | EGL8 | $\begin{array}{r} 8 \\ \varepsilon 00 \angle 9000 \\ \hline \end{array}$ | $\begin{array}{r} \varepsilon \\ \angle T 9 Z \succ 00^{\circ} 0 \end{array}$ | 8Z80GL＇0 | 0 | 679 | 8SET | 970 | 009 | G62T | ¢ S－6T 7－عโ：גəшу |
| T6LLロ9E | STEカT | $\begin{array}{r} 9 \\ \dagger \mathrm{G} 9 \mathrm{Z} 8000 \\ \hline \end{array}$ | $\begin{array}{r} \tau \\ 9 \varepsilon \angle \varepsilon+00^{\circ} \end{array}$ | L66t9 ${ }^{\prime} 0$ | 0 | 802 | OヤカT | ع976 | 00G | LZET | 乙 S－LT 7－عI：גəш＞ |
| 0088Z98 | LLZET | $\begin{array}{r} L \\ \angle S E 6 \angle 00 \circ \end{array}$ | $\begin{array}{r} \tau \\ 0 \tau 0 \varepsilon \triangleright 00 \cdot 0 \end{array}$ | 89力て92．0 | 0 | S89 | LTヵT | ع976 | 00G | OTET | T S－LT 7－हI：גəшя |
| 8LSt0LE | ZS6ST | $\begin{array}{r} \varepsilon \\ 9 \mathrm{G} \angle \angle 800^{\circ} \end{array}$ | tLOSt00＇0 | 6LEtLL＇0 | 0 | てもL | 88ヵ $\tau$ | 8ヵT6 | 00G | LعET | 乙 S－SI 7－عI：גəшメ |
| てヤOヤL9E | \＆ZO†T | $\begin{array}{r} \varepsilon \\ \angle 982800^{\circ} 0 \end{array}$ | $\begin{array}{r} 8 \\ \text { SIOSt00.0 } \end{array}$ | 9200LL＇0 | 0 | ZZL | $6 ヤ \square \tau$ | 8ャ76 | 00G | ヤTET | T S－ST 7－عI：גəшу |
| SELIZLE | T888T | $\begin{array}{r} \mathrm{I} \\ 70986000 \end{array}$ | $\begin{array}{r} 9 \\ \text { ZLE8৮00'0 } \end{array}$ | ちてT6LL＇0 | 0 | L $\downarrow$ L | T8ヶT | D6TL | 00G | G6ZT |  |
| 900989E | 6608T | $\begin{array}{r} 9 \\ \varepsilon \angle 896000 \end{array}$ | $\begin{array}{r} \varepsilon \\ \angle \forall Z 8 \vdash 00^{\circ} 0 \end{array}$ | LEZ9LL＇0 | 0 | tZL | 8عャ $\tau$ | D6TL | 00G | 9LZT |  |
| とヤt8TLE | Z668T | $\begin{array}{r} 8 \\ \text { †T } 28600 \cdot 0 \end{array}$ | $\begin{array}{r} 8 \\ \varepsilon \triangleright \tau 8 \vdash 000 \end{array}$ | 7868LL＇0 | 0 | ttL | T8ヶ $\tau$ | D6TL | 00G | Z6ZT | て S－IT フ－¢โ：」əшя |
| 0097898 | S9TLT | $\begin{array}{r} 2 \\ \angle 88 \mathrm{t} 6000 \end{array}$ | $\begin{array}{r} \nabla \\ \varepsilon \triangleright \angle 8 \vdash 00^{\circ} 0 \end{array}$ | 96T9LL＇0 | 0 | tZL | 8عャT | D6TL | 00G | GLZT |  |
| GZLOOtE | 8てもして | $\begin{array}{r} 9 \\ 800 \mathrm{~g} \angle 00 \end{array}$ | $\begin{array}{r} \text { Z } \\ \text { S89 } \end{array}$ | 9ZEZL＇0 | 0 | ELS | 乙ZてT | S8Z9 | 00G | E92T |  |
| 88ZてTぃE | 8069 | 809t900＇0 | $\begin{array}{r} \varepsilon \\ 88 \triangleright \tau \triangleright 00^{\circ} 0 \end{array}$ | LOtGZL＇0 | 0 | 8LG | 8TZT | S8Z9 | 009 | 092T | ャ S－GZ 7－عโ：גəш» |
|  |  | 乙 |  |  |  |  |  |  |  |  |  |


| †G600ع¢ | でLLLIT | 896ヶでロ＊ 0 | 8LOELOO＇0 | G600ZL＇0 | 0 | 8LS | LSET | 8TG8 | 00G | SSEI |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 6L0Z8ZE | ZS09TI | 9StITちO＊ | で七てLO0＇0 | 9928TL＇0 | 0 | †99 | 0ヵ¢ | E9GL | 00G | 6ع\＆โ |  |
| 9†08ヤて\＆ | TSS80T | 98IE6E0＇0 | TLOZLOO＇0 | でSカtLぐ0 | 0 | OSS | 60\＆T | E9GL | 009 | น८\＆โ |  |
| LESISIE | ZST90t | †062680＇0 | Z ZTE6900 | 7G9LOL＇0 | 0 | 乙Zら | 86IT | E9GL | 009 | ヤGZT |  |
| 6789862 | 6L698 | 99967EO＇0 | عカIL900＊0 | IE6Z89＊0 | 0 | 0 | 200T | 90T9 | 00G | 8EIT |  |
| SEtSZSZ | L8EGL | TGZ67E0＇0 | S9ti900：0 | LヵEとZ9＇0 | 0 | 0 | LEL | Lt9G | 00G | 986 |  |
| 092LI6T | でヤロロ | 898T920＊0 | $\begin{array}{r} 8 \\ 0979500 \cdot 0 \end{array}$ | †Z6EZs＇0 | 0 | 0 | 629 | Sع9E | 009 | 988 | L лоэ ${ }^{-}$dxә－عт：дәшя |
| L96SSZT | \＆G9tz | G9GsIZ0＇0 | $\begin{array}{r} \text { ? } \\ 0889700 \% \end{array}$ | 6ZE6LE0 | 0 | 0 | 0 | Z80乙 | 00G | ZZL |  |
| 69EてE8 | TSt9 | L2680T0＇0 | $\begin{array}{r} \varepsilon \\ 69 Z Z \varepsilon 000^{0} \end{array}$ | عと809て＇0 | 0 | 0 | 0 | S88T | 009 | 289 | $\varepsilon \wedge 0{ }^{-}$dxә－¢т：дәшх |
| 96280G | LもGZT | 8TOTE0＇0 | LZてTLO0＇0 | 2T9LSt＇0 | 0 | 0 | 0 | LOGZ | 009 | LEL |  |
| 886209 | LもGZT | 68TETE0＇0 | ZSSTLO0＇0 | ZS8SST＇0 | 0 | 0 | 0 | LOGZ | 009 | 98L |  |
| † 2868 t | LもGZT | 6とて8TE0＊0 | ع9Z0L00＇0 | SEZST＊0 | 0 | 0 | 0 | LOGZ | 00G | て\＆L |  |
| LOZ8St | 0ヤ0ZT | StLZZEOO | て978900．0 | STSttio | 0 | 0 | 0 | LOGZ | 009 | 9ZL |  |
| 89ヵらโァ | โヵG6 | LヤIE6Z0＇0 | $\downarrow$ ¢ $20 \angle 00{ }^{\circ}$ | $9 ヵ$ ¢てET0 | 0 | 0 | 0 | LOGZ | 009 | OZL |  |
| 〉8StEE | Z268 | 6TZ9EE0＇0 | $\begin{array}{r} 8 \\ 080 \angle L 00 \cdot 0 \end{array}$ | Z8S80T＇0 | 0 | 0 | 0 | LOGZ | 009 | SOL |  |
| ャ¢8Tヶて | 2079 | TOSSZE0＇0 | 8てt七t80000 | 28668L0＇0 | 0 | 0 | 0 | LOGZ | 00G | 269 |  |
| Lヤ892T | L69t | SZSTVt0＇0 | S8S $2800{ }^{8} 0$ | 8968てヤ0＊0 | 0 | 0 | 0 | 8LZT | 00G | عャ9 |  |
| SItEG | とてとて | ટદIZES0＇0 | 8LEOZTO＊ | 906S8T0＇0 | 0 | 0 | 0 | 8LZT | 009 | Sع9 |  |
| St0\＆t | GZIT | 88T6760＇0 | Lヵ989T0＇0 | L96 $29700^{\circ} 0$ | 0 | 0 | 0 | ع＜8 | SOS | Z6S |  |
| S $\angle \downarrow \tau$ | 0 | 9T0t900＊${ }^{6}$ | 9โ0t900＊0 | $\begin{array}{r} L \\ \mathrm{GZ} 6 \nabla \mathrm{~S} 000 \div \end{array}$ | 0 | 0 | 0 | عL8 | Z09 | LEL |  |
| IIV | paddeuun | 10．1或 | 10113 | әбеләлоว | 06N | GLN | OSN | xew | u！N | ueวN |  |



| ャ6ELTSE | I9992 | 66662T0＊0 | L97GS00＊0 | S9967L＇0 | 0 | $\angle 99$ | †TSI | 8Sカ6 | 009 | IZヤT |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ع6IZ8ャE | とャt0Z | 9IITO＊0 | 668tS00－0 | LSELDL＇0 | 0 | 9G9 | 9んカて | 8St6 | OOS | Z6\＆โ |  |
| 9力tて8Eと | 92L6T | 78860T0 0 | 00ZZS00．0 | L66EL＇0 | 0 | 629 | ع9ET | 76T6 | 009 | LIET |  |
| ャ97L6TE | LTSTZ | E9Z9It0 0 | TGL6700＊0 | †892ZL＇0 | 0 | L9G | 8SIT | 6โヶ8 | 009 | 66IT |  |
| 6SE8E8Z | Lヵ96T | 2082TIO＇0 | ع9Ett00．0 | 890ع89＇0 | 0 | 0 | 968 | ع897 | OOS | 8EOT | L $10 Ј^{-}$dxə－ 2 L：дәшя |
| LITZOヵZ | 0SE8 | 918TL00＇0 | $\begin{array}{r} 9 \\ \succ 0 \varepsilon \angle \varepsilon 00 \cdot 0 \\ \hline \end{array}$ | E8T9T9＊0 | 0 | 0 | † 29 | LITD | 009 | S06 |  |
| โ60IZTZ | 8STI | $\begin{array}{r} \mathrm{T} \\ 00 t 9 \varepsilon 00 \cdot 0 \\ \hline \end{array}$ | $\begin{array}{r} \mathrm{g} \\ 0960 \varepsilon 00: 0 \\ \hline \end{array}$ | D88LGS ${ }^{\circ}$ | 0 | 0 | Z8S | LITD | 009 | $\angle 88$ |  |
| ZSEャ9¢\＆ | LZE6† | 七ET00ZO＊ | $\begin{array}{r} L \\ 0 \varepsilon s t 900: 0 \end{array}$ | 9SG6SL＇0 | 0 | LIL | 909T | SStIT | 009 | ع9†T |  |
| L七6T998 | IZ\＆6† | 98LOOZO＇0 | $\begin{array}{r} \varepsilon \\ 6609900 \cdot 0 \end{array}$ | ZST6SL＇0 | 0 | STL | S6SI | SStIT | 009 | 297 |  |
| カヤZ6SSE | LZE6† | 6SZ66T0＇0 | $\begin{array}{r} 6 \\ 8 \triangleright \& 900 \\ \hline \end{array}$ | ZZ08SL＇0 | 0 | ITL | E8ST | SStIT | 009 | 6SカT | 6T＾оЈ dxə－St：дəuメ |
| と90tロらE | †8009 | 99T00ZO＇0 | $9997900 \cdot{ }^{9}$ | 696SSL＇0 | 0 | 969 | SLST | SStIT | OOS | LStT | LT＾о才 dxə－¢T：дəшメ |
| と9โちてらع | †t¢6ヶ | 90286T0 0 | SSST900＊0 | ITStSL＇0 | 0 | $\angle 89$ | $\varepsilon \vdash S \tau$ | $\varepsilon \varepsilon 86$ | 009 | てヤワT |  |
| とャ0T8ち¢ | て602ヵ | †S8LTO＇0 | $\begin{array}{r} 6 \\ 08 \angle 6900 \cdot 0 \\ \hline \end{array}$ | S6909L＇0 | 0 | 699 | OTST | عદ86 | 009 | TOヤT |  |
| 08L9LEE | โ6โE\＆ | S8ESST0＇0 | $\begin{array}{r} 6 \\ 0 z 98900 \cdot 0 \\ \hline \end{array}$ | ててTもぐ0 | 0 | 829 | 9ZET | عદ86 | 009 | ITET | IT＾оЈ dxə－¢T：дəшх |
| T686STE | てぃ9โE | StEsto 0 | S8tS00＇0 | 6620ZL＇0 | 0 | 6GG | IZII | عદ86 | 00G | GLII |  |
| LSZE9LZ | 6ZTIE | 6LL8ST0＇0 | $\begin{array}{r} 9 \\ \nabla \tau 6 \angle \triangleright 00.0 \\ \hline \end{array}$ | $\angle S t 0 \angle 90^{\circ}$ | 0 | 0 | $\downarrow$ ๑8 | $\downarrow$ ¢ャG | 009 | 000T | L＾о才 ${ }^{\text {dx }}$－ST：дәшу |
| นてLも0¢て | カてヤてて | 8L88てT0 0 | $6 \tau \tau \angle 00 \cdot 0^{9}$ | LT8869 0 | 0 | 0 | てヤ9 | L9Tt | 009 | LL8 |  |
| LعとદZOZ | 0عャ8 | $\begin{array}{r} 8 \\ \text { Z } \wp \text { G } 2000 \\ \hline \end{array}$ | ZT8ITE00＇0 | 8T8LES＇0 | 0 | 0 | OSS | L9Tt | 009 | SS8 | $\varepsilon \wedge 0 Ј$ dxə－¢T：дәшя |
| 099てTとを | 6S66IT | カIS6Tち00 | $\begin{array}{r} \varepsilon \\ \text { ZLSZLOO.0 } \end{array}$ | て\＆とてL＇0 | 0 | 689 | โ9\＆โ | 8TS8 | 00 s | $\downarrow$ ¢ $\downarrow$ | $\varepsilon 乙 ~ \wedge о ว-d x ə-\varepsilon \tau:$ дəш» |
| とヤワ80¢\＆ | 6S66IT |  | $\begin{array}{r} 2 \\ 8 \angle \hbar Z \angle 00^{\circ} \end{array}$ | 8L6IZL＇0 | 0 | 989 | 6SET | 8TG8 | 009 | $\downarrow$ ャ¢T |  |
|  |  |  | 6 |  |  |  |  |  |  |  |  |


| عદZLSE\＆ | TSTST | †G6E600＇0 | 8ヵて6ヤ00＊0 | Z6T0EL｀0 | 0 | S09 | てTET | T929 | 009 | S0\＆T |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 9ちてILZE | OLTST | LS0t600＇0 | ¢sटLt00＊0 | S96TL＇0 | 0 | Z99 | StIT | 1929 | 00G | 七0ZT |  |
| 功T06て | ع\＆¢9T | ع806600＇0 | S992t00＊0 | ELS889＇0 | 0 | 0 | 976 | 8โ99 | 009 | ESOT | L лоэdxə－І乙：ıəшя |
| L88T9才Z | STEL | ¢ $2 \in \angle 7900 \cdot 0$ | てIZSE00＊0 | TL8Z9＇0 | 0 | 0 | †69 | てT9＊ | 00G | ZZ6 |  |
| 66S9LIZ | 七七T\＆ | ¢T99700＇0 |  | ZL8ZLS＇0 | 0 | 0 | 209 | てT9ヵ | 00G | 006 |  |
| 0LOtISE | LZ9ET |  | ［ ${ }^{\text {L }}$ | 6ST8tL＇0 | 0 | $\angle 89$ | Z8ヵโ | โてヤ8 | 00S | 0Zャt |  |
| ESLITSE | LZ9ET | 26Eカ600＊${ }^{\text {L }}$ | SS6SG00＇0 | $62 t \angle \downarrow L \prime 0$ | 0 | †89 | 08ヵT | てZヤ8 | 00G | OZャT |  |
| t986098 | LZ9ET | $\begin{array}{r} \varepsilon \\ \text { S} \square \nabla t 6000 \\ \hline \end{array}$ | $\begin{array}{r} L \\ \text { T86ss00.0 } \end{array}$ | 8689tL＇0 | 0 | I89 | 8LヵT | น乙ヤ8 | 009 | 9IちT |  |
| EtGGOSE | ZOEヵT | $\begin{array}{r} \varepsilon \\ \tau S \angle t 600^{\circ} \\ \hline \end{array}$ | $\begin{array}{r} \text { L } \\ 6 \varepsilon \varepsilon \triangleright s 00 \cdot 0 \end{array}$ | St89tL＇0 | 0 | $\varepsilon \angle 9$ | $0 \angle \nabla \tau$ | โてヤ8 | 009 | カエヤI |  |
| $\varepsilon \angle t \square 6 \square \varepsilon$ | カーナカT | $\begin{array}{r} 9 \\ 0 \angle 8+600 \cdot 0 \end{array}$ | $\begin{array}{r} 6 \\ \varepsilon \text { عIO†SOO } \\ \hline \end{array}$ | LI8StL＇0 | 0 | 999 |  | てZヤ8 | 009 | 90ヵT |  |
| ヤTEZ9ヵ¢ | 90LET | $\begin{array}{r} \text { L } \\ 88 \mathrm{~s} 2600 \end{array}$ | $\begin{array}{r} 6 \\ 89 \varepsilon \varepsilon ร 000 \end{array}$ | LS92tL＇0 | 0 | ャS9 | LてカT | โてヤ8 | OOS | ヤ8\＆โ |  |
| ヤ0TE6\＆ะ | LS60T | $\begin{array}{r} 2 \\ \nabla 9 \tau \downarrow 800 \circ 0 \end{array}$ | カヤTZS00＇0 | ャع6SEL＇0 | 0 | عZ9 | S9ET | てZヤ8 | 009 | 8ZとT |  |
| LZ08ててE | عIEOT | $\begin{array}{r} 9 \\ \text { T8S0800'0 } \\ \hline \end{array}$ | $\begin{array}{r} 9 \\ 0688 \vdash 00 \cdot 0 \\ \hline \end{array}$ | L6ちZZL＇0 | 0 | GLS | ELII | て乙セ8 | 009 | 6IZT |  |
| L8t0062 | TVLOT | $\begin{array}{r} \nabla \\ 6 \mathrm{~S} 66 \angle 00^{\circ} \end{array}$ | $\begin{array}{r} 8 \\ \text { ع } \\ \hline \end{array}$ | $60689{ }^{\circ} 0$ | 0 | 0 | 826 | 6 699 | 009 | 6S0T | L＾о才 dxә－6โ：дәшу |
| 8800Ltて | LGL8 | $\begin{array}{r} 6 \\ \angle 880 \angle 00^{\circ} 0 \\ \hline \end{array}$ | L89SE00＇0 | 8LL9Z9＇0 | 0 | 0 | $\angle 69$ | SEtt | 009 | Z26 | G＾о才 dxə－6โ：גəш＞ |
| 8\＆IZ9Tて | 0ع92 | $\begin{array}{r} 8 \\ \downarrow \tau Z \varepsilon ャ 00 \cdot 0 \end{array}$ | $\begin{array}{r} \mathrm{G} \\ \varepsilon 0 \tau \tau 00 \cdot 0 \end{array}$ | Z9ES9S＇0 | 0 | 0 | L6G | SEtt | 009 | †06 |  |
| T989ちGE | ع6982 | とてL9ET0＇0 | 乙ع69900＇0 | T68ちGL＇0 | 0 | ¢02 | ESSI | 8St6 | OOS | 9عャI |  |
| ع6† | †TS8Z | 80T9ET0＇0 | SEL9S00＇0 | 960tSL＇0 | 0 | Z69 | ESSI | 8St6 | 009 | LEカT |  |
| G68TtSE | †TS8Z | 8L8SETO＇0 | $\begin{array}{r} 6 \\ 99 \triangleright 9 \mathrm{GO} \\ \hline \end{array}$ | LT6ESL＇0 | 0 | S89 | $\varepsilon \dagger S T$ | 8St6 | OOS | SEャT |  |
| 6791ESE | ELELZ | عLEZETO＇0 | $\begin{array}{r} L \\ \text { I689s00'0 } \end{array}$ | †LIZSL＇0 | 0 | † 29 | LZST | 8St6 | 009 | 6てカT |  |
|  |  |  | 2 |  |  |  |  |  |  |  |  |


| で96Lもて | 0989 | $\begin{array}{r} L \\ \tau \varepsilon \triangleright \tau 900 \circ 0 \end{array}$ | $\begin{array}{r} \square \\ 9 \varepsilon 6 \varepsilon \varepsilon 00 \cdot 0 \\ \hline \end{array}$ | カ0IZZ9＇0 | 0 | 0 | Z69 | IZtS | 009 | 676 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ST6ILIL | カャOZ | 6Z68800＇0 | $\begin{array}{r} 9 \\ \text { †GS6Z00.0 } \end{array}$ | 68TS99＇0 | 0 | 0 | L6S | IZヶG | 009 | $\angle 68$ |  |
| Lヤ60LEE | TLEZZ | ZS9TIO＇0 | $\begin{array}{r} \varepsilon \\ 6260900.0 \end{array}$ | 9tヵてL＇0 | 0 | E8S | ヤLZT | 9889 | 00S | 9TET |  |
| 0¢6TLEE | TLEZて | 69t91T0＇0 | $\begin{array}{r} L \\ 9680900 \end{array}$ | 980GZL＇0 | 0 | S89 | †LZT | 9889 | 009 | 9IET |  |
| 88TELEE | てZ\＆8T | L8ZヤOT0＇0 | $\begin{array}{r} 8 \\ 9 \varepsilon s 0900 \\ \hline \end{array}$ | ع9tt ${ }^{\text {a }}$ | 0 | 789 | GLZT | 9889 | OOS | 9IET |  |
| ZZ8GLEE | L679T | $\begin{array}{r} \quad \stackrel{7}{\circ} \\ \text { s9z6600 } \end{array}$ | $\begin{array}{r} \nabla \\ \text { Z880900 } \end{array}$ | LT8tZL＇0 | 0 | S8S | SLZT | 9889 | 00S | STET |  |
| عT00LE | 9GLST | $\begin{array}{r} 2 \\ \text { s } \angle 99600^{\circ} \end{array}$ | $\begin{array}{r} L \\ \varepsilon L E O G 00 \circ \end{array}$ | T9LもZL＇0 | 0 | †89 | ELZT | 9889 | 00S | てIET | SI $10{ }^{-}$dxə－عZ：дəшィ |
| LعT97EE | とで9 ${ }^{\text {a }}$ | ع689600＊0 ${ }_{\text {® }}$ | $\begin{array}{r} 9 \\ 88 z 8+00 \cdot 0 \\ \hline \end{array}$ | 9LIZZL＇0 | 0 | † $\angle$ S | †GZT | 9889 | 009 | 00\＆T |  |
| OSSS62E | とで9 | $\begin{array}{r} L \\ \angle 099600 \end{array}$ | $\begin{array}{r} 2 \\ 0 \mathrm{~S} 99700 \cdot 0 \end{array}$ | 8Lt6TL＇0 | 0 | 299 | EIZT | 9889 | 009 | 692T |  |
| 8STE8TE | て92ちT | $\varepsilon$ 8 ¢ 28800 | $\begin{array}{r} 8 \\ 0 \text { OLてカナ0 } 0 \end{array}$ | 90260 ${ }^{\prime} 0$ | 0 | 6Z9 | OZIT | 6โ99 | 009 | TOZT |  |
| 0G97682 | 8ZOST | $\begin{array}{r} 8 \\ 0 \mathrm{~S} Z \mathrm{O} 600 \cdot 0 \end{array}$ | $\begin{array}{r} 2 \\ \varepsilon I 80 t 000^{0} \end{array}$ | †SOZ89＊0 | 0 | 0 | عT6 | 6 699 | 009 | LSOT |  |
| て9عと97て | 68EL | t E888900 | $\begin{array}{r} \nabla \\ 6 \angle 0 t \varepsilon 00 \cdot 0 \end{array}$ | 8LEZ9＇0 | 0 | 0 | 769 | 6T7G | 009 | 026 | ¢＾оЈ ${ }^{-}$dxə－ع乙：дәшу |
| てعL09Iて | SZ9t | $67 t 0500^{\circ} 0$ | ZZST6Z00＊ | 7S8S99＇0 | 0 | 0 | 七6S | 6TちG | 009 | $\varepsilon 68$ |  |
| 6988tte | 92912 | L09SITO＇0 | $\begin{array}{r} 2 \\ \nabla 8 เ \varepsilon \varsigma 00 \cdot 0 \end{array}$ | †عELEL＇0 | 0 | 089 | S8ET | LS69 | 009 | S9ET |  |
| t0009tE | ZG602 | LSSEITO＇0 | $\begin{array}{r} 6 \\ \text { sISES00:0 } \\ \hline \end{array}$ | Z8ELEL＇0 | 0 | 0ع9 | ヤ8\＆โ | LS69 | 009 | S9ET |  |
| カ6G6tte | Z9602 | ZLヤEITO＇0 | $\begin{array}{r} \mathrm{L} \\ \varepsilon 乙 \succ \varepsilon S 00 \end{array}$ | $88 G L E L{ }^{\prime} 0$ | 0 | 0ع9 | ฤ8\＆โ | LS69 | OOS | ع9ET | 6โ＾оЈ ${ }^{\text {d }}$ dxə－โて：ıəшメ |
| LZLLロナE | Z9602 | 9عZEITO＇0 | $\begin{array}{r} 6 \\ \text { EGIES00.0 } \end{array}$ | 8t9LEL＇0 | 0 | 879 | 8LET | LS69 | 009 | 09ET |  |
| てTムIナナを | 6ZS8T | E6ZSOT0＇0 | $\begin{array}{r} \mathrm{G} \\ \text { عZOZs00.0 } \end{array}$ | $67 \varepsilon 9 \varepsilon L{ }^{\circ}$ | 0 | SZ9 | 9LET | LS69 | 00S | 8SET |  |
| 68T9โ七E | 69S8T | TLZSOTO＇0 | $\begin{array}{r} \mathrm{G} \\ 9 \text { ISTS00 } \end{array}$ | SZOtEL＇0 | 0 | ST9 | عऽยโ | LS69 | 009 | عゅET |  |
|  |  | $\varepsilon$ | 6 |  |  |  |  |  |  |  |  |

kmer：21－Llo（Lm） 23 －Slo（Sm）0－DR 17500 kmer：21－Llo（Lm） 23 －Slo（Sm） 0 －DR 17300



 kmer：21－Llo（Lm） 21 －Slo（Sm） 0 －DR 21150 kmer：21－Llo（Lm） 21 －Slo（Sm） 0 －DR 19150 kmer：21－Llo（Lm） 19 －Slo（Sm） 0 －DR 17500

 kmer：21－Llo（Lm） 19 －Slo（Sm） 0 －DR 19150 －Lt 15－St 4－P kmer $13-$ K（Kmerg） 21


| てヵ970ع์ | L8SET | $\begin{array}{r} L \\ 6 \tau \varepsilon 8800 \cdot 0 \end{array}$ | $\begin{array}{r} 6 \\ 0 \varepsilon s \angle \triangleright 00 \cdot 0 \end{array}$ | D86ITL＇0 | 0 | $\dagger$ ¢ | LLIT | 9889 | 009 | OLZT | عZ＾оכ dxə－¢Z：ıəшメ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 8ャ6Z0\＆ع | L8SET | $\begin{array}{r} \nabla \\ 9 \angle 188000^{\circ} \end{array}$ | $\begin{array}{r} \tau \\ \varepsilon 0 t \angle t 00^{\circ} 0 \end{array}$ | G60ZTL＇0 | 0 | ttG | SLIT | 9889 | 00G | 692T |  |
| T0TZ0E\＆ | L8SET | $\begin{array}{r} 6 \\ 8008800 \cdot 0 \end{array}$ | $\begin{array}{r} 9 \\ \text { †てZ८৮0.0 } \end{array}$ | 9LLITL＇0 | 0 | $\varepsilon \dagger G$ | SLII | 9889 | 009 | OLZT | 6I＾0Ј dxə－¢Z：дəшメ |
| LEt00E\＆ | L8SET | $\begin{array}{r} \tau \\ 8 \tau 0 \angle 800^{\circ} 0 \end{array}$ | 6029b00＇0 | 乙ЕITL＇0 | 0 | OちG | DLII | 9889 | 00G | 692T |  |
| 96LE6ZE | L8SET | $\begin{array}{r} L \\ \varepsilon 8 \tau \angle 800^{\circ} 0 \end{array}$ | $\begin{array}{r} \tau \\ \varepsilon 6 z 9 t 00^{\circ} 0 \end{array}$ | てعZOTL＇0 | 0 | 88G | 897I | 9889 | 00G | 892T |  |
| 8ャLZ8ZE | 6ZSt $T$ | 9978800＇0 | $\begin{array}{r} 8 \\ 66 \mathrm{St}+00 \\ \hline \end{array}$ | 七\＆Z60L＇0 | 0 | $\downarrow$ ¢G | †9II | 9889 | 009 | E92T |  |
| 0\＆StGZE | 06L0T | Et89 ${ }^{6} 00^{\circ} 0$ | $\begin{array}{r} 6 \\ +\nabla 6 \varepsilon t 00 \cdot 0 \\ \hline \end{array}$ | 七E9LOL＇0 | 0 | 97S | てヵII | 9889 | 009 | てもくT |  |
| 8GL9GTE | 8060T | g ${ }^{8}$ | 98ヶてヤ00\％ | †TIZOL＇0 | 0 | OTS | 8LOT | L98G | 00G | 78IT |  |
| ELLST6Z | $88 \angle 8$ | ヵTG6900 ${ }^{\text {L }}$ | $\begin{array}{r} L \\ \square 8 \mathrm{~S} 6800 \cdot 0 \end{array}$ | LLL8L9＇0 | 0 | 0 | عโ6 | 2T8G | 009 | 990T |  |


| Parameter Settings | N50 |
| :---: | :---: |
| kmer:19-exp cov 27 | 1435 |
| kmer:21-exp_cov 17 | 1379 |
| kmer:21-exp_cov 27 | 1379 |
| kmer:23-exp_cov 17 | 1285 |
| kmer:23-exp_cov 27 | 1293 |
| kmer:21-exp_cov 7 | 935 |
| kmer:23-exp_cov 7 | 935 |
| kmer:19-exp_cov 17 | 1427 |
| kmer:19-exp_cov 27 | 1435 |
| kmer:19-exp_cov 7 | 901 |
| kmer:19-exp_cov auto | 1110 |
| kmer:21-exp_cov 17 | 1379 |
| kmer:21-exp_cov 7 | 936 |
| kmer:21-exp_cov auto | 1196 |
| kmer:23-exp_cov auto | 1160 |

Table 4B - Evaluation of homology-guided assembly on real world data with VELVET (utilizing left-over reads).
kmer:21-Llo(Lm)
kmer:21-Llo(Lm) 21 -Slo(Sm) 0 -DR 17150
kmer:21-Llo(Lm) 23 -Slo(Sm) 0 -DR 17150


